

Package: RRPP (via r-universe)

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Title Linear Model Evaluation with Randomized Residuals in a Permutation Procedure

Version 2.0.3.999

Description Linear model calculations are made for many random versions of data. Using residual randomization in a permutation procedure, sums of squares are calculated over many permutations to generate empirical probability distributions for evaluating model effects. This package is described by Collyer & Adams (2018). Additionally, coefficients, statistics, fitted values, and residuals generated over many permutations can be used for various procedures including pairwise tests, prediction, classification, and model comparison. This package should provide most tools one could need for the analysis of high-dimensional data, especially in ecology and evolutionary biology, but certainly other fields, as well.

Depends R (>= 4.4.0)

License GPL (>= 3)

URL <https://github.com/mlcollyer/RRPP>

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Imports parallel, ape, ggplot2, Matrix

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VignetteBuilder knitr

NeedsCompilation no

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Config/testthat/edition 3**Repository** <https://phylotastic.r-universe.dev>**RemoteUrl** <https://github.com/mlcollyer/RRPP>**RemoteRef** HEAD**RemoteSha** 49ed1516a0b3aab931d8ff7815f23673d7fe7f5**Contents**

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add.trajectories	<i>Plot Function for RRPP</i>
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Description

Function adds trajectories to a principal component plot

Usage

```
add.trajectories(
  TP,
  traj.pch = 21,
  traj.col = 1,
  traj.lty = 1,
  traj.lwd = 1,
  traj.cex = 1.5,
  traj.bg = 1,
  start.bg = 3,
  end.bg = 2
)
```

Arguments

TP	plot object (from plot.trajectory.analysis)
traj.pch	Plotting "character" for trajectory points. Can be a single value or vector of length equal to the number of trajectories. See par and its description for pch.
traj.col	The color of trajectory lines. Can be a single value or vector of length equal to the number of trajectories. See par and its description for col.
traj.lty	Trajectory line type. Can be a single value or vector of length equal to the number of trajectories. See par and its description for lty.
traj.lwd	Trajectory line width. Can be a single value or vector of length equal to the number of trajectories. See par and its description for lwd.
traj.cex	Trajectory point character expansion. Can be a single value or vector of length equal to the number of trajectories. See par and its description for cex.
traj.bg	Trajectory point background. Can be a single value or vector of length equal to the number of trajectories. See par and its description for bg.
start.bg	Trajectory point background, just the start points. Can be a single value or vector of length equal to the number of trajectories. See par and its description for bg. Green start points are the default.
end.bg	Trajectory point background, just the end points. Can be a single value or vector of length equal to the number of trajectories. See par and its description for bg. Red end points are the default.

Details

The function adds trajectories to a plot made by [plot.trajectory.analysis](#). This function has a restricted set of plot parameters based on the number of trajectories to be added to the plot.

Author(s)

Michael Collyer

References

- Adams, D. C., and M. M. Cerney. 2007. Quantifying biomechanical motion using Procrustes motion analysis. *J. Biomech.* 40:437-444.
- Adams, D. C., and M. L. Collyer. 2007. The analysis of character divergence along environmental gradients and other covariates. *Evolution* 61:510-515.
- Adams, D. C., and M. L. Collyer. 2009. A general framework for the analysis of phenotypic trajectories in evolutionary studies. *Evolution* 63:1143-1154.
- Collyer, M. L., and D. C. Adams. 2007. Analysis of two-state multivariate phenotypic change in ecological studies. *Ecology* 88:683-692.
- Collyer, M. L., and D. C. Adams. 2013. Phenotypic trajectory analysis: comparison of shape change patterns in evolution and ecology. *Hystrix* 24: 75-83.
- Collyer, M.L., D.J. Sekora, and D.C. Adams. 2015. A method for analysis of phenotypic change for phenotypes described by high-dimensional data. *Heredity*. 115:357-365.

See Also

[plot.default](#) and [par](#)

add.tree

Plot tool to add phylogenetic trees to ordination plots

Description

Function adds a tree based on a description of edges from a class phylo object to an existing plot made from an ordinate object.

Usage

```
add.tree(  
  OP,  
  tree,  
  edge.col = 1,  
  edge.lty = 1,  
  edge.lwd = 1,  
  anc.pts = FALSE,  
  return.ancs = FALSE,  
  ...  
)
```

Arguments

OP	An object with class <code>plot.ordinate</code> .
tree	An object of class <code>phylo</code> .
edge.col	A single value or vector equal to the number of edges for edge colors.
edge.lty	A single value or vector equal to the number of edges for edge line type
edge.lwd	A single value or vector equal to the number of edges for edge line weight.
anc.pts	A logical value for whether to add points for ancestral values.
return.ancs	A logical value for whether ancestral values should be printed.
...	Arguments passed onto <code>points</code> , used only for ancestral points.

Details

With some `ordinate` plots, it might be desirable to add a tree connecting points in a prescribed way, which would be tedious using `points` or `lines`. This function will project a tree from an object of class `phylo` into a plot with class, `plot.ordinate`. Using an edges matrix from a `phylo` object, this function will systematically connect plot points with lines that pass through estimated ancestral character points in the same plot space. Ancestral states are estimated assuming a Brownian motion model of evolutionary divergence.

Author(s)

Michael Collyer

See Also

[lines](#) and [points](#)

Examples

```
# Examples use residuals from a regression of salamander morphological
# traits against body size (snout to vent length, SVL).
# Observations are species means and a phylogenetic covariance matrix
# describes the relatedness among observations.

data("PlethMorph")
Y <- as.data.frame(PlethMorph[c("TailLength", "HeadLength",
"Snout.ey", "BodyWidth",
"Forelimb", "Hindlimb")])
Y <- as.matrix(Y)
R <- lm.rrpp(Y ~ SVL, data = PlethMorph,
iter = 0, print.progress = FALSE)$LM$residuals

PCA <- ordinate(R, scale. = TRUE)
pc.plot <- plot(PCA, pch = 19, col = "blue")

add.tree(pc.plot, tree = PlethMorph$tree, anc.pts = TRUE,
pch = 19, cex = 0.5, col = "red")
```

`anova.lm.rppp`*ANOVA for lm.rppp model fits*

Description

Computes an analysis of variance (ANOVA) table using distributions of random statistics from [lm.rppp](#). ANOVA can be performed on one model or multiple models. If the latter, the first model is considered a null model for comparison to other models. The ANOVA is functionally similar to a non-parametric likelihood ratio test for all null-full model comparisons. Residuals from the null model will be used to generate random pseudo-values via RRPP for evaluation of subsequent models. The permutation schedule from the null model will be used for random permutations. This function does not correct for improper null models. One must assure that the null model is nested within the other models. Illogical results can be generated if this is not the case.

Usage

```
## S3 method for class 'lm.rppp'
anova(
  object,
  ...,
  effect.type = c("F", "cohenf", "SS", "MS", "Rsq"),
  error = NULL,
  print.progress = TRUE
)
```

Arguments

<code>object</code>	Object from lm.rppp
<code>...</code>	Additional lm.rppp model fits or other arguments passed to <code>anova</code> .
<code>effect.type</code>	One of "F", "cohenf", "SS", "MS", "Rsq" to choose from which distribution of statistics to calculate effect sizes (Z). See lm.rppp .
<code>error</code>	An optional character string to define MS error term for calculation of F values. See lm.rppp for examples.
<code>print.progress</code>	A logical argument if multiple models are used and one wishes to view progress for sums of squares (SS) calculations.

Author(s)

Michael Collyer

Examples

```
## Not run:
# See examples for lm.rppp to see how anova.lm.rppp works in conjunction
# with other functions
```

```

data(Pupfish)
names(Pupfish)
Pupfish$logSize <- log(Pupfish$CS) # better to not have functions in formulas

# Single-Model ANOVA

fit <- lm.rpp(coords ~ logSize + Sex*Pop, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 999)
anova(fit)
anova(fit, effect.type = "MS")
anova(fit, effect.type = "Rsq")
anova(fit, effect.type = "cohenf")

# Multi-Model ANOVA (like a Likelihood Ratio Test)
fit.size <- lm.rpp(coords ~ logSize, SS.type = "I", data = Pupfish,
print.progress = FALSE, iter = 999)
fit.sex <- lm.rpp(coords ~ logSize + Sex, SS.type = "I", data = Pupfish,
print.progress = FALSE, iter = 999)
fit.pop <- lm.rpp(coords ~ logSize + Pop, SS.type = "I", data = Pupfish,
print.progress = FALSE, iter = 999)
anova(fit.size, fit.sex, fit.pop,
print.progress = FALSE) # compares two models to the first

# see lm.rpp examples for mixed model ANOVA example and how to vary SS type

## End(Not run)

```

```
anova.measurement.error
```

ANOVA for lm.rpp model fits used in measurement.error

Description

Computes an analysis of variance (ANOVA) table using distributions of random statistics from [lm.rpp](#). This function is the same as [anova.lm.rpp](#) but includes statistics specific to [measurement.error](#), and with restrictions on how P-values and effect.sizes are calculated.

Usage

```
## S3 method for class 'measurement.error'
anova(object, ...)
```

Arguments

object	Object from lm.rpp
...	Additional lm.rpp model fits or other arguments passed to anova.

Author(s)

Michael Collyer

Examples

```
# See measurement.error help file examples for use.
```

classify

Deprecated functions in RRPP

Description

The following function has been deprecated in RRPP

Usage

```
classify()
```

Details

This function has been deprecated. Use [prep.lda](#) instead.

coef.lm.rpp

coef for lm.rpp model fits

Description

Computes ordinary or generalized least squares coefficients over the permutations of an [lm.rpp](#) model fit with predefined random permutations. For each coefficient vector, the Euclidean distance is calculated as an estimate of the amount of change in Y, the $n \times p$ matrix of dependent variables; larger distances mean more change in location in the data space associated with a one unit change in the model design, for the parameter described. Random coefficients are based on either RRPP or FRPP, as defined by the [lm.rpp](#) model fit.

This function can be used to test the specific coefficients of an [lm.rpp](#) fit. The test statistics are the distances (d), which are also standardized (Z-scores). The Z-scores might be easier to compare, as the expected values for random distances can vary among coefficient vectors.

If RRPP is used, all distributions of coefficient vector distances are based on appropriate null models, as defined by SS type. Please be aware that this can result in two seemingly strange but reasonable phenomena. First, if type II or type III SS is used, the intercept will not appear in test results (because the function seeks model parameter differences to know for which coefficients to calculate Euclidean distances). Even if it appears for type I SS, this is merely an artifact of sequential model building and there really is no meaningful test of intercept = 0. Second, Euclidean distances might not always be logical, especially when viewing univariate coefficients, in which case the expected d is $|\text{bl}|$. Coefficients without a test are based on the full model; tests are based on the estimates of

coefficients (b), given a null model. For example, for a model, $y \sim b_1 + b_2 + b_3$, with type I SS, b_2 will be estimated and tested, using a null model, $y \sim b_1$ and a full model, $y \sim b_1 + b_2$. The estimate for b_2 might not be the same in the test as when estimated from the model, $y \sim b_1 + b_2 + b_3$. Therefore, the d statistic might not reflect what one would expect from the full model (like when using type III SS).

