Package: TreEvo (via r-universe)

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Type Package

Title Using ABC to Understand Trait Evolution

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Description Various functions for estimating parameters of trait evolution in comparative analyses using Approximate Bayesian Computation.

License GPL

URL <https://github.com/bomeara/treevo>

BugReports <https://github.com/bomeara/TreEvo/issues>

Depends R $(>= 3.5.0)$, ape

Imports coda, fastmatch, foreach, graphics, grDevices, MASS, methods, parallel, partitions, phylolm, phytools, pls, RcppZiggurat, rgl, stats, utils, corpcor, mvtnorm, covr

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TreEvo-package *TreEvo–abc for comparative methods*

Description

A package for applying Approximate Bayesian Computation to estimating parameters of trait evolution in comparative analyses.

Details

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Author(s)

Brian O'Meara, Barb L. Banbury, David W. Bapst

Maintainer: David Bapst <dwbapst@gmail.com>

Examples

example analysis, using data simulated with TreEvo

```
set.seed(1)
# let's simulate some data, and then try to infer the parameters using ABC
# get a 20-taxon coalescent tree
tree \le rcoal(20)
# get realistic edge lengths
tree$edge.length <- tree$edge.length*20
genRateExample <- c(0.01)
ancStateExample <- c(10)
#Simple Brownian motion
simCharExample <- doSimulation(
   phy = tree,
    intrinsicFn = brownianIntrinsic,
    extrinsicFn = nullExtrinsic,
    startingValues = ancStateExample, #root state
    intrinsicValues = genRateExample,
    extrinsicValues = c(0),
    generation.time = 100000
    )
# NOTE: the example analyses below sample too few particles,
    # over too few steps, with too few starting simulations
    # - all for the sake of examples that reasonably test the functions
# Please set these values to more realistic levels for your analyses!
resultsBMExample <- doRun_prc(
  phy = tree,
  traits = simCharExample,
  intrinsicFn = brownianIntrinsic,
  extrinsicFn = nullExtrinsic,
  startingPriorsFns = "normal",
  startingPriorsValues = list(c(mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
  intrinsicPriorsFns = c("exponential"),
  intrinsicPriorsValues = list(10),
  extrinsicPriorsFns = c("fixed"),
  extrinsicPriorsValues = list(0),
  generation.time = 100000,
  nRuns = 2,
  nStepsPRC = 3,
  numParticles = 20,
```

```
nInitialSimsPerParam = 10,
jobName = "examplerun_prc",
stopRule = FALSE,
multicore = FALSE,
coreLimit = 1
\lambda
```
boxcoxTransformation *Box-Cox Transformation for Simulation Summary Values*

Description

boxcoxTransformation Box-Cox transforms summary values from a single simulation, while boxcoxTransformationMatrix Box-Cox transforms summary values from multiple simulations. The output of boxcoxTransformationMatrix needs to be provided as input for boxcoxTransformation.

Usage

boxcoxTransformation(summaryValuesVector, boxcoxAddition, boxcoxLambda)

boxcoxTransformationMatrix(summaryValuesMatrix)

Arguments

summaryValuesVector

Vector of summary statistics from a single simulation

boxcoxAddition Vector of boxcox additions from boxcoxTransformationMatrix

boxcoxLambda Vector of boxcox lambda values from boxcoxTransformationMatrix summaryValuesMatrix

Matrix of summary statistics from simulations

Value

boxcoxTransformation returns a vector of Box-Cox transformed summary statistics from a single observation. boxcoxTransformationMatrix returns a matrix of Box-Cox transformed summary statistics with the same dimensions as summaryValuesMatrix.

Author(s)

Brian O'Meara and Barb Banbury

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Examples

```
set.seed(1)
data(simRunExample)
# example simulation
simDataParallel <- parallelSimulateWithPriors(
 nrepSim = 5,
 multicore = FALSE,
 coreLimit = 1,
 phy = simPhyExample,
 intrinsicFn = brownianIntrinsic,
 extrinsicFn = nullExtrinsic,
 startingPriorsFns = "normal",
 startingPriorsValues = list(c(
    mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
 intrinsicPriorsFns = c("exponential"),
 intrinsicPriorsValues = list(10),
 extrinsicPriorsFns = c("fixed"),
 extrinsicPriorsValues = list(0),
 generation.time = 100000,
 checkpointFile = NULL,
 checkpointFreq = 24,
 verbose = FALSE,
 freevector = NULL, taxonDF = NULL)
nParFree <- sum(attr(simDataParallel, "freevector"))
# separate the simulation results:
 # 'true' generating parameter values from the summary values
summaryValuesMat <- simDataParallel[, -1:-nParFree]
boxTranMat <- boxcoxTransformationMatrix(
 summaryValuesMatrix = summaryValuesMat
 )
boxTranMat
boxcoxTransformation(
 summaryValuesVector = summaryValuesMat[, 1],
 boxcoxAddition = boxTranMat$boxcoxAddition,
 boxcoxLambda = boxTranMat$boxcoxLambda
 )
```
compareListIPD *Plot Interparticle Distance between Runs*

Description

This function plots interparticle distance (IPD) between runs for each free parameter.

Usage

```
compareListIPD(particleDataFrameList, verbose = FALSE)
```
Arguments

Value

Produces a plot with IPD between runs per generation.

Author(s)

Brian O'Meara and Barb Banbury

Examples

data(simRunExample)

```
pdfList <- list(resultsBMExample[[1]]$particleDataFrame,
     resultsBoundExample[[1]]$particleDataFrame)
```

```
compareListIPD(particleDataFrameList = pdfList, verbose = TRUE)
```


Run Approximate Bayesian Computation for Phylogenetic Compara*tive Methods*

Description

The doRun functions are the main interface for TreEvo users to do Approximate Bayesian Computation (ABC) analysis, effectively wrapping the [simulateWithPriors](#page-44-1) functions to perform simulations, which themselves are wrappers for the [doSimulation](#page-12-1) function. The two current doRun functions are doRun_prc which applies a partial rejection control (PRC) ABC analysis over multiple generations of simulations, and doRun_rej which performs a full rejection ('rej') ABC analysis.

Usage

```
doRun_prc(
 phy,
  traits,
  intrinsicFn,
  extrinsicFn,
  startingPriorsValues,
```
doRun

```
startingPriorsFns,
  intrinsicPriorsValues,
  intrinsicPriorsFns,
  extrinsicPriorsValues,
  extrinsicPriorsFns,
  numParticles = 300,
  nStepsPRC = 5,
  nRuns = 2,
  nInitialSims = NULL,
  nInitialSimsPerParam = 100,
  generation.time = 1000,
  TreeYears = max(branching.times(phy)) * 1e+06,
 multicore = FALSE,
  coreLimit = NA,
 multicoreSuppress = FALSE,
  standardDevFactor = 0.2,
  epsilonProportion = 0.7,
  epsilonMultiplier = 0.7,
  validation = "CV",
  scale = TRUE,
  variance.cutoff = 95,
  stopRule = FALSE,
  stopValue = 0.05,
  maxAttempts = Inf,
  diagnosticPRCmode = FALSE,
  jobName = NA,
  saveData = FALSE,verboseParticles = TRUE
)
doRun_rej(
 phy,
  traits,
  intrinsicFn,
  extrinsicFn,
  startingPriorsValues,
  startingPriorsFns,
  intrinsicPriorsValues,
  intrinsicPriorsFns,
  extrinsicPriorsValues,
  extrinsicPriorsFns,
  generation.time = 1000,
  TreeYears = max(branching.times(phy)) * 1e+06,
 multicore = FALSE,
  coreLimit = NA,
  validation = "CV",
  scale = TRUE,
  nInitialSims = NULL,
```
8 doRun and the state of th

```
nInitialSimsPerParam = 100,
 variance.cutoff = 95,
 standardDevFactor = 0.2,
  jobName = NA,
  abcTolerance = 0.1,checkpointFile = NULL,
 checkpointFreq = 24,
 savesims = FALSE
)
```
Arguments

"normal", 2 for "lognormal", 2 for "gamma", 1 for "exponential").

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Details

Both doRun functions take an input phylogeny (phy), observed trait data set (traits), models (intrinsicFn, extrinsicFn), and priors (startingPriorsValues, startingPriorsFns, intrinsicPriorsValues, intrinsicPriorsFns, extrinsicPriorsValues, extrinsicPriorsFns). Pulling from the priors, it simulates an initial set of simulations (nInitialSims). This set of simulations is boxcox transformed , and a PLS regression (see [methodsPLS](#page-27-1)) is performed for each free parameter to determine the most informative summary statistics (using variance.cutoff). The euclidean distance is calculated between each each initial simulation's most informative summary statistics and the input observed data.

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Following that step, the approach of the two functions diverge drastically.

For function doRun_rej, those simulations whose most informative summary statistics fall below abcTolerance are kept as accepted 'particles' (simulations runs), describing the posterior distribution of parameters. No additional generations of simulations are performed.

Coversely, function doRun_prc performs an ABC-PRC analysis, which follows a much more complicated algorithm with additional generations. In PRC, tolerance is set based on epsilonProportion and epsilonMultiplier, and the analysis begins with generation 1 and continues through a number of generations equal to nStepsPRC. Single simulation runs ('particles') are accepted if the distance of the most informative summary stats to the original data is less than this tolerance. A generation is complete when enough particles (numParticles) have been accepted. These particles make up the distribution for the next generation. The accepted particles from the final generation describe the posterior distributions of parameters.

Value

The output of these two functions are lists, composed of multiple objects, which differ slightly in their content among the two functions. For doRun_prc, the output is:

- input.data Input variables: jobName, nTaxa (number of taxa), nInitialSims, generation.time, TreeYears, timeStep, totalGenerations, epsilonProportion, epsilonMultiplier, nRuns (number of runs), nStepsPRC, numParticles, standardDevFactor.
- priorList List of prior distributions. This is used for doing post-analysis comparisons between prior and posterior distributions, such as with function plotPosteriors.
- particleDataFrame DataFrame with information from each simulation, including generation, attempt, id, parentid, distance, weight, and parameter states.
- toleranceVector Final tolerance vector.
- phy Input phylogeny.
- traits Input traits.
- simTime Processor time for initial simulations.
- time.per.gen Processor time for subsequent generations.
- postSummary Summarizes the posterior distribution from the final generation for all free parameters, giving the mean, standard deviation and Highest Posterior Density (at a 0.8 alpha) for each parameter.

If nRuns is greater than 1, the output from doRun_prc will be a list object composed of multiple output lists, as described.

- For doRun_rej, the output is:
- input.data Input variables: jobName, nTaxa (number of taxa), nInitialSims, generation.time, TreeYears, timeStep, totalGenerations, epsilonProportion, epsilonMultiplier, nRuns (number of runs), nStepsPRC, numParticles, standardDevFactor.
- priorList List of prior distributions. This is used for doing post-analysis comparisons between prior and posterior distributions, such as with function plotPosteriors.
- phy Input phylogeny.
- traits Input traits.

trueFreeValuesANDSummaryValues Parameter estimates and summary stats from all sims.

simTime Processor time for simulations.

abcDistancesRaw Euclidean distances for each simulation and free parameter.

- particleDataFrame DataFrame with information from each simulation, including generation, attempt, id, parentid, distance, weight, and parameter states.
- postSummary Summarizes the posterior distribution from the final generation for all free parameters, giving the mean, standard deviation and Highest Posterior Density (at a 0.8 alpha) for each parameter.
- parMeansList A list of parameter means for both fixed and unfixed parameters, sorted into a list of three vectors (starting, intrinsic, extrinsic).

Author(s)

Brian O'Meara and Barb Banbury

jobName = "examplerun_prc",

References

Sisson et al. 2007, Wegmann et al. 2009

```
set.seed(1)
data(simRunExample)
# NOTE: the example analyses below sample too few particles,
    # over too few steps, with too few starting simulations
    # - all for the sake of examples that demonstrate these
    # within a reasonable time-frame
## Please set these values to more realistic levels for your analyses!
resultsPRC <- doRun_prc(
 phy = simPhyExample,
 traits = simCharExample,
 intrinsicFn = brownianIntrinsic,
 extrinsicFn = nullExtrinsic,
 startingPriorsFns = "normal",
 startingPriorsValues = list(c(mean(simCharExample[, 1]),
         sd(simCharExample[, 1]))),
 intrinsicPriorsFns = c("exponential"),
 intrinsicPriorsValues = list(10),
 extrinsicPriorsFns = c("fixed"),
 extrinsicPriorsValues = list(0),
 generation.time = 10000,
 nRuns = 2,nStepsPRC = 3,
 numParticles = 20,
 nInitialSimsPerParam = 10,
```
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```
stopRule = FALSE,
 multicore = FALSE,
 coreLimit = 1
 \lambdaresultsPRC
#one should make sure priors are uniform with doRun_rej!
resultsRej <- doRun_rej(
   phy = simPhyExample,
    traits = simCharExample,
    intrinsicFn = brownianIntrinsic,
    extrinsicFn = nullExtrinsic,
    startingPriorsFns = "normal",
    startingPriorsValues = list(c(mean(simCharExample[, 1]),
         sd(simCharExample[, 1]))),
    intrinsicPriorsFns = c("exponential"),
    intrinsicPriorsValues = list(10),
    extrinsicPriorsFns = c("fixed"),
    extrinsicPriorsValues = list(0),
    generation.time = 10000,
    jobName = "examplerun_rej",
    abcTolerance = 0.05,
   multicore = FALSE,
    coreLimit = 1
    \lambda
```
resultsRej

doSimulation *Discrete-Time Character Simulation*

Description

The function doSimulation evolves continuous characters under a discrete time process. These functions are mainly used as internal components, generating simulations within ABC analyses using the [doRun](#page-5-1) functions. See *Note* below.

Usage

```
doSimulation(
  phy = NULL,
  intrinsicFn,
  extrinsicFn,
  startingValues,
  intrinsicValues,
  extrinsicValues,
```

```
generation.time = 1000,
 TreeYears = max(branching.times(phy)) * 1e+06,
 timeStep = NULL,
 returnAll = FALSE,
 taxonDF = NULL,
 checkTimeStep = TRUE
\mathcal{L}
```
Arguments

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Details

The phylogenetic tree used is rescaled such that the distance from the root to the furthest tip is rescaled to equal 1 time-unit, and it is this rescaled edge lengths to with arguments timeStep refers to. Typically, this will be determined though as a ratio of TreeYears (which is the number of calendar years constituing the root-to-furthest-tip distance, and is determined by default as if the user had supplied a tree with edge lengths in time-units of 1 time-unit $= 1$ million years), and generation.time, which gives the length of timeSteps in calendar years (e.g. generation.time = 1000 means an evolutionary change in trait values every 1000 years). Note that the real number of trait change events simulated may be less less, because simulations start over at each branching node, but intervals between changes should be so fine that this should be negligible (related, the results should be independent of your choice for generation.time or timeStep). We recommend that the effective timeStep should be as short as is computationally possible. SaveRealParams is useful for tracking the *real* true values if simulating data to test the performance of ABC analyses. It is not useful for ABC analyses of empirical data.

Value

If $returnAll = FALSE$ (the default), this function returns a data frame of species character (tip) values in the tree, as a single column named 'states' with rownames reflecting the taxon names given in phy\$tip.label. If returnAll = TRUE, the raw data.frame from the simulation will instead be returned.

Note

The [simulateWithPriors](#page-44-1) functions are effectively the engine that powers the [doRun](#page-5-1) functions, while the [doSimulation](#page-12-1) functions are the pistons within the [simulateWithPriors](#page-44-1) engine. In general, most users will just drive the car - they will just use [doRun](#page-5-1), but some users may want to use [simulateWithPriors](#page-44-1) or [doSimulation](#page-12-1) functions to do various simulations.

Author(s)

Brian O'Meara and Barb Banbury

```
set.seed(1)
tree \le rcoal(20)
# get realistic edge lengths
```

```
tree$edge.length <- tree$edge.length*20
#Simple Brownian motion
char <- doSimulation(
   phy = tree,
   generation.time = 100000,
   intrinsicFn = brownianIntrinsic,
   extrinsicFn = nullExtrinsic,
   startingValues = c(10), #root state
   intrinsicValues = c(0.01),extrinsicValues = c(0))
#Character displacement model with minimum bound
char <- doSimulation(
   phy = tree,
   generation.time = 100000,
   intrinsicFn = boundaryMinIntrinsic,
   extrinsicFn = ExponentiallyDecayingPushExtrinsic,
   startingValues = c(10), #root state
   intrinsicValues = c(0.05, 10, 0.01),extrinsicValues = c(0, .1, .25))
```
extrinsicModels *Extrinsic Character Evolution Models*

Description

Functions describing various models of 'extrinsic' evolution (i.e. evolutionary processes dependent on factors extrinsic to the evolving lineage, such as environmental change, or other evolving lineages that interact with the lineage in question (competitors, predators, etc).

Usage

```
nullExtrinsic(params, selfstates, otherstates, timefrompresent)
nearestNeighborDisplacementExtrinsic(
 params,
  selfstates,
 otherstates,
  timefrompresent
)
everyoneDisplacementExtrinsic(params, selfstates, otherstates, timefrompresent)
```
ExponentiallyDecayingPushExtrinsic(

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```
params,
selfstates,
otherstates,
timefrompresent
```
Arguments

)

Details

The following extrinsic models are:

nullExtrinsic describes a model of no extrinsic character change. It has no parameters, really.

nearestNeighborDisplacementExtrinsic describes a model of extrinsic trait evolution where character values of a focal taxon depend on the values of closest relatives on the tree (e.g. competitive exclusion). The input parameters for this model are: nearestNeighborDisplacementExtrinsic with parameters params = sigma, springK, maximumForce

everyoneDisplacementExtrinsic describes a model of extrinsic trait evolution where the character values of a focal taxon depend on the values of all co-extant relatives on the simulated tree. The input parameters for this model are: everyoneDisplacementExtrinsic with parameters params = sigma, springK, maximumForce

ExponentiallyDecayingPushExtrinsic describes a model of extrinsic trait evolution where the character values of a focal taxon is 'pushed' away from other taxa with similar values, but the force of that 'push' exponentially decays as lineages diverge and their character values become less similar. The input parameters for this model are: ExponentiallyDecayingPushExtrinsic with parameters params = sigma, maximumForce, halfDistance

Value

A vector of values representing character displacement of that lineage over a single time step.