Usage

```
## S3 method for class 'lm.rpp'
coef(object, SE = FALSE, test = FALSE, confidence = 0.95, ...)
```

Arguments

object	Object from <code>lm.rpp</code>
SE	Whether to include standard errors of coefficients. Standard errors are muted if <code>test = TRUE</code> .
test	Logical argument that if <code>TRUE</code> , performs hypothesis tests (Null hypothesis is vector distance = 0) for the observed coefficients. If <code>FALSE</code> , only the observed coefficients are returned.
confidence	The desired confidence limit to print with a table of summary statistics, if <code>test = TRUE</code> . Because distances are directionless, confidence limits are one-tailed.
...	Other arguments (currently none)

Author(s)

Michael Collyer

Examples

```
## Not run:
# See examples for lm.rpp to see how anova.lm.rpp works in conjunction
# with other functions

data(Pupfish)
names(Pupfish)
Pupfish$logSize <- log(Pupfish$CS)

fit <- lm.rpp(coords ~ logSize + Sex*Pop,
SS.type = "I", data = Pupfish, verbose = TRUE)

coef(fit) # Just coefficients
coef(fit, SE = TRUE) # Coefficients with SE
coef(fit, test = TRUE,
confidence = 0.99) # Test of coefficients

## End(Not run)
```

`convert2ggplot`*Convert RRPP plots to ggplot objects*

Description

Function attempts to coerce plot information from an RRPP plot object to an amenable ggplot object.

Usage

```
convert2ggplot(object)
```

Arguments

`object` A plot object produced from `plot.lm.rrpp` and type equals either "PC" or "regression", `plot.predict.lm.rrpp`, or `plot.ordinate`. Essentially, any RRPP plot except a series of diagnostic plots should work.

Details

This function will attempt to use the plot arguments from an RRPP plot object to make a ggplot that can be additionally updated, as desired. Not all plot characteristics can be converted. For example, text arguments are not currently passed to `ggplot`, as the `text` function and `geom_text` arguments do not easily align. However, one can use text arguments produced by a RRPP plot object and `geom_text` to augment a ggplot object the way they like.

This function assumes no responsibility for arguments made by `ggplot`. It merely produces a ggplot object that should resemble an RRPP plot default. Any augmentation of ggplot objects can be done either by direct intervention of the ggplot produced or reformatting the initial RRPP plot produced. One should not expect direct correspondence between R base plot parameters and ggplot parameters. For example, error bars will generally appear as different widths, without an easy way to control them, changing from one format to the other.

Author(s)

Michael Collyer

Examples

```
## Not run:
### Linear Model Example

data(Pupfish)
fit <- lm.rrpp(coords ~ log(CS) + Sex*Pop, SS.type = "I",
  data = Pupfish, print.progress = FALSE)

# Predictions (holding alternative effects constant)

shapeDF <- expand.grid(Sex = levels(Pupfish$Sex),
```

```

Pop = levels(Pupfish$Pop))
rownames(shapeDF) <- paste(shapeDF$Sex, shapeDF$Pop, sep = ".")

shapePreds <- predict(fit, shapeDF)
summary(shapePreds, PC = TRUE)

# Plot prediction

P <- plot(shapePreds, PC = TRUE, ellipse = TRUE)
convert2ggplot(P)

### Ordination Example

data("PlethMorph")

Y <- as.data.frame(PlethMorph[c("TailLength", "HeadLength",
                               "Snout.eye", "BodyWidth",
                               "Forelimb", "Hindlimb")])

Y <- as.matrix(Y)
R <- lm.rpp(Y ~ SVL, data = PlethMorph,
           print.progress = FALSE)$LM$residuals

# PCA (on correlation matrix)

PCA.ols <- ordinate(R, scale. = TRUE)
PCA.ols$rot
prcomp(R, scale. = TRUE)$rotation # should be the same

PCA.gls <- ordinate(R, scale. = TRUE,
                  transform. = FALSE,
                  Cov = PlethMorph$PhyCov)

P <- plot(PCA.gls)
convert2ggplot(P)

## End(Not run)

```

effect.size

Obtain Effect-size from a vector of values

Description

A function to find the effect size (Z-score) of a target, from a vector of values presumably obtained in random permutations.

Usage

```
effect.size(x, center = TRUE, target = NULL)
```

Arguments

x	The vector of data to use.
center	Logical value for whether to center x.
target	The value to target in the distribution. (If null, the first value in the vector is used.). If the target exists outside the range of x, very small or very large z-scores are possible. Additionally, if the target is excessively outside of the range of x, it could affect the Box-Cox transformation used to transform x.

Author(s)

Michael Collyer

fishy

Simulated fish data for measurement error analysis

Description

Simulated fish data for measurement error analysis

Details

Data as simulated in Collyer and Adams (2024), resembling a fish shape, comprising Procrustes coordinates for 11 anatomical landmarks. Data represent 120 configurations for 60 subjects, each with two replicates of measurement. The 60 subjects represent 20 subjects each from three groups.

Author(s)

Michael Collyer

References

Collyer, M.L, and D.C. Adams. 2024. Interrogating random and systematic measurement error in morphometric data. *Evolutionary Biology*. In press.

fitted.lm.rppp	<i>Extract fitted values</i>
----------------	------------------------------

Description

Extract fitted values

Usage

```
## S3 method for class 'lm.rppp'
fitted(object, ...)
```

Arguments

object	plot object (from lm.rppp)
...	Arguments passed to other functions

Author(s)

Michael Collyer

Examples

```
# See examples for lm.rppp
```

focusMEonSubjects	<i>Plot Function for RRPP</i>
-------------------	-------------------------------

Description

Reduces a plot.measurement.error to a single research subject. This can be for cases when many overlapping subjects in a plot obscure interpretation for specific subjects.

Usage

```
focusMEonSubjects(x, subjects = NULL, shadow = TRUE, ...)
```

Arguments

x	Plot from plot.measurement.error
subjects	The specific subject to plot
shadow	A logical value for whether to show other subject values as shadows of their locations.
...	Other arguments passed onto plot

Author(s)

Michael Collyer

getANOVASStats

*Utility Function for RRPP***Description**

A function mostly for internal processing but can be used to extract ANOVA statistics for other uses, such as plotting histograms

Usage

```
getANOVASStats(fit, stat = c("SS", "MS", "Rsq", "F", "cohenf", "all"))
```

Arguments

fit	Object from <code>lm.rrpp</code> .
stat	The ANOVA statistic to extract. Returns every RRPP permutation of the statistic. If "all", a list of each statistic is returned.

Author(s)

Michael Collyer

Examples

```
## Not run:
data(Pupfish)
fit <- lm.rrpp(coords ~ log(CS) + Sex*Pop, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 999)
anova(fit)
Fstats <- getANOVASStats(fit, stat = "F")
par(mfrow = c(2, 2))
hist(Fstats$Fs[1,], breaks = 50, main = "log(CS)", xlab = "F")
abline(v = Fstats$Fs[1, 1])
hist(Fstats$Fs[2,], breaks = 50, main = "Sex", xlab = "F")
abline(v = Fstats$Fs[2, 1])
hist(Fstats$Fs[3,], breaks = 50, main = "Pop", xlab = "F")
abline(v = Fstats$Fs[3, 1])
hist(Fstats$Fs[4,], breaks = 50, main = "Sex:Pop", xlab = "F")
abline(v = Fstats$Fs[4, 1])

## End(Not run)
```

getModelCov

Utility Function for RRPP

Description

A function mostly for internal processing but can be used to extract either the model covariance matrix (Cov) or the projection matrix for transformations made from the covariance matrix (Pcov), which is basically the square-root of the covariance matrix. This matrix is the model covariance used for estimation, not the residual covariance matrix (see [getResCov](#)). There are also options for S3 or S4 format versions, or a forcing of symmetry for Pcov.

Usage

```
getModelCov(
  fit,
  type = c("Cov", "Pcov"),
  format = c("S3", "S4"),
  forceSym = TRUE
)
```

Arguments

fit	Object from lm.rrpp
type	Whether the Cov or Pcov matrix is returned
format	Whether an S3 or S4 format is returned
forceSym	Logical value for whether a symmetric matrix should be returned for Pcov, even if Pcov was triangular as a solution.

Author(s)

Michael Collyer

getModels

Utility Function for RRPP

Description

A function mostly for internal processing but can be used to obtain terms, design matrices, or QR decompositions used for each reduced or full model that is fitted in an [lm.rrpp](#) fit.

Usage

```
getModels(fit, attribute = c("terms", "X", "qr", "all"))
```


Arguments

fit	Object from lm.rrpp
attribute	The various attributes that are used to extract RRPP Model information, including "terms", "X" (design matrices), "qr" (QR decompositions), or "all".

Author(s)

Michael Collyer

getPermInfo *Utility Function for RRPP*

Description

A function mostly for internal processing but can be used to extract RRPP permutation information for other reasons.

Usage

```
getPermInfo(  
  fit,  
  attribute = c("perms", "perm.method", "block", "perm.seed", "perm.schedule", "all")  
)
```

Arguments

fit	Object from lm.rrpp
attribute	The various attributes that are used to generate RRPP permutation schedules. If there are n observations, each iteration has some randomization of 1:n, restricted by the arguments that match attributes provided by this function.

Author(s)

Michael Collyer

getResCov	<i>Utility Function for RRPP</i>
-----------	----------------------------------

Description

A function mostly for internal processing but can be used to extract the residual covariance matrix. This matrix is the residual covariance matrix, not the model covariance matrix used for estimation (see [getModelCov](#)). Options for averaging over degrees of freedom or number of observations, plus standardization, are also available.

Usage

```
getResCov(fit, useDf = TRUE, standardize = FALSE)
```

Arguments

fit	Object from lm.rppp
useDf	Logical value for whether the degrees of freedom from the linear model fit should be used (if TRUE), as opposed to the number of observations (if FALSE).
standardize	Logical value for whether residuals should be standardized. If TRUE, a correlation matrix is produced.

Author(s)

Michael Collyer

getTerms	<i>Utility Function for RRPP</i>
----------	----------------------------------

Description

A function mostly for internal processing but can be used to extract The terms for each reduced and full model used in an [lm.rppp](#) fit.

Usage

```
getTerms(fit)
```

Arguments

fit	Object from lm.rppp
-----	-------------------------------------

Author(s)

Michael Collyer

Description

Function performs analyses concerned with the repeatability (reliability) of multivariate data (measurements) collected from the same research subjects. Although there is no requirement for repeated measurements on all research subjects, the analysis assumes that multiple observations are made.