Author(s)

Brian O'Meara and Barb Banbury

See Also

Intrinsic models are described at [intrinsicModels](#page-21-1).

```
set.seed(1)
# Examples of simulations with various extrinsic models (and null intrinsic model)
tree \le rcoal(20)
# get realistic edge lengths
tree$edge.length <- tree$edge.length*20
#No trait evolution except due to
      # character displacement due to nearest neighbor taxon
char <- doSimulation(
   phy = tree,
   intrinsicFn = nullIntrinsic,
   extrinsicFn = nearestNeighborDisplacementExtrinsic,
   startingValues = c(10), #root state
   intrinsicValues = c(0),
    extrinsicValues = c(0.1, 0.1, 0.1),generation.time = 100000)
#Similarly, no trait evolution except due to
      # character displacement from all other taxa in the clade
char <- doSimulation(
    phy = tree,
    intrinsicFn = nullIntrinsic,
    extrinsicFn = everyoneDisplacementExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0),extrinsicValues = c(0.1, 0.1, 0.1),generation.time = 100000)
# A variant where force of character displacement decays exponentially
       # as lineages become more different
char <- doSimulation(
   phy = tree,
    intrinsicFn = nullIntrinsic,
    extrinsicFn = ExponentiallyDecayingPushExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0),extrinsicValues = c(0.1, 0.1, 2),
   generation.time = 100000)
```
getBMRatePrior 19

Description

This function automatically calculates prior distributions for the rate of trait evolution under the Brownian Motion (BM) model on a discrete time-scale, at a given timeStep, in the sense that that variable is used with other TreEvo functions like doRun_prc.

Usage

```
getBMRatePrior(phy, traits, timeStep, verbose = TRUE)
```
Arguments

Details

Returns a matrix of prior values that can be used in the doRun functions. Builds on functions in phylolm to estimate distribution.

Value

Returns a matrix of prior values

Author(s)

Brian O'Meara and Barb Banbury

Examples

data(simRunExample)

#timeStep = 0.1 -> effectively ~100 steps over the tree length

```
getBMRatePrior(phy = simPhyExample, traits = simCharExample,
  timeStep = 0.01, verbose = TRUE)
```
highestDensityInterval

Highest Density Interval

Description

This function calculates highest density intervals (HDIs) for a given univariate vector. Typically, this is done to obtain highest posterior density (HPD) for each freely varying parameter estimated in the posterior of a Bayesian MCMC analysis. If these intervals are calculated for more than one variable, they are referred to instead as regions.

Usage

```
highestDensityInterval(
  dataVector,
  alpha,
  code = FALSE,verboseMultimodal = TRUE,
  stopIfFlat = TRUE,
  ...
)
```
Arguments

Details

By default, HDI calculation is preformed by fitting a kernal density estimate (KDE) via R function density with default bandwidth, rescaling the kernal to a density, sorting intervals along the KDE by that density, and then summing these values from largest to smallest, until the desired alpha is reached. This algorithm is quick, and accounts for potentially multimodal distributions, or those with complex shapes, unlike unimodal intervals, such as quantiles, or the [HPDinterval](#page-0-0) in package coda.

Alternatively, a user can opt to use function [HPDinterval](#page-0-0) from package coda to calculate highest density intervals. These will work as long as the data has a single mode - data with multiple modes may have overly large quantiles (to encompass those multiple modes), resulting in overly wide estimates of coverage.

References

Hyndman, R. J. 1996. Computing and Graphing Highest Density Regions. *The American Statistician* 50(2):120-126.

See Also

[HPDinterval](#page-0-0) in package coda for an alternative used by older versions of TreEvo which cannot properly handle multimodal distributions.

Examples

set.seed(444)

```
# let's imagine we have some variable with
    # an extreme bimodal distribution
z \leq sample(c(rnorm(50, 1, 2), rnorm(100, 50, 3)))
hist(z)
# now let's say we want to know the what sort of values
# are reasonably consistent with this distribution
# for example, let's say we wanted the ranges within
# which 80% of our data occurs
# one way to do this would be a quantile
    # two tailed 80% quantiles
quantile(z, probs = c(0.1, 0.9))
# that seems overly broad - there's essentially no density
# in the central valley - but we want to exclude values found there!
# A value of 30 doesn't match this data sample, right??
# the problem is that all quantile methods are essentially based on
# the empirical cumulative distribution function - which is monotonic
# (as any cumulutative function should be), and thus
```

```
# A different approach is to use density from stats
density(z)
# we could then take the density estimates for
# particular intervals, rank-order them, and
# then cumulative sample until we reach
# our desired probability density (alpha)
# let's try that
alpha <-0.8zDensOut <- density(z)
zDensity <- zDensOut$y/sum(zDensOut$y)
inHPD <- cumsum(-sort(-zDensity)) <= alpha
# now reorder
inHPD <- inHPD[order(order(-zDensity))]
colDens <- rep(1, length(zDensity))
colDens[inHPD] <- 2
# and let's plot it, with colors
plot(zDensOut$x, zDensity, col = colDens)
# and we can do all that (except the plotting)
    # with highestDensityInterval
highestDensityInterval(z, alpha = 0.8)
#############################
# example with output from doRun_prc
data(simRunExample)
# we'll use summarizePosterior, which just automates picking
 # the last generation, and freely-varying parameters for HDRs
# alpha = 0.95summarizePosterior(
  resultsBMExample[[1]]$particleDataFrame,
  alpha = 0.95)
# you might be tempted to use alphas like 95%, but with bayesian statistics
# we often don't sample the distribution well enough to know
# its shape to exceeding detail. alpha = 0.8 may be more reasonable.
summarizePosterior(
  resultsBMExample[[1]]$particleDataFrame,
  alpha = 0.8)
```
intrinsicModels *Intrinsic Character Evolution Models*

Description

Functions describing various models of 'intrinsic' evolution (i.e. evolutionary processes intrinsic to the evolving lineage, independent of other evolving lineages (competitors, predators, etc).

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Usage

nullIntrinsic(params, states, timefrompresent) brownianIntrinsic(params, states, timefrompresent) boundaryIntrinsic(params, states, timefrompresent) boundaryMinIntrinsic(params, states, timefrompresent) boundaryMaxIntrinsic(params, states, timefrompresent) autoregressiveIntrinsic(params, states, timefrompresent) maxBoundaryAutoregressiveIntrinsic(params, states, timefrompresent) minBoundaryAutoregressiveIntrinsic(params, states, timefrompresent) autoregressiveIntrinsicTimeSlices(params, states, timefrompresent) autoregressiveIntrinsicTimeSlicesConstantMean(params, states, timefrompresent) autoregressiveIntrinsicTimeSlicesConstantSigma(params, states, timefrompresent)

Arguments

Details

The following intrinsic models are:

nullIntrinsic describes a model of no intrinsic character change. It has no parameters, really.

brownianIntrinsic describes a model of intrinsic character evolution via Brownian motion. The input parameters for this model are: boundaryIntrinsic with parameters params = sigma

boundaryIntrinsic describes a model of intrinsic character evolution where character change is restricted above a minimum and below a maximum threshold. The input parameters for this model are: boundaryMinIntrinsic with parameters params = sigma, minimum, maximum

boundaryMinIntrinsic describes a model of intrinsic character evolution where character change is restricted above a minimum threshold. The input parameters for this model are: boundaryMinIntrinsic with parameters params = sigma, minimum

autoregressiveIntrinsic describes a model of intrinsic character evolution. New character values are generated after one time step via a discrete-time OU process. The input parameters for this model are: autoregressiveIntrinsic with params = sigma (sigma), attractor (character mean), attraction (alpha)

minBoundaryAutoregressiveIntrinsic describes a model of intrinsic character evolution. New character values are generated after one time step via a discrete-time OU process with a minimum bound. The input parameters for this model are: MinBoundaryAutoregressiveIntrinsic with parameters params = sigma (sigma), attractor (character mean), attraction (alpha), minimum

autoregressiveIntrinsicTimeSlices describes a model of intrinsic character evolution. New character values are generated after one time step via a discrete-time OU process with differing means, sigma, and attraction over time. In the various *TimeSlices* models, time threshold units are in time before present (i.e., 65 could be 65 MYA). The last time threshold should be 0. The input parameters for this model are: autoregressiveIntrinsicTimeSlices with parameters params = sd-1 (sigma-1),attractor-1 (character mean-1), attraction-1 (alpha-1), time threshold-1,sd-2 (sigma-2), attractor-2 (character mean-2), attraction-2 (alpha-2), time threshold-2

autoregressiveIntrinsicTimeSlicesConstantMean describes a model of intrinsic character evolution. New character values are generated after one time step via a discrete-time OU process with differing sigma and attraction over time The input parameters for this model are: autoregressiveIntrinsicTimeSlice with parameters params = sd-1 (sigma-1), attraction-1 (alpha-1), time threshold-1, sd-2 (sigma-2),attraction-2 (alpha-2), time threshold-2, attractor (character mean)

autoregressiveIntrinsicTimeSlicesConstantSigma describes a model of intrinsic character evolution. New character values are generated after one time step via a discrete-time OU process with differing means and attraction over time. The input parameters for this model are: autoregressiveIntrinsicTimeSlicesConstantSigma with parameters params = sigma (sigma),attractor-1 (character mean-1), attraction-1 (alpha-1), time threshold-1,attractor-2 (character mean-2), attraction-2 (alpha-2), time threshold-2

Value

A vector of values representing character displacement of that lineage over a single time step.

Author(s)

Brian O'Meara and Barb Banbury

See Also

Another intrinsic model with multiple optima is described at [multiOptimaIntrinsic](#page-30-1). Extrinsic models are described at [abcmodels.extrinsic](#page-15-1).

```
set.seed(1)
# Examples of simulations with various intrinsic models (and null extrinsic model)
tree \le- rcoal(20)
# get realistic edge lengths
tree$edge.length <- tree$edge.length*20
```


```
#Simple Brownian motion Intrinsic Model
char <- doSimulation(
   phy = tree,
    intrinsicFn = brownianIntrinsic,
   extrinsicFn = nullExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0.01),extrinsicValues = c(0),
    generation.time = 100000)
# Simple model with BM, but a minimum bound at 0, max bound at 15
char <- doSimulation(
    phy = tree,
    intrinsicFn = boundaryIntrinsic,
    extrinsicFn = nullExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0.01, 0, 15),extrinsicValues = c(0),
    generation.time = 100000)
# Autoregressive (Ornstein-Uhlenbeck) model
      # with minimum bound at 0
char <- doSimulation(
   phy = tree,
    intrinsicFn = minBoundaryAutoregressiveIntrinsic,
    extrinsicFn = nullExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0.01, 3, 0.1, 0),extrinsicValues = c(0),
   generation.time = 100000)
# Autoregressive (Ornstein-Uhlenbeck) model
      # with max bound at 1
char <- doSimulation(
   phy = tree,
    intrinsicFn = maxBoundaryAutoregressiveIntrinsic,
    extrinsicFn = nullExtrinsic,
    startingValues = c(10), #root state
    intrinsicValues = c(0.01, 3, 0.1, 1),extrinsicValues = c(0),
    generation.time = 100000)
```
landscapeFPK_Intrinsic

Intrinsic Trait Evolution Model for a Macroevolutionary Landscape on a Fokker-Planck-Kolmogorov Potential Surface (Boucher et al., 2018)

Description

This function describes a discrete-time Fokker-Planck-Kolmogorov Potential Surface model (the FPK model for short), described for trait macroevolution by Boucher et al. (2018), and included here in TreEvo for use as an intrinsic trait model. This model can be used to describe a complex landscape of hills and valleys for a bounded univariate trait space.

Usage

```
landscapeFPK_Intrinsic(params, states, timefrompresent, grainScaleFPK = 100)
```

```
getTraitBoundsFPK(traitData)
```

```
plot_landscapeFPK_model(
 params,
  grainScaleFPK = 1000,
  traitName = "Trait",
 plotLandscape = TRUE
)
```
Arguments

Details

The FPK model is a four parameter model for describing the evolution of a trait without reference to the traits of other taxa (i.e. an intrinsic model in the terminology of package TreEvo). Three of these parameters are used to describe the shape of the landscape, which dictates a lineage's overall deterministic evolutionary trajectory on the landscape, while the fourth parameter (sigma) is a dispersion parameter that describes the rate of unpredictable, stochastic change.

The bounds on the trait space are treated as two additional parameters, but these are intended in the model as described by Boucher et al. to be treated as nuisance parameters. Boucher et al. intentionally fix these bounds at a far distance beyond the range of observed trait values, so in order to ensure they have as little effect on the evolutionary trajectories as possible.

The discrete time Fokker-Planck-Kolmogorov model used here describes a landscape specific to a population at a particular time, with a particular trait value. This landscape represents a potential surface, where height corresponds to a tendency to change in that direction. This allows for multiple optima, and assigns different heights to those optima, which represent the current attraction for a population to move toward that trait value. The shape of this potential surface is the macroevolutionary landscape. which Boucher et al describe the shape of using a fourth-order polynomial with the cubic component removed:

$$
V(x) = ax^4 + bx^2 + cx
$$

Where x is the trait values within the bounded interval - for simplicity, these are internally rescaled to sit within the arbitrary interval (-1.5 : 1.5). The parameters thus that describe the landscape shape are the coefficients *a*, *b*, and *c*. To calculate the landscape, the trait space is discretized into fine intervals, and the potential calculated for each interval. The scale of this discretization can be controlled by the user.

Note that if the landscape has a single peak, or if the potential surface is flat, the model effectively collapses to Brownian Motion, or Ornstein-Uhlenbeck with a single optima. To (roughly) quote Boucher et al: 'Finally, note that both BM and the OU model are special cases of the FPK model: BM corresponds to $V(x)=0$ and OU to $V(x)=((\alpha \text{lph}a/\alpha \text{pl}^2)*x^2)-((2 \text{pl}^2 \text$

Value

A vector of values representing character displacement of that lineage over a single time step.

Author(s)

David W. Bapst, loosely based on studying the code for function Sim_FPK from package BBMV.

References

Boucher, F. C., V. Demery, E. Conti, L. J. Harmon, and J. Uyeda. 2018. A General Model for Estimating Macroevolutionary Landscapes. *Systematic Biology* 67(2):304-319.

See Also

An alternative approach in TreEvo to estimating a macroevolutionary landscape with multiple optima is the intrinsic model [multiOptimaIntrinsic](#page-30-1), however this model requires an *a priori* choice on the number of optima and the assumption that the optima have similar attractor strength. Other intrinsic models are described at [intrinsicModels](#page-21-1).

```
set.seed(444)
traitData<-rnorm(100,0,1)
# need traits to calculate bounds
bounds<-getTraitBoundsFPK(traitData)
```

```
# pick a value at random
trait<-0
# two peak symmetric landscape example
params<-c(
a=2,
b=-4,c=0,
sigma=1,
bounds)
plot_landscapeFPK_model(params)
# simulate under this model - simulated trait DIVERGENCE
landscapeFPK_Intrinsic(params=params, states=trait, timefrompresent=NULL)
# simulate n time-steps, repeat many times, plot results
repeatSimSteps<-function(params,trait,nSteps){
for(i in 1:nSteps){
# add to original trait value to get new trait value
 trait<-trait+landscapeFPK_Intrinsic(
  params=params, states=trait, timefrompresent=NULL)
  }
trait
}
repSim<-replicate(30,repeatSimSteps(params,trait,20))
hist(repSim,main="Simulated Trait Values")
# uneven two peak symmetric landscape example
params<-c(
a=2,
b=-4,c=0.3,
sigma=1,
bounds)
plot_landscapeFPK_model(params)
# simulate under this model - simulated trait DIVERGENCE
landscapeFPK_Intrinsic(params=params, states=trait, timefrompresent=NULL)
repSim<-replicate(30,repeatSimSteps(params,trait,20))
hist(repSim,main="Simulated Trait Values")
```


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Description

Function returnPLSModel fits a PLS regression (using [plsr](#page-0-0)) individually to each freely varying parameter of a model, unlike a true multivariate PLS regression. A secondary step than limits the number of components to those that explain some minimum cumulative percentage of variance (see argument variance.cutoff). For ABC, this seems to result in much better results, without one parameter dominating the combined variance.