Usage

```
ICCstats(  
  fit,  
  subjects = NULL,  
  with_in = NULL,  
  groups = NULL,  
  multivariate = FALSE,  
  print.AOV = TRUE  
)
```

Arguments

<code>fit</code>	The <code>lm.rpp</code> , previously evaluated.
<code>subjects</code>	A single character value indicating which term in an ANOVA table corresponds to research subjects.
<code>with_in</code>	One or more character values indicating which terms in an ANOVA table are measured within subjects (replications, plus maybe interactions). If <code>NULL</code> , the only replication within-subject will be considered as residuals.
<code>groups</code>	An optional character value to indicate if a factor in the model frame of the <code>lm.rpp</code> fit that could account for subject variation. Using this argument might minimize the importance of subject variation, if subjects have disparate values that could inflate ICC. Note that this name could be different than what is shown in the ANOVA table, if <code>measurement.error</code> was used. Use <code>names(fit\$LM\$data)</code> , substituting <code>fit</code> with the name assigned to the <code>measurement.error</code> object, to know the groups factor, if used.
<code>multivariate</code>	Logical value for whether to include to calculate ICC matrix generalizations and perform eigenanalysis.
<code>print.AOV</code>	Logical value for whether to include ANOVA table as screen output, when calculating ISS statistics. Note that this function can return ICC statistics, even if they do not make sense. It is possible to generate ICC stats with any ANOVA table, with at least one term.

Details

Function uses ANOVA statistics or SSCP matrices to find the ratio of among-subject to within-subject variance. The former is a dispersion-based approach and the latter is a multivariate generalization of the ICC statistic (as a matrix product). The multivariate generalizations of the statistics described by Liljequist et al. (2019) are used to find matrix products, from which eigenanalysis is performed, providing ICC statistics by eigenvectors.

Three statistics describe the ICC for the population, agreement of measurements among subjects, and consistency between measurements. The last statistic does not necessarily measure the sameness between measurements but the consistency of change between measurements, which might be indicative of a systematic measurement error. If groups are used, these three statistics are repeated, using the SSCP for groups-adjusted data. This approach accounts for group differences, which would avoid large subject variation compared to measurement error inflating ICC values. If there are inherently disparate groups from which subjects are sampled, this approach can elucidate better agreement and consistency in light of group differences.

This function is most useful for analyses performed with `measurement.error`, but any `lm.rpp` fit can be used, so long as research subjects can be defined.

It is essential that all arguments are terms that can be found in the model frame of the model fit, as provoke by ANOVA. Using `anova(fit)` will elucidate the row names of the ANOVA that could be used.

Value

Objects of class "ICCstats" return the following:

ICC_disp	The intraclass correlation coefficient (ICC) based on the dispersion of values.
ICC_mult	The eigenvalues of ICC matrices

Author(s)

Michael Collyer

References

Liljequist, D., Elfving, B., & Skavberg Roaldsen, K. (2019). Intraclass correlation—A discussion and demonstration of basic features. *PloS one*, 14(7), e0219854.

Examples

```
## Not run:
# Measurement error analysis on simulated data of fish shapes

data(fishy)

# Analysis unconcerned with groups

ME1 <- measurement.error(
  Y = "coords",
  subjects = "subj",
  replicates = "reps",
```

```

    data = fishy)

anova(ME1)
ICCstats(ME1, subjects = "Subjects", with_in = "Systematic ME")

# Analysis concerned with groups

ME2 <- measurement.error(
  Y = "coords",
  subjects = "subj",
  replicates = "reps",
  groups = "groups",
  data = fishy)

anova(ME2)
ICCstats(ME2, subjects = "Subjects",
  with_in = "Systematic ME", groups = "groups")
ICCstats(ME2, subjects = "Subjects",
  with_in = c("Systematic ME", "Systematic ME:Groups"),
  groups = "groups")

## End(Not run)

```

interSubVar

Reveal the inter-subject variability from a measurement error analysis

Description

Function produces both a list of inter-subject Euclidean distance matrices, based on replicate measurements of the same subjects, and one matrix that summarizes the variability among the inter-subject distances, across subjects. This function can be considered a tool for the evaluation of subject estimate precision. The function, `plot.interSubVar` can produce a heat map of the inter-subject variability.

Usage

```
interSubVar(ME, type = c("range", "sd", "var", "cv"))
```

Arguments

ME	A measurement error object
type	A value to indicate the type of variability (statistic) to measure, which can be one of range (the maximum value minus the minimum value, not the two values), standard deviation (sd), variance (var), or coefficient of variation (cv). No attempt is made to assure the distribution of values is appropriate for the statistics. For example, if only two replicates are available, using sd, var, or cv might not be wise. Or if the replicated values are exact, cv will be NA (and other stats will be 0). Choice of statistic should consider the distribution of values.

Value

An object of class `interSubVar` is a list containing the following

<code>var.map</code>	A distance matrix object with values that map the variability statistic used for inter-subject Euclidean distances.
<code>distance.mats</code>	The inter-subject distance matrices for every replicate.
<code>subject.order</code>	A vector of subject levels in the order that was used to guarantee consistent sorting across distance matrices.
<code>var.map</code>	The variability type (statistic) that was used.

Author(s)

Michael Collyer

Examples

```
## Not run:
# Measurement error analysis on simulated data of fish shapes

data(fishy)

# Analysis unconcerned with groups

ME1 <- measurement.error(
  Y = "coords",
  subjects = "subj",
  replicates = "reps",
  data = fishy)

anova(ME1)
ICCstats(ME1, subjects = "Subjects", with_in = "Systematic ME")
plot(ME1)

# Analysis concerned with groups

ME2 <- measurement.error(
  Y = "coords",
  subjects = "subj",
  replicates = "reps",
  groups = "groups",
  data = fishy)

anova(ME2)
ICCstats(ME2, subjects = "Subjects",
  with_in = "Systematic ME", groups = "groups")
P <- plot(ME2)
focusMEonSubjects(P, subjects = 18:20, shadow = TRUE)

## End(Not run)
```

lm.rpp	<i>Linear Model Evaluation with a Randomized Residual Permutation Procedure</i>
--------	---

Description

Function performs a linear model fit over many random permutations of data, using a randomized residual permutation procedure.

Usage

```
lm.rpp(
  f1,
  iter = 999,
  turbo = FALSE,
  seed = NULL,
  int.first = FALSE,
  RRPP = TRUE,
  full.resid = FALSE,
  block = NULL,
  SS.type = c("I", "II", "III"),
  data = NULL,
  Cov = NULL,
  print.progress = FALSE,
  Parallel = FALSE,
  verbose = FALSE,
  ...
)
```

Arguments

f1	A formula for the linear model (e.g., $y \sim x_1 + x_2$). Can also be a linear model fit from lm .
iter	Number of iterations for significance testing
turbo	A logical value that if TRUE, suppresses coefficient estimation in every random permutation. This will affect subsequent analyses that require random coefficients (see coef.lm.rpp) but might be useful for large data sets for which only ANOVA is needed.
seed	An optional argument for setting the seed for random permutations of the re-sampling procedure. If left NULL (the default), the exact same P-values will be found for repeated runs of the analysis (with the same number of iterations). If seed = "random", a random seed will be used, and P-values will vary. One can also specify an integer for specific seed values, which might be of interest for advanced users.
int.first	A logical value to indicate if interactions of first main effects should precede subsequent main effects

RRPP	A logical value indicating whether residual randomization should be used for significance testing
full.resid	A logical value for whether to use the full model residuals, only (sensu ter Braak, 1992). This only works if RRPP = TRUE and SS.type = III. Rather than permuting reduced model residuals, this option permutes only the full model residuals in every random permutation of RRPP.
block	An optional factor for blocks within which to restrict resampling permutations.
SS.type	A choice between type I (sequential), type II (hierarchical), or type III (marginal) sums of squares and cross-products computations.
data	A data frame for the function environment, see rrpp.data.frame
Cov	An optional argument for including a covariance matrix to address the non-independence of error in the estimation of coefficients (via GLS). If included, any weights are ignored.
print.progress	A logical value to indicate whether a progress bar should be printed to the screen. This is helpful for long-running analyses.
Parallel	Either a logical value to indicate whether parallel processing should be used, a numeric value to indicate the number of cores to use, or a predefined socket cluster. This argument defines parallel processing via the <code>parallel</code> library. If TRUE, this argument invokes forking or socket cluster assignment of all processor cores, except one. If FALSE, only one core is used. A numeric value directs the number of cores to use, but one core will always be spared. If a predefined socket cluster (Windows) is provided, the cluster information will be passed to <code>parallel</code> .
verbose	A logical value to indicate if all possible output from an analysis should be retained. Generally this should be FALSE, unless one wishes to extract, e.g., all possible terms, model matrices, QR decomposition, or random permutation schemes.
...	Arguments typically used in <code>lm</code> , such as <code>weights</code> or <code>offset</code> , passed on to <code>LM.fit</code> (an internal RRPP function) for estimation of coefficients. If both <code>weights</code> and a covariance matrix are included, <code>weights</code> are ignored (since inverses of <code>weights</code> are the diagonal elements of weight matrix, used in lieu of a covariance matrix.)

Details

The function fits a linear model using ordinary least squares (OLS) or generalized least squares (GLS) estimation of coefficients over any number of random permutations of the data. A permutation procedure that randomizes vectors of residuals is employed. This procedure can randomize two types of residuals: residuals from null models or residuals from an intercept model. The latter is the same as randomizing full values, and is referred to as a full randomization permutation procedure (FRPP); the former uses the residuals from null models, which are defined by the type of sums of squares and cross-products (SSCP) sought in an analysis of variance (ANOVA), and is referred to as a randomized residual permutation procedure (RRPP). Types I, II, and III SSCPs are supported.

Users define the SSCP type, the permutation procedure type, whether a covariance matrix is included (GLS estimation), and a few arguments related to computations. Results comprise observed linear model results (coefficients, fitted values, residuals, etc.), random sums of squares (SS) across

permutation iterations, and other parameters for performing ANOVA and other hypothesis tests, using empirically-derived probability distributions.

lm.rppp emphasizes estimation of standard deviates of observed statistics as effect sizes from distributions of random outcomes. When performing ANOVA, using the `anova` function, the effect type (statistic choice) can be varied. See `anova.lm.rppp` for more details. Please recognize that the type of SS must be chosen prior to running `lm.rppp` and not when applying `anova` to the `lm.rppp` fit, as design matrices for the linear model must be created first. Therefore, `SS.type` is an argument for `lm.rppp` and `effect.type` is an argument for `anova.lm.rppp`. If MANOVA statistics are preferred, eigenvalues can be added with `manova.update` and statistics summarized with `summary.manova.lm.rppp`. See `manova.update` for examples.

The `coef.lm.rppp` function can be used to test the specific coefficients of an `lm.rppp` fit. The test statistics are the distances (d), which are also standardized (Z-scores). The Z-scores might be easier to compare, as the expected values for random distances can vary among coefficient vectors (Adams and Collyer 2016).

ANOVA vs. MANOVA:

Two SSCP matrices are calculated for each linear model effect, for every random permutation: R (Residuals or Random effects) and H, the difference between SSCPs for "full" and "reduced" models. (Full models contain and reduced models lack the effect tested; SSCPs are hypothesized to be the same under a null hypothesis, if there is no effect. The difference, H, would have a trace of 0 if the null hypothesis were true.) In RRPP, ANOVA and MANOVA correspond to two different ways to calculate statistics from R and H matrices.

ANOVA statistics are those that find the trace of R and H SSCP matrices before calculating subsequent statistics, including sums of squares (SS), mean squares (MS), and F-values. These statistics can be calculated with univariate data and provide univariate-like statistics for multivariate data. These statistics are dispersion measures only (covariances among variables do not contribute) and are the same as "distance-based" stats proposed by Goodall (1991) and Anderson (2001). MANOVA stats require multivariate data and are implicitly affected by variable covariances. For MANOVA, the inverse of R times H (invR.H) is first calculated for each effect, then eigenanalysis is performed on these matrix products. Multivariate statistics are calculated from the positive, real eigenvalues. In general, inferential conclusions will be similar with either approach, but effect sizes might differ.

ANOVA tables are generated by `anova.lm.rppp` on `lm.rppp` fits and MANOVA tables are generated by `summary.manova.lm.rppp`, after running `manova.update` on `lm.rppp` fits.

Currently, mixed model effects are only possible with \$ANOVA statistics, not \$MANOVA.

More detail is found in the vignette, ANOVA versus MANOVA.

Notes for RRPP 0.5.0 and subsequent versions:

The output from `lm.rppp` has changed, compared to previous versions. First, the \$LM component of output no longer includes both OLS and GLS statistics, when GLS fits are performed. Only GLS statistics (coefficients, residuals, fitted values) are provided and noted with a "gls." tag. GLS statistics can include those calculated when weights are input (similar to the `lm` argument). Unlike previous versions, GLS and weighted LS statistics are not labeled differently, as weighted LS is one form of generalized LS estimation. Second, a new object, \$Models, is included in output, which contains the linear model fits (`lm` attributes) for all reduced and full models that are possible to estimate fits.

Notes for RRPP 0.3.1 and subsequent versions:

F-values via RRPP are calculated with residual SS (RSS) found uniquely for any model terms, as per Anderson and ter Braak (2003). This method uses the random pseudo-data generated by each term's null (reduced) model, meaning RSS can vary across terms. Previous versions used an intercept-only model for generating random pseudo-data. This generally has appropriate type I error rates but can have elevated type I error rates if the observed RSS is small relative to total SS. Allowing term by term unique RSS alleviates this concern.

Value

An object of class `lm.rpp` is a list containing the following

<code>call</code>	The matched call.
<code>LM</code>	Linear Model objects, including data (Y), coefficients, design matrix (X), sample size (n), number of dependent variables (p), dimension of data space (p.prime), QR decomposition of the design matrix, fitted values, residuals, weights, offset, model terms, data (model) frame, random coefficients (through permutations), random vector distances for coefficients (through permutations), whether OLS or GLS was performed, and the mean for OLS and/or GLS methods. Note that the data returned resemble a model frame rather than a data frame; i.e., it contains the values used in analysis, which might have been transformed according to the formula. The response variables are always labeled Y.1, Y.2, ..., in this frame.
<code>ANOVA</code>	Analysis of variance objects, including the SS type, random SS outcomes, random MS outcomes, random R-squared outcomes, random F outcomes, random Cohen's f-squared outcomes, P-values based on random F outcomes, effect sizes for random outcomes, sample size (n), number of variables (p), and degrees of freedom for model terms (df). These objects are used to construct ANOVA tables.
<code>PermInfo</code>	Permutation procedure information, including the number of permutations (perms), The method of residual randomization (perm.method), and each permutation's sampling frame (perm.schedule), which is a list of reordered sequences of 1:n, for how residuals were randomized.
<code>Models</code>	Reduced and full model fits for every possible model combination, based on terms of the entire model, plus the method of SS estimation.

Author(s)

Michael Collyer

References

- Anderson MJ. 2001. A new method for non-parametric multivariate analysis of variance. *Austral Ecology* 26: 32-46.
- Anderson MJ. and C.J.F. ter Braak. 2003. Permutation tests for multi-factorial analysis of variance. *Journal of Statistical Computation and Simulation* 73: 85-113.
- Collyer, M.L., D.J. Sekora, and D.C. Adams. 2015. A method for analysis of phenotypic change for phenotypes described by high-dimensional data. *Heredity*. 115:357-365.

Adams, D.C. and M.L. Collyer. 2016. On the comparison of the strength of morphological integration across morphometric datasets. *Evolution*. 70:2623-2631.

Adams, D.C and M.L. Collyer. 2018. Multivariate phylogenetic anova: group-clade aggregation, biological challenges, and a refined permutation procedure. *Evolution*. 72:1204-1215.

ter Braak, C.J.F. 1992. Permutation versus bootstrap significance tests in multiple regression and ANOVA. pp 79–86 In *Bootstrapping and Related Techniques*. eds K-H. Jockel, G. Rothe & W. Sendler. Springer-Verlag, Berlin. [lm](#) for more on linear model fits.

See Also

procD.lm and procD.pgls within geomorph;

Examples

```
## Not run:

# Examples use geometric morphometric data
# See the package, geomorph, for details about obtaining such data

data("PupfishHeads")
names(PupfishHeads)

# Head Size Analysis (Univariate)-----

fit <- lm.rpp(log(headSize) ~ sex + locality/year, SS.type = "I",
data = PupfishHeads, print.progress = FALSE, iter = 999)
summary(fit)
anova(fit, effect.type = "F") # Maybe not most appropriate
anova(fit, effect.type = "Rsq") # Change effect type, but still not
# most appropriate

# Mixed-model approach (most appropriate, as year sampled is a random
# effect:

anova(fit, effect.type = "F", error = c("Residuals", "locality:year",
"Residuals"))

# Change to Type III SS

fit <- lm.rpp(log(headSize) ~ sex + locality/year, SS.type = "III",
data = PupfishHeads, print.progress = FALSE, iter = 999,
verbose = TRUE)
summary(fit)
anova(fit, effect.type = "F", error = c("Residuals", "locality:year",
"Residuals"))

# Coefficients Test

coef(fit, test = TRUE)

# Predictions (holding alternative effects constant)
```

```

sizeDF <- data.frame(sex = c("Female", "Male"))
rownames(sizeDF) <- c("Female", "Male")
sizePreds <- predict(fit, sizeDF)
summary(sizePreds)
plot(sizePreds)

# Diagnostics plots of residuals

plot(fit)

# Body Shape Analysis (Multivariate) -----

data(Pupfish)
names(Pupfish)

# Note:

dim(Pupfish$coords) # highly multivariate!
fit <- lm.rppp(coords ~ log(CS) + Sex*Pop, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 999,
verbose = TRUE)
summary(fit, formula = FALSE)
anova(fit)
coef(fit, test = TRUE)

# Predictions (holding alternative effects constant)

shapeDF <- expand.grid(Sex = levels(Pupfish$Sex),
Pop = levels(Pupfish$Pop))
rownames(shapeDF) <- paste(shapeDF$Sex, shapeDF$Pop, sep = ".")
shapeDF

shapePreds <- predict(fit, shapeDF)
summary(shapePreds)
summary(shapePreds, PC = TRUE)

# Plot prediction

plot(shapePreds, PC = TRUE)
plot(shapePreds, PC = TRUE, ellipse = TRUE)

# Diagnostics plots of residuals

plot(fit)

# PC-plot of fitted values

groups <- interaction(Pupfish$Sex, Pupfish$Pop)
plot(fit, type = "PC", pch = 19, col = as.numeric(groups))

# Regression-like plot

```

```

plot(fit, type = "regression", reg.type = "PredLine",
     predictor = log(Pupfish$CS), pch=19,
     col = as.numeric(groups))

# Body Shape Analysis (Distances) -----

D <- dist(Pupfish$coords) # inter-observation distances
length(D)
Pupfish$D <- D

fitD <- lm.rpp(D ~ log(CS) + Sex*Pop, SS.type = "I",
              data = Pupfish, print.progress = FALSE, iter = 999)

# These should be the same:
summary(fitD, formula = FALSE)
summary(fit, formula = FALSE)

# GLS Example (Univariate) -----

data(PlethMorph)
fitOLS <- lm.rpp(TailLength ~ SVL, data = PlethMorph,
                print.progress = FALSE, iter = 999)
fitGLS <- lm.rpp(TailLength ~ SVL, data = PlethMorph, Cov = PlethMorph$PhyCov,
                print.progress = FALSE, iter = 999)

anova(fitOLS)
anova(fitGLS)

sizeDF <- data.frame(SVL = sort(PlethMorph$SVL))

# Prediction plots

# By specimen
plot(predict(fitOLS, sizeDF)) # Correlated error
plot(predict(fitGLS, sizeDF)) # Independent error

# With respect to independent variable (using abscissa)
plot(predict(fitOLS, sizeDF), abscissa = sizeDF) # Correlated error
plot(predict(fitGLS, sizeDF), abscissa = sizeDF) # Independent error

# GLS Example (Multivariate) -----

Y <- as.matrix(cbind(PlethMorph$TailLength,
                    PlethMorph$HeadLength,
                    PlethMorph$Snout.eye,
                    PlethMorph$BodyWidth,
                    PlethMorph$Forelimb,
                    PlethMorph$Hindlimb))
PlethMorph$Y <- Y
fitOLSm <- lm.rpp(Y ~ SVL, data = PlethMorph,
                 print.progress = FALSE, iter = 999)
fitGLSm <- lm.rpp(Y ~ SVL, data = PlethMorph,

```

```

Cov = PlethMorph$PhyCov,
print.progress = FALSE, iter = 999)

anova(fitOLSm)
anova(fitGLSm)

# Prediction plots

# By specimen
plot(predict(fitOLSm, sizeDF)) # Correlated error
plot(predict(fitGLSm, sizeDF)) # Independent error

# With respect to independent variable (using abscissa)
plot(predict(fitOLSm, sizeDF), abscissa = sizeDF) # Correlated error
plot(predict(fitGLSm, sizeDF), abscissa = sizeDF) # Independent error

## End(Not run)

```

lm.rrpp.ws

Linear Model Evaluation with RRPP performed within subjects

Description

Function performs a linear model fit over many random permutations of data, using a randomized residual permutation procedure restricted to subjects.