Usage

```
returnPLSModel(
  trueFreeValuesMatrix,
  summaryValuesMatrix,
  validation = "CV",
  scale = TRUE,
  variance.cutoff = 95,
  verbose = TRUE,
  segments = min(10, nrow(summaryValuesMatrix) - 1),
  ...
\mathcal{L}
```
PLSTransform(summaryValuesMatrix, pls.model)

Arguments

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Details

Function PLSTransform uses results from a Partial Least Squares (PLS) model fit with returnPLSModel to transform summary values.

Value

Function returnPLSModel returns a PLS model, and function PLSTransform returns transformed summary statistics.

Author(s)

Brian O'Meara and Barb Banbury

See Also

Function returnPLSModel effectively wraps function plsr from package pls (see documentation at [mvr](#page-0-0)).

```
set.seed(1)
simPhyExample <- rcoal(20)
simPhyExample$edge.length <- simPhyExample$edge.length * 20
# example simulation
nSimulations <- 6
simDataParallel <- parallelSimulateWithPriors(
  nrepSim = nSimulations,
  multicore = FALSE,
  coreLimit = 1,
  phy = simPhyExample,
  intrinsicFn = brownianIntrinsic,
  extrinsicFn = nullExtrinsic,
  startingPriorsFns = "normal",
  startingPriorsValues = list(
      c(mean(simCharExample[, 1]),
      sd(simCharExample[, 1]))),
   intrinsicPriorsFns = c("exponential"),
   intrinsicPriorsValues = list(10),
  extrinsicPriorsFns = c("fixed"),
  extrinsicPriorsValues = list(0),
  generation.time = 10000,
  checkpointFile = NULL,
```

```
checkpointFreq = 24,
   verbose = FALSE,
   freevector = NULL,
   taxonDF = NULL)
nParFree <- sum(attr(simDataParallel, "freevector"))
# separate the simulation results:
   # 'true' generating parameter values from the summary values
trueFreeValuesMat <- simDataParallel[, 1:nParFree]
summaryValuesMat <- simDataParallel[, -1:-nParFree]
PLSmodel <- returnPLSModel(
    trueFreeValuesMatrix = trueFreeValuesMat,
    summaryValuesMatrix = summaryValuesMat,
    validation = "CV",
    scale = TRUE,
    variance.cutoff = 95 ,
    segments = nSimulations
    \mathcal{L}PLSmodel
PLSTransform(
    summaryValuesMatrix = summaryValuesMat,
    pls.model = PLSmodel
    \lambda
```
multiOptimaIntrinsic *Single Evolutionary Regime Model with Multiple Optima*

Description

This model describes an evolutionary process where multiple optima exist. Lineages are attracted to an optima in their vicinity (this is handled as a stochastic process where which attract affects which population at a given point in time is weighted with respect to the proximity of a given population's trait value to the given optima), but as a lineage approaches the attractor that controls it, it may experience less directional evolution in the direction of the optima, and overall show more variation. This framework allows for the model to describe the evolution with respect to multiple optima simultaneously, without needing to treat individual transitions between optima (or macroevolutionary 'regimes') as a separate parameter. Thus, the optima exist within a single evolutionary regime, with only a scaling parameter present that allows more or less frequent transitions between optima by altering the impact of proximity to optima.

Usage

```
multiOptimaIntrinsic(params, states, timefrompresent)
```
Arguments

Details

multiOptimaIntrinsic describes a model of intrinsic character evolution with multiple regimes. New character values are generated after one time step via a discrete-time OU process with a particular optima assigned to a particular regime, and each time-step a lineage has some finite probability of switching to a new regime, and being drawn to that regime's optima. The chance of a lineage being drawn to a particular optima is based on proximity to that optima, but the chance of switching to another regime is never completely negligible. The strength of the draw to the optima, the attraction strength, 'alpha', is the same for all regimes (all optima). This model has *n* input parameters: multiOptimaIntrinsic with params = sigma (rate of dispersion), alpha (strength of attraction to an optima), rho (an exponent scaling the weighting of distance to optima – this parameter will control the probability of a lineage switching optima), and, finally, *n* (two or more) theta values, which are the optima for the different macroevolutionary adaptive regimes.

Our biological interpretation for this model is a scenario in which optima represent fixed phenotypic trait values, conveying maximum adaptive benefit relative to neighboring values in trait space. The proximity of a population to an optima makes it more likely to fall under the influence of that regime, and thus experience directional selection in the direction of that optima. However, as there are multiple optima, a lineage might be influenced by multiple nearby optima over its evolutionary history, rather than simply the closest trait optimum. Lineages equidistant between multiple optima should be equally likely to be drawn to any specific optima, and populations in general should experience the influence of nearby optima inversely relative to their distance from the optima. Thus, a lineage very close to an optimum would show a large variance in its trait values as it circles the adaptive plateau, with infrequent but sudden, far-spanning movements toward a different optimum.

Value

A vector of values representing character displacement of that lineage over a single time step.

Author(s)

David W. Bapst

See Also

An alternative approach in TreEvo to estimating a macroevolutionary landscape with multiple optima is the Fokker-Planck-Kolmogorov (FPK) model, which can be fit with landscapeFPK_Intrinsic. This model does not assume a set number of optima nor that they have similar attractor strength, but parameters may be difficult to interpret in isolation, and fitting this model may be slower with

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TreEvo due to necessary linear algebra transformations. Other intrinsic models are described at [intrinsicModels](#page-21-1).

```
# three optima model, with strong attraction
set.seed(1)
params<-c(
sigma=0.1,
alpha=0.7,
rho=1,
theta=c(-20,20,50)
\lambdamultiOptimaIntrinsic(params=params, states=0, timefrompresent=NA)
# simulate n time-steps, repeat many times, plot results
repeatSimSteps<-function(params,trait=0,nSteps){
for(i in 1:nSteps){
# add to original trait value to get new trait value
 trait<-trait+multiOptimaIntrinsic(
  params=params, states=trait, timefrompresent=NA)
 }
trait
}
repSim<-replicate(300,repeatSimSteps(params,trait=0,100))
hist(repSim,main="Simulated Trait Values",breaks=20)
# same model above, with more switching between optima
set.seed(1)
params<-c(
sigma=0.1,
alpha=0.7,
rho=0.5,
theta=c(-20,20,50)
)
multiOptimaIntrinsic(params=params, states=0, timefrompresent=NA)
# simulate n time-steps, repeat many times, plot results
repeatSimSteps<-function(params,trait=0,nSteps){
for(i in 1:nSteps){
# add to original trait value to get new trait value
 trait<-trait+multiOptimaIntrinsic(
  params=params, states=trait, timefrompresent=NA)
 }
trait
}
repSim<-replicate(300,repeatSimSteps(params,trait=0,100))
hist(repSim,main="Simulated Trait Values",breaks=20)
```


Description

This function calculates Effective Sample Size (ESS) on results. The ESS algorithm performs best when results are from multiple runs.

Usage

```
pairwiseESS(inputData)
```
Arguments

inputData The input dataset can be a single data frame or a list of data frames.

Value

Returns a matrix with ESS values of all pairwise runs.

Author(s)

Brian O'Meara and Barb Banbury

```
data(simRunExample)
```

```
# this will give a warning
pairwiseESS(resultsBMExample[[1]]$particleDataFrame)
# ESS should be calculated over multiple runs
pairwiseESS(resultsBMExample)
# you can also manually assemble a list of particleDataFrame tables
    # and use this as the input
inputList <- list(
   resultsBMExample[[2]]$particleDataFrame,
   resultsBMExample[[1]]$particleDataFrame
    \lambdapairwiseESS(inputList)
```


Description

This function calculates Kolmogorov-Smirnov on results.

Usage

```
pairwiseKS(particleDataFrameList)
```
Arguments

```
particleDataFrameList
```
An object of type list, composed of particleDataFrames from separate analyses.

Value

Returns a matrix with Kolmogorov-Smirnov values of all pairwise runs.

Author(s)

Brian O'Meara and Barb Banbury

Examples

```
data(simRunExample)
pdfList <- list(
  Brownian = resultsBMExample[[1]]$particleDataFrame,
  Bounded = resultsBoundExample[[1]]$particleDataFrame
  )
pairwiseKS(particleDataFrameList = pdfList)
```
parentOffspringPlots *Plotting Parent-Offspring Particles*

Description

This function uses the particleDataFrame output by TreEvo ABC analyses and plots parentoffspring particles from generation to generation.

Usage

parentOffspringPlots(particleDataFrame)

Arguments

particleDataFrame

particleDataFrame output by TreEvo ABC analyses.