Usage

```

lm.rrpp.ws(
  f1,
  subjects,
  iter = 999,
  turbo = FALSE,
  seed = NULL,
  int.first = FALSE,
  RRPP = TRUE,
  data,
  Cov = NULL,
  delta = 0.001,
  gamma = c("sample", "equal"),
  print.progress = FALSE,
  verbose = FALSE,
  Parallel = FALSE,
  ...
)

```

Arguments

<code>f1</code>	A formula for the linear model (e.g., $y \sim x_1 + x_2$).
<code>subjects</code>	A variable that can be found in the data frame indicating the research subjects for the analysis. This variable must be in the data frame. It can be either numeric (if its slot in the data frame is known) or a character, e.g., "sub_id". It is imperative that it is ordered the same as the data but that the data do not have row names the same as subjects. For example, the subjects variable in the data frame might be sub_id: sub1, sub1, sub1, sub2, sub2, sub2, ... and the row names of the data might be obs1, obs2, obs3, obs4, obs5, obs6, ... The data do not need to have row names but the subjects variable has to be provided.
<code>iter</code>	Number of iterations for significance testing
<code>turbo</code>	A logical value that if TRUE, suppresses coefficient estimation in every random permutation. This will affect subsequent analyses that require random coefficients (see <code>coef.lm.rrpp</code>) but might be useful for large data sets for which only ANOVA is needed.
<code>seed</code>	An optional argument for setting the seed for random permutations of the resampling procedure. If left NULL (the default), the exact same P-values will be found for repeated runs of the analysis (with the same number of iterations). If <code>seed = "random"</code> , a random seed will be used, and P-values will vary. One can also specify an integer for specific seed values, which might be of interest for advanced users.
<code>int.first</code>	A logical value to indicate if interactions of first main effects should precede subsequent main effects
<code>RRPP</code>	A logical value indicating whether residual randomization should be used for significance testing
<code>data</code>	A data frame for the function environment, see <code>rrpp.data.frame</code> . A data frame is required for this analysis.
<code>Cov</code>	An optional argument for including a covariance matrix to address the non-independence of error in the estimation of coefficients (via GLS). If included, any weights are ignored. This matrix must match in dimensions either the number of subject levels or the number of observations.
<code>delta</code>	A within-subject scaling parameter for covariances, ranging from 0 to 1. If <code>delta = 0</code> , a slight value (0.001) is added to assure variances of the covariance matrix are 0.1 percent larger than covariances.
<code>gamma</code>	A sample-size scaling parameter that is adjusted to be 1 ("equal") scaling or the square-root of the sample size for subject observations ("sample").
<code>print.progress</code>	A logical value to indicate whether a progress bar should be printed to the screen. This is helpful for long-running analyses.
<code>verbose</code>	A logical value to indicate if all possible output from an analysis should be retained. Generally this should be FALSE, unless one wishes to extract, e.g., all possible terms, model matrices, QR decomposition, or random permutation schemes.
<code>Parallel</code>	Either a logical value to indicate whether parallel processing should be used, a numeric value to indicate the number of cores to use, or a predefined socket

cluster. This argument defines parallel processing via the `parallel` library. If `TRUE`, this argument invokes forking or socket cluster assignment of all processor cores, except one. If `FALSE`, only one core is used. A numeric value directs the number of cores to use, but one core will always be spared. If a predefined socket cluster (Windows) is provided, the cluster information will be passed to `parallel`.

... Arguments typically used in `lm`, such as `weights` or `offset`, passed on to `lm.rpp` for estimation of coefficients. If both `weights` and a covariance matrix are included, `weights` are ignored (since inverses of `weights` are the diagonal elements of weight matrix, used in lieu of a covariance matrix.)

Details

The function fits a linear model using ordinary least squares (OLS) or generalized least squares (GLS) estimation of coefficients over any number of random permutations of the data, but the permutations are mostly restricted to occur with subject blocks for any model terms other than subjects. All functionality should resemble that of `lm.rpp`. However, an argument for research subjects is also required. The purpose of this function is to account for the non-independence among observations of research subjects (due to sampling within subjects), while also allowing for the non-independence among subjects to be considered (Adams and Collyer, submitted).

By comparison, the covariance matrix option in `lm.rpp` must have a one-to-one match to observations, which can be matched by the row names of the data. In this function, the covariance matrix can be the same one used in `lm.rpp` but the number of observations can be greater. For example, if subjects are species or some other level of taxonomic organization, data can comprise measurements on individuals. Users have the option to expand the covariance matrix for subjects or input one they have generated.

Irrespective of covariance matrix type, the row names of the data matrix must match the subjects. This step assures that the analysis can proceed in `lm.rpp`. It is also best to make sure to use an `rpp.data.frame`, so that the subjects can be a name in that data frame. For example, if research subjects are species and data (observations) are collected from individuals within species, then a procedure like the following should produce results:

```
rownames(Y) <- species
rdf <- rpp.data.frame(Y = Y, subjects = species, x = x)
fit <- lm.rpp.ws(Y ~ species * x, subject = species, data = rdf, Cov = myCov, ...)
```

where ... means other arguments. The covariances in the the Covariance matrix can be sorted by the subjects factor but data will not be sorted. Therefore, names matching the subjects is essential. Additionally, subjects must be a factor in the data frame or a factor in the global environment. It cannot be part of a list. Something like `subjects <- mylist$species` will not work. Assuring that data and subjects are in the same `rpp.data.frame` object as data is the best way to avoid errors.

Most attributes for this analysis are explained with `lm.rpp`. The notable different attributes for this function are that: (1) a covariance matrix for the non-independence of subjects can be either a symmetric matrix that matches in dimensions the number of subjects or the number of observations; (2) a parameter (`delta`) that can range between near 0 and 1 to calibrate the covariances between observations of different subjects; and (3) a parameter (`gamma`) that is either 1 (equal) or the square-root of the subject sample size (`sample`) to calibrate the covariances among observations within subjects. If `delta = 0`, it is expected that the covariance between individual observations, between

subjects, is the same as expected from the covariance matrix, as if observations were the single observations made on subjects. As δ approaches 1, the observations become more independent, as if it is expected that the many observations would not be expected to be as correlated as if from one observation. Increasing δ might be useful, if, for example, many individuals are sampled within species, from different locations, different age groups, etc. Alternatively, the sample size (n_i) for subject i can also influence the trend of inter-subject covariances. If more individual observations are sampled, the correlation between subjects might be favored to be smaller compared to fewer observations. The covariances can be adjusted to allow for greater independence among observations to be assumed for larger samples.

A design matrix, \mathbf{X} , is constructed with 0s and 1s to indicate subjects association, and it is used to expand the covariance matrix (\mathbf{C}) by $\mathbf{XCt(X)}$, where $\mathbf{t(X)}$ is the matrix transpose. The parameters in \mathbf{X} are multiplied by $\exp(-\delta * \gamma)$ to scale the covariances. (If $\delta = 0$ and $\gamma = 1$, they are unscaled.)

These options for scaling covariances could be important for data with hierarchical organization. For example, data sampled from multiple species with expected covariances among species based on phylogenetic distances, might be expected to not covary as strongly if sampling encounters other strata like population, sex, and age. An a priori expectation is that covariances among observations would be expected to be smaller than between species, if only one observation per species were made.

If one wishes to have better control over between-subject and within-subject covariances, based on either a model or empirical knowledge, a covariance matrix should be generated prior to analysis. One can input a covariance matrix with dimensions the same as $\mathbf{XCt(X)}$, if they prefer to define covariances in an alternative way. A function to generate such matrices based on separate inter-subject and intra-subject covariance matrices is forthcoming.

IMPORTANT. It is assumed that either the levels of the covariance matrix (if subject by subject) match the subject levels in the subject argument, or that the order of the covariance matrix (if observation by observation) matches the order of the observations in the data. No attempt is made to reorder a covariance matrix by observations and row-names of data are not used to re-order the covariance matrix. If the covariance matrix is small (same in dimension as the number of subject levels), the function will compile a large covariance matrix that is correct in terms of order, but this is based on the subjects argument, only.

The covariance matrix is important for describing the expected covariances among observations, especially knowing observations between and within subjects are not independent. However, the randomization of residuals in a permutation procedure (RRPP) is also important for testing inter-subject and intra-subject effects. There are two RRPP philosophies used. If the variable for subjects is part of the formula, the subject effect is evaluated with type III sums of squares and cross-products (estimates SSCPs between a model with all terms and a model lacking subject term), and RRPP performed for all residuals of the reduced model. Effects for all other terms are evaluated with type II SSCPs and RRPP restricted to randomization of reduced model residuals, within subject blocks. This assures that subject effects are held constant across permutations, so that intra-subject effects are not confounded by inter-subject effects.

More details will be made and examples provided after publication of articles introducing the novel RRPP approach.

The `lm.rpp` arguments not available for this function include: `full.resid`, `block`, and `SS.type`. These arguments are fixed because of the within-subject blocking for tests, plus the requirement for type II SS for within-subject effects.

Value

An object of class `lm.rpp.ws` is a list containing the following

<code>call</code>	The matched call.
<code>LM</code>	Linear Model objects, including data (Y), coefficients, design matrix (X), sample size (n), number of dependent variables (p), dimension of data space (p.prime), QR decomposition of the design matrix, fitted values, residuals, weights, offset, model terms, data (model) frame, random coefficients (through permutations), random vector distances for coefficients (through permutations), whether OLS or GLS was performed, and the mean for OLS and/or GLS methods. Note that the data returned resemble a model frame rather than a data frame; i.e., it contains the values used in analysis, which might have been transformed according to the formula. The response variables are always labeled Y.1, Y.2, ..., in this frame.
<code>ANOVA</code>	Analysis of variance objects, including the SS type, random SS outcomes, random MS outcomes, random R-squared outcomes, random F outcomes, random Cohen's f-squared outcomes, P-values based on random F outcomes, effect sizes for random outcomes, sample size (n), number of variables (p), and degrees of freedom for model terms (df). These objects are used to construct ANOVA tables.
<code>PermInfo</code>	Permutation procedure information, including the number of permutations (perms), The method of residual randomization (perm.method), and each permutation's sampling frame (perm.schedule), which is a list of reordered sequences of 1:n, for how residuals were randomized.
<code>Models</code>	Reduced and full model fits for every possible model combination, based on terms of the entire model, plus the method of SS estimation.

Author(s)

Michael Collyer

References

Adams, D.C and M.L Collyer. (submitted) Extended phylogenetic regression models for comparing within-species patterns across the Tree of Life. *Methods in Ecology and Evolution*

ter Braak, C.J.F. 1992. Permutation versus bootstrap significance tests in multiple regression and ANOVA. pp .79–86 In *Bootstrapping and Related Techniques*. eds K-H. Jockel, G. Rothe & W. Sandler. Springer-Verlag, Berlin. [lm](#) for more on linear model fits.

See Also

[lm.rpp](#); [measurement.error](#)

Examples

```
## Not run:
data(fishy)
```

```

suppressWarnings(fit <- lm.rppp.ws(coords ~ subj + groups * reps,
  subjects = "subj",
  data = fishy))

anova(fit)

## End(Not run)

```

logLik.lm.rppp

Calculate the log-likelihood of a lm.rppp fit

Description

logLik.lm.rppp returns the log-likelihood of an lm.rppp object. Ridge regularization will be performed for ill-conditioned or singular residual covariance matrices, but dimension reduction could be augmented via projection, using the arguments, tol and pc.no. See [ordinate](#) for details.

Usage

```

## S3 method for class 'lm.rppp'
logLik(object, tol = NULL, pc.no = NULL, Z = TRUE, gls.null = FALSE, ...)

```

Arguments

object	Object from lm.rppp
tol	A value indicating the magnitude below which components should be omitted, following projection. See ordinate for details.
pc.no	Optionally, a number specifying the maximal number of principal components, passed onto ordinate , as argument, rank.
Z	A logical value for whether to calculate Z scores based on RRPP.
gls.null	A logical value for if a fit has a GLS estimation, should the null model (intercept) also have a GLS estimation, for estimating Z. Should be FALSE if the log-likelihood is measured to compare different GLS estimations for a covariance matrices
...	further arguments passed to or from other methods

Author(s)

Michael Collyer

looCV

*Diagnostic cross-validation tool for ordination based on fitted values***Description**

Function performs a leave-one-out cross-validation estimate of ordination scores, which is helpful for determining if apparent "group differences" in ordination plots arise merely from data dimensionality.

Usage

```
looCV(fit, ...)
```

Arguments

<code>fit</code>	A <code>lm.rpp</code> fit.
<code>...</code>	Arguments passed to <code>ordinate</code>

Details

The function uses the strategy of Thioulouse et al. (2021) to perform N ordinations for N observations, in which each of the N observations are left out of the estimation of linear model coefficients, but the vector of data for the left-out observation is projected on the eigenvectors of the fitted values obtained from the leave-one-out cross-validation (jackknife) strategy. The purpose of this diagnostic tool is to determine whether apparent "group differences" in an ordination plot (using the function, `ordinate`) are because of high-dimensional data (number of variables exceed number of observations) rather than real differences. An apparent group difference is common for high-dimensional data, when variables are far greater in number than observations (Cardini et al., 2019). However, leave-one-out cross-validation can help elucidate whether an observed visual difference is spurious.

This function differs from the strategy of Thioulouse et al. (2021) in two important ways. First, this function uses the linear model design from a `lm.rpp` fit, and can contain any number of independent variables, rather than a single factor for groups. Second, after obtaining leave-one-out cross-validated scores, a Procrustes alignment between cross-validated scores and "observed" (real) scores is performed, which minimizes summed squared distances between the alternative ordinations. This latter step assures comparisons are appropriate.

The type = "PC" plot from `plot.lm.rpp` has the same scores as obtained from `ordinate(Y, A = H)`, using the `ordinate` function, where H is a hat matrix (that can be calculated from `plot.lm.rpp` output), and Y is a matrix of data. This function updates H for every possible case that one row of Y is left out (meaning the rotation matrix from `ordinate` is updated N times). If the H matrix is robust in spite of dropped data and design matrix parameters, the result will be similar to the original ordination. If apparent group differences are spurious, H will tend to change, as will data projections.

The functions `summary.looCV` and `plot.looCV` are essential for evaluating results. These support functions compare eigenvalues and projected scores, between observed and cross-validated cases.

This function should be viewed as a diagnostic tool and not as a data transformation tool! The cross-validated scores will not retain Euclidean distances among observations. This could cause problems in analyses that substitute cross-validated scores as data.

Value

An object of class looCV is a list containing the following

d	List of eigenvalues, for observed and cross-validated cases.
scores	List of principal component scores, for observed and cross-validated cases.

Author(s)

Michael Collyer

References

Thioulouse, J., Renaud, S., Dufour, A. B., & Dray, S. (2021). Overcoming the Spurious Groups Problem in Between-Group PCA. *Evolutionary Biology*, In press.

Cardini, A., O'Higgins, P., & Rohlf, F. J. (2019). Seeing distinct groups where there are none: spurious patterns from between-group PCA. *Evolutionary Biology*, 46(4), 303-316.

See Also

[summary.looCV](#), [plot.looCV](#)

Examples

```
# Example with real group differences

data(Pupfish)
fit <- lm.rrpp(coords ~ Pop*Sex, data = Pupfish, iter = 0)
CV1 <- looCV(fit)
summary(CV1)
group <- interaction(Pupfish$Pop, Pupfish$Sex)
plot(CV1, flip = 1, pch = 19, col = group)

# Example with apparent but not real group differences

n <- NROW(Pupfish$coords)
p <- NCOL(Pupfish$coords)
set.seed(1001)
Yr <- matrix(rnorm(n * p), n, p) # random noise

fit2 <- lm.rrpp(Yr ~ Pop*Sex, data = Pupfish, iter = 0)
CV2 <- looCV(fit2)
summary(CV2)
group <- interaction(Pupfish$Pop, Pupfish$Sex)
plot(CV2, pch = 19, col = group)
```

lr_test

*Likelihood ratio test for a linear model, based on RRPP***Description**

Function performs likelihood ratio tests on an `lm.rpp` fit, using RRPP or FRPP. Likelihood ratio statistics are calculated for every random permutation, and the effect size is estimated from the distribution of random statistics. The likelihood ratio tests has some resemblance to MANOVA, especially using Wilks' lambda. Sums of squares and cross-products (SSCP) matrices are calculated over the random permutations of a `lm.rpp` fit. SSCP matrices are computed, as are the inverse of R times H (invR.H), where R is a SSCP for the residuals or random effects and H is the difference between SSCP matrices of full and reduced models (see `manova.update`). From invR.H , Wilks lambda is first estimated, and the likelihood ratio stat is then estimated as $-n * \log(\text{Wilks})$.

This function does one of two things. It either performs an update using `manova.update`, using Wilks' lambda as the test statistic, converting Wilks' lambda to likelihood ratio statistics or it uses the results from a previously performed update to calculate new statistics.

Usage

```
lr_test(fit, verbose = FALSE, ...)
```

Arguments

<code>fit</code>	Linear model fit from <code>lm.rpp</code> or a fit that has already been updated with <code>manova.update</code> .
<code>verbose</code>	Logical value for whether to include all random Wilks' lambda and likelihood ratio statistics from random permutations.
<code>...</code>	Arguments passed onto <code>manova.update</code> .

Author(s)

Michael Collyer

References

Adams, D. C., and M. L. Collyer. 2024. Extended phylogenetic regression models for comparing within-species patterns across the tree of life. *Methods in Ecology and Evolution*. In review.

Examples

```
# Body Shape Analysis (Multivariate) -----
## Not run:
data(Pupfish)

# Although not recommended as a practice, this example will use only
# three principal components of body shape for demonstration.
```

```

# A larger number of random permutations should also be used.

Pupfish$shape <- ordinate(Pupfish$coords)$x[, 1:3]

fit <- lm.rpp(shape ~ log(CS) + Sex, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 499)
summary(fit, formula = FALSE)
anova(fit) # ANOVA table

# MANOVA

fit.m <- manova.update(fit, print.progress = FALSE, tol = 0.001)
summary(fit.m, test = "Roy")
summary(fit.m, test = "Wilks")

# Likelihood Ratio Test

LRT <- lr_test(fit.m)
summary(LRT)

## End(Not run)

```

mahal_dist

Calculate the pairwise Mahalanobis distances between observations

Description

This function emulates the [dist](#) function but allows a covariance matrix (Cov) to be included for standardizing distances. It is assumed that the Covariance matrix makes sense with respect to the data, and that the number of variables match between data and covariance matrix.

Usage

```

mahal_dist(x, Cov, ...)

```

Arguments

x	A numeric matrix of data frame.
Cov	A covariance matrix with the same number of variables as the data.
...	Other arguments passed to dist .

Details

No tests are performed on distances but could be performed with the [pairwise](#) function. Distances are only calculated if the covariance matrix is not singular.

Value

An object of class "dist".

Author(s)

Michael Collyer

Examples

```
# Using the Pupfish data (see lm.rpp help for more detail)

data(Pupfish)
Pupfish$Y <- ordinate(Pupfish$coords)$x[, 1:3]
fit <- lm.rpp(Y ~ Sex * Pop, SS.type = "I",
  data = Pupfish, print.progress = FALSE, iter = 0)
means <- unique(model.matrix(fit)) %*% coef(fit)
rownames(means) <- unique(interaction(Pupfish$Sex, Pupfish$Pop))
means
S <- getResCov(fit)
dist(means)
mahal_dist(means, S)
```

manova.update

MANOVA update for lm.rpp model fits

Description

Function updates a `lm.rpp` fit to add `$MANOVA`, which like `$ANOVA`, provides statistics or matrices typically associated with multivariate analysis of variance (MANOVA).

MANOVA statistics or sums of squares and cross-products (SSCP) matrices are calculated over the random permutations of a `lm.rpp` fit. SSCP matrices are computed, as are the inverse of R times H ($\text{inv}R.H$), where R is a SSCP for the residuals or random effects and H is the difference between SSCP matrices of full and reduced models (see below). From $\text{inv}R.H$, MANOVA statistics are calculated, including Roy's maximum root (eigenvalue), Pillai trace, Hotelling-Lawley trace, and Wilks lambda (via `summary.manova.lm.rpp`).

The `manova.update` to add `$MANOVA` to `lm.rpp` fits requires more computation time than the `$ANOVA` statistics that are computed automatically in `lm.rpp`. Generally, the same inferential conclusions will be found with either approach, when observations outnumber response variables. For high-dimensional data (more variables than observations) data are projected into a Euclidean space of appropriate dimensions (rank of residual covariance matrix). One can vary the tolerance for eigenvalue decay or specify the number of PCs, if a smaller set of PCs than the maximum is desired. This is advised if there is strong correlation among variables (the data space could be simplified to fewer dimensions), as spurious results are possible. Because distributions of MANOVA stats can be generated from the random permutations, there is no need to approximate F-values, like with parametric MANOVA. By restricting analysis to the real, positive eigenvalues calculated, all statistics can be calculated (but Wilks lambda, as a product but not a trace, might be less reliable as variable number approaches the number of observations).

ANOVA vs. MANOVA:

Two SSCP matrices are calculated for each linear model effect, for every random permutation: R (Residuals or Random effects) and H, the difference between SSCPs for "full" and "reduced" models. (Full models contain and reduced models lack the effect tested; SSCPs are hypothesized to be the same under a null hypothesis, if there is no effect. The difference, H, would have a trace of 0 if the null hypothesis were true.) In RRPP, ANOVA and MANOVA correspond to two different ways to calculate statistics from R and H matrices.

ANOVA statistics are those that find the trace of R and H SSCP matrices before calculating subsequent statistics, including sums of squares (SS), mean squares (MS), and F-values. These statistics can be calculated with univariate data and provide univariate-like statistics for multivariate data. These statistics are dispersion measures only (covariances among variables do not contribute) and are the same as "distance-based" stats proposed by Goodall (1991) and Anderson (2001). MANOVA stats require multivariate data and are implicitly affected by variable covariances. For MANOVA, the inverse of R times H (invR.H) is first calculated for each effect, then eigen-analysis is performed on these matrix products. Multivariate statistics are calculated from the positive, real eigenvalues. In general, inferential conclusions will be similar with either approach, but effect sizes might differ.