Details

Each parameter is plotted twice for parent-offspring relationships through the generations. In the top row, particles are plotted as a measure of distance to the observed data; the farther away the particle the bigger the circle. In the bottom row, particles are plotted as a measure of their weights; larger circles are closer to observed data and therefore carry more weight in the analysis.

As of version 0.6.0, rejected particles are not saved for outputting by the parallelized algorithm, and thus they are no longer displayed by this function.

Value

Creates a set of parent-offspring plots.

Author(s)

Brian O'Meara and Barb Banbury

Examples

```
data(simRunExample)
parentOffspringPlots(resultsBMExample[[1]]$particleDataFrame)
```
plotABC_3D *3D ABCplots*

Description

Plot posterior density distribution for each generation in 3d plot window

Usage

```
plotABC_3D(
 particleDataFrame,
 parameter,
  show.particles = "none",
 plot.parent = FALSE,
 realParam = FALSE,
  realParamValues = NA
)
```
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Arguments

Details

This opens a new interactive 3d plotting window and plots the posterior density distribution of accepted particles from each generation. Several options are available to add to the plot: plotting particles by weight or distance, plotting particle parantage, and plotting the real parameter values (if known).

As of version 0.6.0, rejected particles are not saved for outputting by the parallelized algorithm, and thus they are no longer displayed by this function, unlike previous versions.

Note

This function requires access to the function triangulate and the as method for class gpc.poly from package gpclib. As of 08-22-19, this package was not available from CRAN as a Windows binary, and thus this function is likely unavailable to many (if not all) Windows users.

This function also requires the package rgl, which is usually easier to obtain than package gpclib, but may not be buildable on some UNIX workstations.

Author(s)

Barb Banbury

```
# need to check for required suggested packages
if(requireNamespace("gpclib", quietly = TRUE) & requireNamespace("rgl", quietly = TRUE)){
```

```
data(simRunExample)
plotABC_3D(
    particleDataFrame = resultsBMExample[[1]]$particleDataFrame,
    parameter = 7,
    show.particles = "none",
    plot.parent = FALSE,
    realParam = FALSE,
    realParamValues = NA
```
}

 \mathcal{L}

plotPosteriors *Plot posterior distributions*

Description

For each free parameter in the posterior, this function creates a plot of the distribution of values estimated in the last generation. This function can also be used to visually compare against true (generating) parameter values in a simulation.

Usage

```
plotPosteriors(
  particleDataFrame,
  priorsList,
  realParam = FALSE,
  realParamValues = NA
\lambda
```
Arguments

particleDataFrame

A particleDataFrame object returned by TreEvo ABC analyses, can be a single data frame or a list of data frames. If the particleDataFrame is a list of separate TreEvo runs, posteriors will be layered over each other to check for repeatability. The relative gray-scale of posterior distributions in the plot depends on their total number of runs.

- priorsList A priorList list object, returned by TreEvo [doRun](#page-5-1) functions, where each element is itself a list of length two, composed of the name for the prior function (e.g. 'uniform', and a vector of the parameters for that prior distribution). Can be a single such list, or a list of priorList lists from a series of analyses (i.e. a list of depth 3). If the priorList is a list of lists (if it is found to be a list of depth 3, only the first list will be evaluated, and all other lists will be ignored. In other words, priors are expected to be identical for all runs considered by this function, such the choice of using the list of priors from the first analysis in the list is acceptable for all comparisons.
- realParam If TRUE, this function will plot line segments where real parameter values are known. (Usually only true when simulated data is analyzed.)

realParamValues

Values for real parameters, include a value for each parameter (including fixed values). Otherwise should be NA.

Value

Returns a plot for each free parameter.

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Note

realParam and realParamValues should only be used with simulated data, where the true values are known.

Author(s)

Barb Banbury and Brian O'Meara

See Also

[plotPrior](#page-38-1) for a set of functions for visualizing and summarizing prior and posterior distributions, including a visual comparison for single parameters.

Examples

```
data(simRunExample)
```
make a list of particleDataFrames to plot multiple runs resultsPDFlist <- lapply(resultsBMExample, function(x) x\$particleDataFrame)

```
plotPosteriors(
  resultsPDFlist,
  priorsList = resultsBMExample[[1]]$priorList,
  realParam = TRUE,
  realParamValues = c(ancStateExample, genRateExample)
  \lambda
```


Description

Assorted functions for visualizing and summarizing the prior and posterior probability distributions associated with ABC analyses.

Usage

```
plotPrior(
  priorFn = match.arg(arg = priorFn, choices = c("fixed", "uniform", "normal",
    "lognormal", "gamma", "exponential"), several.ok = FALSE),
  priorVariables,
  plotQuants = TRUE,
 plotLegend = TRUE
)
```
plotUnivariatePosteriorVsPrior(

```
posteriorCurve,
 priorCurve,
 label = "parameter",
  trueValue = NULL,
  ...
\mathcal{L}getUnivariatePriorCurve(
 priorFn,
 priorVariables,
 nPoints = 1e+05,
 from = NULL,
 to = NULL,alpha = 0.8,
 coda = FALSE,
 verboseMultimodal = TRUE,
  ...
\mathcal{L}getUnivariatePosteriorCurve(
 acceptedValues,
 from = NULL,
 to = NULL,
 alpha = 0.8,
 code = FALSE,verboseMultimodal = TRUE,
  ...
\mathcal{L}
```
Arguments

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Details

Function plotPrior visualizes the shape of various prior probability distributions available in TreEvo ABC analyses, while getUnivariatePriorCurve returns density coordinates and summary statistics from user-selected prior probability distribution.

Similarly, function getUnivariatePosteriorCurve returns density coordinates and summary statistics from the posterior distribution of an ABC analysis.

Both getUnivariatePriorCurve and getUnivariatePosteriorCurve also calculate the highest density intervals for their respective parameters, using the function [highestDensityInterval](#page-19-1).

Function plotUnivariatePosteriorVsPrior plots the univariate density distributions from the prior and posterior against each other for comparison, along with the highest density intervals (HDI) for both.

The summaries calculated from getUnivariatePriorCurve and getUnivariatePosteriorCurve are used as the input for plotUnivariatePosteriorVsPrior, hence the relationship of these functions to each other, and why they are listed together here.

Value

plotPrior and plotUnivariatePosteriorVsPrior produce plots of the respective distributions (see above).

getUnivariatePriorCurve returns a list of x and y density coordinates, mean, and the highest density intervals (HDI) for their respective distribution.

getUnivariatePosteriorCurve does the same for a posterior sample of parameter estimates, returning a list of x and y density coordinates, mean, and the highest posterior density intervals (HPD).

Author(s)

Brian O'Meara and Barb Banbury

See Also

Highest posterior densities are calculated via [highestDensityInterval](#page-19-1).

[plotPosteriors](#page-37-1) Plots multiple posteriors against their priors and potential known values.

```
data(simRunExample)
# examples with plotPrior
plotPrior(
   priorFn = "exponential",
   priorVariables = c(10))
plotPrior(
   priorFn = "normal",
   priorVariables = c(1, 2))
plotPrior(
   priorFn = "gamma",
   priorVariables = c(2, .2),
   plotQuants = FALSE,
   plotLegend = FALSE)
# examples of getting density coordinates and
 # summary statistics from distributions
priorKernal <- getUnivariatePriorCurve(
   priorFn = "normal",
   priorVariables = c(28, 2),
   nPoints = 100000,
   from = NULL,
   to = NULL,
   alpha = 0.95)
postKernal <- getUnivariatePosteriorCurve(
   acceptedValues =
       resultsBMExample[[1]]$particleDataFrame$starting_1,
    from = NULL,
    to = NULL,alpha = 0.95)
priorKernal
postKernal
```

```
# let's compare this (supposed) prior
 # against the posterior in a plot
plotUnivariatePosteriorVsPrior(
   posteriorCurve = postKernal,
   priorCurve = priorKernal,
   label = "parameter",
    trueValue = NULL)
```
cool!

simRunExample *Example Analysis Output of a Simulated Dataset*

Description

Simulated 30-taxon coalescent tree and simulated character data from a Brownian Motion intrinsic model ([brownianIntrinsic](#page-21-2)), with saved generating parameters. Character data was generated under this model using doSimulation. Also includes results from an example analysis.

Format

Loading the simRunExample example dataset adds seven new objects to the namespace:

- simPhyExample A simulated 30-tip coalescent phylogeny in typical phylo format.
- ancStateExample The starting ancestral value, used for generating the simulated continuous trait data.
- genRateExample The true rate of trait change under Brownian Motion, used for generating the simulated continuous trait data.
- simCharExample The output of [doSimulation](#page-12-1) on simPhyExample, under the model [brownianIntrinsic](#page-21-2). composed of just the simulated trait values as a one-column matrix with row names indicating tip labels, as desired by doRun functions.
- resultsBMExample The results of [doRun_prc](#page-5-2), under the generating model of [brownianIntrinsic](#page-21-2)
- resultsBoundExample The results of [doRun_prc](#page-5-2), under the incorrect model of [boundaryMinIntrinsic](#page-21-2)

The objects resultsBMExample and resultsBoundExample are lists composed of a number of elements (see the documentation for the [doRun_prc](#page-5-2) function for more detail).