Two important differences between `manova.update` and `summary.manova` (for `lm` objects) are that `manova.update` does not attempt to normalize residual SSCP matrices (unnecessary for non-parametric statistical solutions) and (2) uses a generalized inverse of the residual SSCP, if needed, when the number of variables could render eigen-analysis problematic. This approach is consistent with covariance regularization methods that attempt to make covariance matrices positive-definite for calculating model likelihoods or multivariate statistics. If the number of observations far exceeds the number of response variables, observed statistics from `manova.update` and `summary.manova` will be quite similar. If the number of response variables approaches or exceeds the number of observations, `manova.update` statistics will be much more reliable.

ANOVA tables are generated by `anova.lm.rrpp` on `lm.rrpp` fits and MANOVA tables are generated by `summary.manova.lm.rrpp`, after running `manova.update` on `lm.rrpp` fits.

Currently, mixed model effects are only possible with `$ANOVA` statistics, not `$MANOVA`.

More detail is found in the vignette, ANOVA versus MANOVA.

Usage

```
manova.update(
  fit,
  error = NULL,
  tol = 1e-07,
  PC.no = NULL,
  print.progress = TRUE,
  verbose = NULL
)
```

Arguments

<code>fit</code>	Linear model fit from <code>lm.rrpp</code>
<code>error</code>	An optional character string to define R matrices used to calculate <code>invR.H</code> . (Currently only Residuals can be used and this argument defaults to <code>NULL</code> . Future versions will update this argument.)

tol	A tolerance value for culling data dimensions to prevent spurious results. The distribution of eigenvalues for the data will be examined and if the decay becomes less than the tolerance, the data will be truncated to principal components ahead of this point. This will possibly prevent spurious results calculated from eigenvalues near 0. If <code>tol = 0</code> , all possible PC axes are used, which is likely not a problem if observations outnumber variables. If <code>tol = 0</code> and the number of variables exceeds the number of observations, the value of <code>tol</code> will be made slightly positive to prevent problems with eigen-analysis.
PC.no	A value that, if not NULL, can override the tolerance argument, and forces a desired number of data PCs to use for analysis. If a value larger than the possible number of PCs is chosen, the full compliment of PCs (the full data space) will be used. If a number larger than <code>tol</code> would permit is chosen, the minimum number of PCs between the <code>tol</code> argument and <code>PC.no</code> argument is returned.
print.progress	A logical value to indicate whether a progress bar should be printed to the screen. This is helpful for long-running analyses.
verbose	Either a NULL or logical value for whether to retain all MANOVA result (if TRUE). If NULL, the verbose argument used for the <code>lm.rppp</code> is retained for MANOVA update. Essentially, <code>verbose</code> indicates whether to retain all SSCP matrices and all <code>invR.H</code> matrices, for every model effect, in every RRPP iteration.

Value

An object of class `lm.rppp` is updated to include class `manova.lm.rppp`, and the object, `$MANOVA`, which includes

SSCP	Terms and Model SSCP matrices.
invR.H	The inverse of the residuals SSCP times the H SSCP.
eigs	The eigenvalues of <code>invR.H</code> .
e.rank	Rank of the error (residuals) covariance matrix. Currently NULL only.
PCA	Principal component analysis of data, using either <code>tol</code> or <code>PC.no</code> .
manova.pc.dims	Resulting number of PC vectors in the analysis.
e.rank	Rank of the residual (error) covariance matrix, irrespective of the number of dimensions used for analysis.

Author(s)

Michael Collyer

References

- Goodall, C.R. 1991. Procrustes methods in the statistical analysis of shape. *Journal of the Royal Statistical Society B* 53:285-339.
- Anderson MJ. 2001. A new method for non-parametric multivariate analysis of variance. *Austral Ecology* 26: 32-46.

Examples

```

## Not run:
# Body Shape Analysis (Multivariate) -----

data(Pupfish)

# Although not recommended as a practice, this example will use only
# three principal components of body shape for demonstration.
# A larger number of random permutations should also be used.

Pupfish$shape <- ordinate(Pupfish$coords)$x[, 1:3]

Pupfish$logSize <- log(Pupfish$CS)

fit <- lm.rpp(shape ~ logSize + Sex, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 499)
summary(fit, formula = FALSE)
anova(fit) # ANOVA table

# MANOVA

fit.m <- manova.update(fit, print.progress = FALSE, tol = 0.001)
summary(fit.m, test = "Roy")
summary(fit.m, test = "Pillai")

fit.m$MANOVA$eigs$obs # observed eigenvalues
fit.m$MANOVA$SSCP$obs # observed SSCP
fit.m$MANOVA$invR.H$obs # observed invR.H

# Distributions of test statistics

summ.roy <- summary(fit.m, test = "Roy")
dens <- apply(summ.roy$rand.stats, 1, density)
par(mfcol = c(1, length(dens)))
for(i in 1:length(dens)) {
  plot(dens[[i]], xlab = "Roy max root", ylab = "Density",
type = "l", main = names(dens)[[i]])
  abline(v = summ.roy$rand.stats[1, i], col = "red")
}
par(mfcol = c(1,1))

## End(Not run)

```

Description

Function performs analyses concerned with the repeatability (reliability) of multivariate data (measurements) collected from the same research subjects. Although there is no requirement for repeated measurements on all research subjects, the analysis assumes that multiple observations are made.

Usage

```
measurement.error(
  data,
  Y,
  subjects,
  replicates,
  groups = NULL,
  iter = 999,
  seed = NULL,
  multivariate = FALSE,
  use.PCs = TRUE,
  tol = 0.001,
  Parallel = FALSE,
  turbo = TRUE,
  print.progress = FALSE,
  verbose = FALSE
)
```

Arguments

data	A required data frame, either of class <code>data.frame</code> or class <code>rrpp.data.frame</code> . This function cannot be used without a data frame. All arguments for data and variables are names that must exist in the data frame.
Y	A name for a matrix (n x p) of data for n observations and p variables that can be found in the data frame. For example, Y = "morphData".
subjects	A name for a vector or factor of research subjects, found within the data frame (each subject should occur twice or more). The length of the vector in the data frame must equal the number of observations and will be coerced into a factor. For example, subjects = "ID".
replicates	A name for a vector or factor for replicate measurements for research subjects, found within the data frame. The length of the vector in the data frame must equal the number of observations and will be coerced into a factor. For example, replicates = "Rep".
groups	An optional name for a vector in the data frame, coercible to factor, to be included in the linear model (as an interaction with replicates). This would be of interest if one were concerned with systematic ME occurring perhaps differently among certain strata within the data. For example, systematic ME because of an observer bias might only be observed with females or males, in which case the argument might be: groups = "Sex".
iter	Number of iterations for significance testing

seed	An optional argument for setting the seed for random permutations of the resampling procedure. If left NULL (the default), the exact same P-values will be found for repeated runs of the analysis (with the same number of iterations). If seed = "random", a random seed will be used, and P-values will vary. One can also specify an integer for specific seed values, which might be of interest for advanced users.
multivariate	Logical value for whether to include multivariate analyses. Intraclass correlation matrices and relative eigenanalysis are based on products of sums of squares and cross-products (SSCP) matrices, some of which must be inverted and potentially require significant computation time. If FALSE, only statistics based on dispersion of values are calculated.
use.PCs	A logical argument for whether to use the principal components of the data. This might be helpful for relative eigenanalysis, and if $p > n$, in which case inverting singular covariance matrices would not be possible.
tol	A value indicating the magnitude below which components should be omitted, if use.PCs is TRUE. (Components are omitted if their standard deviations are less than or equal to tol times the standard deviation of the first component.) See ordinate for more details.
Parallel	The same argument as in lm.rppp to govern parallel processing (either a logical value – TRUE or FALSE – or the number of threaded cores to use). See lm.rppp for additional details.
turbo	Logical value for whether to suppress coefficient estimation in RRPP iteration, thus turbo-charging RRPP.
print.progress	A logical value to indicate whether a progress bar should be printed to the screen.
verbose	A logical value to indicate if all the output from an lm.rppp analysis should be retained. If FALSE, only the needed output for summaries and plotting is retained.

Details

This function performs analyses as described in Collyer and Adams (2024) to assess systematic and random components of measurement error (ME). It basically performs ANOVA with RRPP, but with different restricted randomization strategies. The reliability of research subject variation can be considered by restricting randomization within replicates; the consistency of replicate measures can be considered by restricting randomization within subjects. Inter-subject variation remains constant across all random permutations within subjects and inter-replicate variation remains constant across all random permutations within replicates. Type II sums of squares and cross-products (SSCP) are calculated to assure conditional estimation.

The results include univariate-like statistics based on dispersion of values and eigenanalysis performed on a signal to noise matrix product of SSCP matrices (sensu Bookstein and Mitteroecker, 2014) including the inverse of the random component of ME and the systematic component of ME. The multivariate test is a form of multivariate ANOVA (MANOVA), using RRPP to generate sampling distributions of the major eigenvalue (Roy's maximum root). Likelihood-ratio tests can also be performed using [lr_test](#).

Intraclass correlation coefficients (ICC) can also be calculated (using [ICCstats](#)), both based on dispersion of values and covariance matrices, as descriptive statistics. Details are provided in [ICCstats](#).

Value

Objects of class "measurement.error" return the same objects as a `lm.rpp` fit, plus a list of the following:

AOV	Analysis of variance to test for systematic error, based on dispersion of values.
mAOV	Multivariate AOV based on product of the inverse of the random component (SSCP) of ME times the systematic component of ME.
SSCP	The sums of squares and cross-products matrices for model effects.
SSCP.ME.product	The products of the inverse of the random ME SSCP and the SSCP matrices for systematic ME,. These are the same matrix products used for eigenanalysis. This is the observed matrix.
SSCP.ME.product.std	A list of the symmetric forms of standardized SSCP.ME.products that yield orthogonal eigenvectors.

Author(s)

Michael Collyer

References

Collyer, M.L. and D.C. Adams. 2024. Interrogating Random and Systematic Measurement Error in Morphometric Data. *Evolutionary Biology*, 51, 179–20.

Bookstein, F.L., & Mitteroecker, P. (2014). Comparing covariance matrices by relative eigenanalysis, with applications to organismal biology. *Evolutionary Biology*, 41(2), 336-350.