Examples

data(simRunExample)

...things to do with this data?

###################

```
# This data was generated using this process:
## Not run:
library(TreEvo)
set.seed(1)
simPhyExample <- rcoal(20)
# get realistic edge lengths
simPhyExample$edge.length <- simPhyExample$edge.length*20
# plot with time axis (root is about ~15 Ma)
plot(simPhyExample)
axisPhylo()
genRateExample <- c(0.001)
ancStateExample <- c(10)
#Simple Brownian motion
simCharExample <- doSimulation(
   phy = simPhyExample,
   intrinsicFn = brownianIntrinsic,
   extrinsicFn = nullExtrinsic,
    startingValues = ancStateExample, #root state
    intrinsicValues = genRateExample,
    extrinsicValues = c(0),
    generation.time = 10000
   \lambdaresultsBMExample <- doRun_prc(
   phy = simPhyExample,
   traits = simCharExample,
   intrinsicFn = brownianIntrinsic,
   extrinsicFn = nullExtrinsic,
    startingPriorsFns = "normal",
    startingPriorsValues = list(c(mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
    intrinsicPriorsFns = c("exponential"),
    intrinsicPriorsValues = list(10),
    extrinsicPriorsFns = c("fixed"),
   extrinsicPriorsValues = list(0),
   generation.time = 10000,
   nRuns = 2,nStepsPRC = 3,
   numParticles = 20,
   nInitialSimsPerParam = 10,
    jobName = "examplerun_prc",
   stopRule = FALSE,
   multicore = FALSE,
   verboseParticles = TRUE,
   coreLimit = 1
    \mathcal{L}
```

```
resultsBoundExample <- doRun_prc(
   phy = simPhyExample,
    traits = simCharExample,
   intrinsicFn = boundaryMinIntrinsic,
   extrinsicFn = nullExtrinsic,
   startingPriorsFns = "normal",
   startingPriorsValues = list(c(mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
    intrinsicPriorsFns = c("exponential", "normal"),
    intrinsicPriorSValues = list(10, c(-10, 1)),extrinsicPriorsFns = c("fixed"),
    extrinsicPriorsValues = list(0),
    generation.time = 10000,
   nRuns = 2,nStepsPRC = 3,
   numParticles = 20,
   nInitialSimsPerParam = 10,
    jobName = "examplerun_prc_bound",
    stopRule = FALSE,
   multicore = FALSE,
   verboseParticles = TRUE,
    coreLimit = 1
   \lambdarm(.Random.seed)
save.image(file = "simRunExample.rdata")
if(interactive()){savehistory("simRunExample.Rhistory")}
## End(Not run)
```
simulateWithPriors *Simulate data for initial TreEvo analysis*

Description

The simulateWithPriors function pulls parameters from prior distributions and conducts a single simulation of continuous trait evolution (using the [doSimulation](#page-12-1) function), returning useful summary statistics for ABC. parallelSimulateWithPriors is a wrapper function for simulateWithPriors that allows for multithreading and checkpointing. This family of functions is mostly used as internal components, generating simulations within ABC analyses using the [doRun](#page-5-1) functions. See *Note* below.

Usage

```
simulateWithPriors(
 phy = NULL,intrinsicFn,
```

```
extrinsicFn,
  startingPriorsFns,
  startingPriorsValues,
  intrinsicPriorsFns,
  intrinsicPriorsValues,
  extrinsicPriorsFns,
  extrinsicPriorsValues,
  generation.time = 1000,
  TreeYears = max(branching.times(phy)) * 1e+06,
  timeStep = NULL,
 giveUpAttempts = 10,
  verbose = FALSE,
  check = TRUE,taxonDF = NULL,freevector = NULL
\mathcal{L}parallelSimulateWithPriors(
 nrepSim,
 multicore,
 coreLimit,
 phy,
  intrinsicFn,
  extrinsicFn,
  startingPriorsFns,
  startingPriorsValues,
  intrinsicPriorsFns,
  intrinsicPriorsValues,
  extrinsicPriorsFns,
 extrinsicPriorsValues,
  generation.time = 1000,
  TreeYears = max(branching.times(phy)) * 1e+06,
  timeStep = NULL,
  checkpointFile = NULL,
  checkpointFreq = 24,
  verbose = TRUE,
  checkTimeStep = TRUE,
  verboseNested = FALSE,
  freevector = NULL,
  taxonDF = NULL,giveUpAttempts = 10
```

```
\lambda
```
Arguments

extrinsicFn Name of (previously-defined) function that governs how traits evolve within a lineage, based on their own ('internal') trait vlaue and the trait values of other taxa.

startingPriorsFns

Vector containing names of prior distributions to use for root states: can be one of "fixed", "uniform", "normal", "lognormal", "gamma", "exponential".

startingPriorsValues

A list of the same length as the number of prior distributions specified in startingPriorsFns (for starting values, this should be one prior function specified for each trait thus one for most univariate trait analyses), with each element of the list a vector the same length as the appropriate number of parameters for that prior distribution (1 for "fixed", 2 for "uniform", 2 for "normal", 2 for "lognormal", 2 for "gamma", 1 for "exponential").

intrinsicPriorsFns

Vector containing names of prior distributions to use for intrinsic function parameters: can be one of "fixed", "uniform", "normal", "lognormal", "gamma", "exponential".

intrinsicPriorsValues

A list of the same length as the number of prior distributions specified in intrinsicPriorsFns (one prior function specified for each parameter in the intrinsic model), with each element of the list a vector the same length# as the appropriate number of parameters for that prior distribution (1 for "fixed", 2 for "uniform", 2 for "normal", 2 for "lognormal", 2 for "gamma", 1 for "exponential").

extrinsicPriorsFns

Vector containing names of prior distributions to use for extrinsic function parameters: can be one of "fixed", "uniform", "normal", "lognormal", "gamma", "exponential".

extrinsicPriorsValues

A list of the same length as the number of prior distributions specified in extrinsicPriorsFns (one prior function specified for each parameter in the extrinsic model), with each element of the list a vector the same length as the appropriate number of parameters for that prior distribution (1 for "fixed", 2 for "uniform", 2 for "normal", 2 for "lognormal", 2 for "gamma", 1 for "exponential").

generation.time

The number of years per generation. This sets the coarseness of the simulation; if it's set to 1000, for example, the population's trait values change every 1000 calendar years. Note that this is in calendar years (see description for argument TreeYears), and not in millions of years (as is typical for dated trees in macroevolutionary studies). Thus, if a branch is 1 million-year time-unit long, and a user applies the default generation.time = 1000, then 1000 evolutionary changes will be simulated along that branch. See documentation for [doSimulation](#page-12-1) for further details.

TreeYears The amount of calendar time from the root to the furthest tip. Most trees in macroevolutionary studies are dated with branch lengths in units of millions of years, and thus the default for this argument is max(branching.times(phy)) $*$ 1e6. If your tree has the most recent tip at time zero (i.e., the modern day), this would be the same as the root age of the tree. If your branch lengths are

Value

Function simulateWithPriors returns a vector of trueFreeValues, the true generating parameters used in the simulation (a set of values as long as the number of freely varying parameters), concatenated with a set of summary statistics for the simulation.

Function parallelSimulateWithPriors returns a matrix of such vectors bound together, with each row representing a different simulation.

By default, both functions also assign a logical vector named freevector, indicating the total number of parameters and which parameters are freely-varying (have TRUE values), as an attribute of the output.

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Note

The [simulateWithPriors](#page-44-1) functions are effectively the engine that powers the [doRun](#page-5-1) functions, while the [doSimulation](#page-12-1) function is the pistons within the [simulateWithPriors](#page-44-1) engine. In general, most users will just drive the car - they will just use [doRun](#page-5-1), but some users may want to use [simulateWithPriors](#page-44-1) or [doSimulation](#page-12-1) to do various simulations.

Author(s)

Brian O'Meara and Barb Banbury

Examples

set.seed(1)

```
tree \le rcoal(20)
# get realistic edge lengths
tree$edge.length <- tree$edge.length*20
# example simulation
# NOTE: the example analyses involve too few simulations,
    # as well as overly coarse time-units...
    # ...all for the sake of examples that reasonably test the functions
simData <- simulateWithPriors(
  phy = tree,
  intrinsicFn = brownianIntrinsic,
  extrinsicFn = nullExtrinsic,
  startingPriorsFns = "normal",
  startingPriorsValues = list(
      c(mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
  intrinsicPriorsFns = c("exponential"),
  intrinsicPriorsValues = list(10),
  extrinsicPriorsFns = c("fixed"),
  extrinsicPriorsValues = list(0),
  generation.time = 100000,
  freevector = NULL,
  giveUpAttempts = 10,
  verbose = TRUE)
simData
simDataParallel <- parallelSimulateWithPriors(
  nrepSim = 2,
  multicore = FALSE,
  coreLimit = 1,
  phy = tree,
  intrinsicFn = brownianIntrinsic,
  extrinsicFn = nullExtrinsic,
  startingPriorsFns = "normal",
  startingPriorsValues = list(
     c(mean(simCharExample[, 1]), sd(simCharExample[, 1]))),
  intrinsicPriorsFns = c("exponential"),
```

```
intrinsicPriorsValues = list(10),
extrinsicPriorsFns = c("fixed"),
extrinsicPriorsValues = list(0),
generation.time = 100000,
checkpointFile = NULL, checkpointFreq = 24,
verbose = TRUE,
freevector = NULL,
taxonDF = NULL)
```
simDataParallel

summarizePosterior *Summarize Posterior Distribution for a Free Parameter*

Description

This function summarizes the distribution of parameter estimates from the posterior of an ABC analysis using the doRun functions in TreEvo, for all freely varying parameters. Only the final generation is considered. This summary includes the mean, standard deviation and Highest Posterior Density (at a 0.8 alpha) for each parameter.

Usage

```
summarizePosterior(
 particleDataFrame,
  alpha = 0.8,
 coda = FALSE,
  verboseMultimodal = TRUE,
  stopIfFlat = TRUE,
  ...
)
```
Arguments

particleDataFrame

Value

Returns a list, wherein each element of the list is secondary list containing the weighted mean, standard deviation, and a matrix giving the highest density intervals (e.g. the highest posterior density intervals). Because posterior estimates of parameter values may be multimodal, multiple sets of bounds may be reported for complex posterior distributions, which each constitute one row of the output matrix. See [highestDensityInterval](#page-19-1) for details.

Author(s)

David W Bapst

See Also

This function is essentially a wrapper for independently applying a few summary statistics and applying [highestDensityInterval](#page-19-1) to multiple parameter estimates, taken from the last generation of an ABC analysis in TreEvo. As each parameter is handled independently, the returned HPD intervals may not properly account for covariation among parameter estimates from the posterior. If testing whether a given observation is within a given density of the posterior or not, please look at function [testMultivarOutlierHDR](#page-51-1).

```
# example with output from doRun_prc
data(simRunExample)
# alpha = 0.95
summarizePosterior(
     resultsBMExample[[1]]$particleDataFrame,
     alpha = 0.95)
# you might be tempted to use alphas like 95%,
    # but with bayesian statistics
# we often don't sample the distribution well enough to know
   # its shape to exceeding detail.
   # alpha = 0.8 may be more reasonable.
summarizePosterior(
   resultsBMExample[[1]]$particleDataFrame,
```

```
alpha = 0.8)
# or even better, for coverage purposes, maybe 0.5
summarizePosterior(
   resultsBMExample[[1]]$particleDataFrame,
   alpha = 0.5)
```
testMultivarOutlierHDR

Test If an Outlier Is Within a Highest Density Region of a Multivariate Cloud of Data Points

Description

This function takes a matrix, consisting of multiple observations for a set of variables, with observations assumed to be independent and identically distributed, calculates a highest density interval for each of those variables (using [highestDensityInterval](#page-19-1)), and then tests if some potential 'outlier' (a particular observation for that set of variables), is within that highest density interval. Typically, users may want to account for possible non-independence of the variables, which could lead to inflated false-positive rates with this test of coverage. To account for this, this function allows for the option of applying principal component analysis to rotate the variables, and then calculate the highest density intervals from the orthogonal principal component scores.

Usage

```
testMultivarOutlierHDR(
  dataMatrix,
  outlier,
  alpha,
  coda = FALSE,
  verboseMultimodal = FALSE,
  pca = TRUE,...
\mathcal{L}
```
Arguments

Details

Quantiles, or highest density intervals are essentially a univariate concept. They are calculated independently on each variable, as if each variable was independent. They are often used to try to piece together 'regions' of confidence or credibility in statistics. Unfortunately, this means that that if variables are correlated, the box-like region they describe in the multivariate space may not cover enough of the actual data scatter, while covering lots of empty space.

There are several solutions. There are a number of approaches for fitting ellipsoids to bivariate data. But what about multivariate datasets, such as sets of parameter estimates from the posterior of a Bayesian analysis, which may have an arbitrary number of variables (and thus dimensions)?

A different solution, applied here when pca = TRUE, is to remove the non-independence among variables by rotating the dataset with principal components analysis. While this approach has its own flaws, such as assuming that the data reflects a multivariate normal. However, this is absolutely an improvement on not-rotating, particularly if being done for the purpose of this functon, which is essentially to measure coverage–to measure whether some particular set of values falls within a highest density region (a multivariate highest density interval).

Value

A logical, indicating whether the given data point (outlier) is within the multivariate data cloud at the specified threshold probability density.

Author(s)

David W. Bapst

See Also

This function is essentially a wrapper for applying highestDensityInterval to multivariate data, along with **[princomp](#page-0-0)** in package stats.

```
# First, you should understand the problems
# with dealing with correlated variables and looking at quantiles
# simulate two correlated variables
set.seed(444)
x <- rnorm(100, 1, 1)
y <- (x*1.5)+rnorm(100)
# find the highest density intervals for each variable
pIntX \leq highestDensityInterval(x, alpha = 0.8)
pIntY <- highestDensityInterval(y, alpha = 0.8)
# These define a box-like region that poorly
# describes the actual distribution of
# the data in multivariate space.
# Let's see this ourselves...
xLims < -c(min(c(x, plntX)), max(c(x, plntX)))yLims <- c(min(c(y, pIntY)), max(c(y, pIntY)))
plot(x, y, xlim = xLims, ylim = yLims)rect(pIntX[1], pIntY[1], pIntX[2], pIntY[2])
# So, that doesn't look good.
# Let's imagine we wanted to test if some outlier
# was within that box:
outlier \leq -c(2, -1)points(x = outlier[1], y = outlier[2], col = 2)
# we can use testMultivarOutlierHDR with pca = FALSE
# to do all of the above without visually checking
testMultivarOutlierHDR(dataMatrix = cbind(x, y),
    outlier = outlier, alpha = 0.8, pca = FALSE)
# Should that really be considered to be within
# the 80% density region of this data cloud?
#####
# let's try it with PCA
pcaRes <- princomp(cbind(x, y))
PC <- pcaRes$scores
pIntPC1 <- highestDensityInterval(PC[, 1], alpha = 0.8)
pIntPC2 <- highestDensityInterval(PC[, 2], alpha = 0.8)
```


```
# plot it
xLims <- c(min(c(PC[, 1], pIntPC1)), max(c(PC[, 1], pIntPC1)))
yLims <- c(min(c(PC[, 2], pIntPC2)), max(c(PC[, 2], pIntPC2)))
plot(PC[, 1], PC[, 2], xlim = xLims, ylim = yLims)
rect(pIntPC1[1], pIntPC2[1], pIntPC1[2], pIntPC2[2])
# That looks a lot better, isnt' filled with lots of
# white space not supported by the observed data.
# And now let's apply testMultivarOutlierHDR, with pca = TRUE
testMultivarOutlierHDR(dataMatrix = cbind(x, y),
    outlier = outlier, alpha = 0.8, pca = TRUE)
#####################
# Example with four complex variables
    # including correlated and multimodal variables
x <- rnorm(100, 1, 1)
y <- (x*0.8)+rnorm(100)
z \leq sample(c(rnorm(50, 3, 2),
  rnorm(50, 30, 3)))
a <- sample(c(rnorm(50, 3, 2),
  rnorm(50, 10, 3)))+x^2
#plot(x, y)
#plot(x, z)
#plot(x, a)
data \leq cbind(x, y, z, a)
# actual outlier, but maybe not obvious if PCA isn't applied
outlier <- c(2, 0.6, 10, 8)
# this one should appear to be an outlier (but only if PCA is applied)
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8)
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8, pca = FALSE)
# this one should be within the 80% area
outlier <- c(1, 0, 30, 5)
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8)
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8, pca = FALSE)
# this one should be an obvious outlier no matter what
outlier <- c(3, -2, 20, 18)
# this one should be outside the 80% area
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8)
testMultivarOutlierHDR(dataMatrix = data,
  outlier = outlier, alpha = 0.8, pca = FALSE)
```
testMultivarOutlierHDR

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