See Also

[lm.rpp.ws](#), [manova.update](#), [lr_test](#)

Examples

```
## Not run:
# Measurement error analysis on simulated data of fish shapes

data(fishy)

# Example two digitization replicates of the same research subjects
rep1 <- matrix(fishy$coords[1,], 11, 2, byrow = TRUE)
rep2 <- matrix(fishy$coords[61,], 11, 2, byrow = TRUE)
plot(rep1, pch = 16, col = gray(0.5, alpha = 0.5), cex = 2, asp = 1)
points(rep2, pch = 16, col = gray(0.2, alpha = 0.5), cex = 2, asp = 1)

# Analysis unconcerned with groups

ME1 <- measurement.error(
  Y = "coords",
  subjects = "subj",
```

```

    replicates = "reps",
    data = fishy)

anova(ME1)
ICCstats(ME1, subjects = "Subjects", with_in = "Systematic ME")
plot(ME1)

# Analysis concerned with groups

ME2 <- measurement.error(
  Y = "coords",
  subjects = "subj",
  replicates = "reps",
  groups = "groups",
  data = fishy)

anova(ME2)
ICCstats(ME2, subjects = "Subjects",
  with_in = "Systematic ME", groups = "groups")
P <- plot(ME2)
focusMEonSubjects(P, subjects = 18:20, shadow = TRUE)

## End(Not run)

```

model.comparison	<i>Model Comparisons, in terms of the log-likelihood, covariance trace, or Z-score.</i>
------------------	---

Description

Function calculates either log-likelihoods or traces of covariance matrices for comparison with respect to parameter penalties, or calculates Z-scores from RRPP, which can be profiled across a gradient (predictor).

Usage

```

model.comparison(
  ...,
  type = c("cov.trace", "logLik", "Z"),
  predictor = NULL,
  tol = NULL,
  pc.no = NULL,
  gls.null = FALSE
)

```

Arguments

... Any number of `lm.rpp` class objects for model fits to be compared.

type	An argument to choose between log-likelihood, covariance trace, or Z results. If Z is chosen, Z-scores are calculated, the same log-likelihoods are calculated as with the log-likelihood type, but also in every RRPP permutation, as describe for the initial mode fits, with choice of null model (below).
predictor	An optional vector that can be used to profile the results based on type across a range of numerical values described by the predictor. A spline will also be fit, which will reveal estimated values of the predictor that yield maximum and minimum values of model comparison metric.
tol	If type = logLik or Z, tol is a tolerance value between 0 and 1, indicating the magnitude below which components should be omitted (if standard deviations of components are less than the eigenvalue of the first component times the tolerance), for calculating the log-likelihood.
pc.no	If type = logLik or Z, an optional value to indicate the number of principal components (maximum rank) to use for calculating the log-likelihood.
gls.null	A logical value indicating whether GLS estimation should be used with the null (intercept) model, for calculating Z scores via RRPP of log-likelihoods. This should be FALSE if comparing different GLS estimations of covariance matrices. It should be TRUE if comparing different model fits with the same GLS-estimated covariance matrix.

Details

The function calculates either log-likelihoods or traces of (residual) covariance matrices, plus parameter penalties, to assist in comparative model evaluation or selection. Because high-dimensional data often produce singular or ill-conditioned residual covariance matrices, this function does one of two things: 1) uses the trace of a covariance matrix rather than its determinant; or 2) provides a ridge-regularization (Warton, 2008) of the covariance matrix, only if it is determined that it is ill-conditioned. Regardless of implementation, covariance matrices are projected into a principal component (PC) space of appropriate dimensions.

The parameter penalty is based on that proposed by Bedrick and Tsai (1994), equal to $2(pk + p(p + 1)/2)$, where p is the appropriate dimension (not number of variables) of the covariance matrix. The parameter, k , is the rank of the model design matrix.

In the case that "logLik" is chosen for the argument, type, AIC scores are calculated. These scores may not perfectly match other packages or software that calculate AIC for multivariate data, if ridge regularization was used (and if other packages require $p =$ the number of data variables). When choosing logLik as the type of comparison, it might be a good idea to adjust the tolerance or number of data principal components. The default (NULL) values will use all data dimensions to calculate log-likelihoods, which might cause problems if the number of variables exceeds the number of observations (producing singular residual covariance matrices). However, one should not reduce data dimensions haphazardly, as this can lead to poor estimates of log-likelihood. Furthermore, using the tolerance argument could result in different numbers of principal components used for each model to calculate log-likelihoods, which might be a concern for comparing models. If both tol and pc.no arguments are used, the solution will use the fewest PCs produced by either argument. Because the trace of a covariance matrix is not sensitive to matrix singularity, no PC adjustment is used for the cov.trace argument.

This function can also calculate Z-scores from RRPP on model log-likelihoods, which can be compared directly or profiled along a gradient (predictor). This might be useful for for comparing

generalized least-squares (GLS) models, for example, along a gradient of a parameter used to scale the covariance matrix for GLS estimation. See Collyer et al. 2022 for an example of using RRPP on log-likelihoods with different covariance matrices.

Users can construct their own tables from the results but this function does not attempt to summarize results, as interpreting results requires some arbitrary decisions. The `anova` function explicitly tests multiple models and can be used for nested model comparisons.

Results can also be plotted using the generic `plot` function.

Caution: For models with GLS estimation, the number of parameters used to estimate the covariance matrix is not taken into consideration. A generalized information criterion is currently in development.

Value

An object of class `model.comparison` is a data frame with either log-likelihoods or covariance traces, plus parameter penalties. AIC scores might be include, if applicable

Author(s)

Michael Collyer

References

- Bedrick, E.J., and C.L. Tsai. 1994. Model selection for multivariate regression in small samples. *Biometrics*, 226-231.
- Warton, D.I., 2008. Penalized normal likelihood and ridge regularization of correlation and covariance matrices. *Journal of the American Statistical Association*. 103: 340-349.
- Collyer, M.L., E.K. Baken, & D.C. Adams. A standardized effect size for evaluating and comparing the strength of phylogenetic signal. *Methods in Ecology and Evolution*. 13: 367–382.

Examples

```
## Not run:
data(Pupfish)
Pupfish$logSize <- log(Pupfish$CS)
fit1 <- lm.rrpp(coords ~ logSize, data = Pupfish, iter = 0,
print.progress = FALSE)
fit2 <- lm.rrpp(coords ~ Pop, data = Pupfish, iter = 0,
print.progress = FALSE)
fit3 <- lm.rrpp(coords ~ Sex, data = Pupfish, iter = 0,
print.progress = FALSE)
fit4 <- lm.rrpp(coords ~ logSize + Sex, data = Pupfish, iter = 0,
print.progress = FALSE)
fit5 <- lm.rrpp(coords ~ logSize + Pop, data = Pupfish, iter = 0,
print.progress = FALSE)
fit6 <- lm.rrpp(coords ~ logSize + Sex * Pop, data = Pupfish, iter = 0,
print.progress = FALSE)

modComp1 <- model.comparison(fit1, fit2, fit3, fit4, fit5,
fit6, type = "cov.trace")
```

```

modComp2 <- model.comparison(fit1, fit2, fit3, fit4, fit5,
fit6, type = "logLik", tol = 0.01)

summary(modComp1)
summary(modComp2)

par(mfcol = c(1,2))
plot(modComp1)
plot(modComp2)

# Comparing fits with covariance matrices
# an example for scaling a phylogenetic covariance matrix with
# the scaling parameter, lambda

data("PlethMorph")
Cov <- PlethMorph$PhyCov
lambda <- seq(0, 1, 0.1)

Cov1 <- scaleCov(Cov, scale. = lambda[1])
Cov2 <- scaleCov(Cov, scale. = lambda[2])
Cov3 <- scaleCov(Cov, scale. = lambda[3])
Cov4 <- scaleCov(Cov, scale. = lambda[4])
Cov5 <- scaleCov(Cov, scale. = lambda[5])
Cov6 <- scaleCov(Cov, scale. = lambda[6])
Cov7 <- scaleCov(Cov, scale. = lambda[7])
Cov8 <- scaleCov(Cov, scale. = lambda[8])
Cov9 <- scaleCov(Cov, scale. = lambda[9])
Cov10 <- scaleCov(Cov, scale. = lambda[10])
Cov11 <- scaleCov(Cov, scale. = lambda[11])

fit1 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov1)
fit2 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov2)
fit3 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov3)
fit4 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov4)
fit5 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov5)
fit6 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov6)
fit7 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov7)
fit8 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov8)
fit9 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov9)
fit10 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov10)
fit11 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov11)

par(mfrow = c(1,1))

MC1 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
fit7, fit8, fit9, fit10, fit11,
type = "logLik")
MC1
plot(MC1)

MC2 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
fit7, fit8, fit9, fit10, fit11,

```

```
type = "logLik", predictor = lambda)
MC2
plot(MC2)

MC3 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
fit7, fit8, fit9, fit10, fit11,
type = "Z", predictor = lambda)
MC3
plot(MC3)

## End(Not run)
```

model.frame.lm.rppp *Extract model frame from a lm.rppp object*

Description

model.frame.lm.rppp returns the model frame constructed for an lm.rppp object.

Usage

```
## S3 method for class 'lm.rppp'
model.frame(formula, ...)
```

Arguments

formula	Object from lm.rppp
...	further arguments passed to or from other methods

Author(s)

Michael Collyer

model.matrix.lm.rppp *Extract the model design matrix from an lm.rppp object*

Description

model.matrix.lm.rppp returns the design matrix constructed for an lm.rppp object.

Usage

```
## S3 method for class 'lm.rppp'
model.matrix(object, ...)
```

Arguments

object Object from [lm.rppp](#)
 ... further arguments passed to or from other methods

Author(s)

Michael Collyer

motionpaths *Simulated motion paths*

Description

Simulated motion paths

Author(s)

Dean Adams

References

Adams, D. C., and M. L. Collyer. 2009. A general framework for the analysis of phenotypic trajectories in evolutionary studies. *Evolution* 63:1143-1154.

na.omit.rppp.data.frame
Handle missing values in rppp.data.frame objects

Description

Handle missing values in rppp.data.frame objects

Usage

```
## S3 method for class 'rppp.data.frame'
na.omit(object, ...)
```

Arguments

object object (from [rppp.data.frame](#))
 ... further arguments (currently not used)

Author(s)

Michael Collyer

Examples

```

y <- matrix(rnorm(15), 5, 3)
x <- rnorm(5)
rdf <- rpp.data.frame(x = x, y = y, d = dist(y))
rdf$x[1] <- NA # create missing data
rdf

ndf <- na.omit(rdf)
ndf

```

ordinate

Ordination tool for data aligned to another matrix

Description

Function performs a singular value decomposition of ordinary least squares (OLS) or generalized least squares (GLS) residuals, aligned to an alternative matrix, plus projection of data onto vectors obtained.

Usage

```

ordinate(
  Y,
  A = NULL,
  Cov = NULL,
  transform. = TRUE,
  scale. = FALSE,
  tol = NULL,
  rank. = NULL,
  newdata = NULL
)

```

Arguments

Y	An n x p data matrix.
A	An optional n x n symmetric matrix or an n x k data matrix, where k is the number of variables that could be associated with the p variables of Y. If NULL, an n x n identity matrix will be used.
Cov	An optional n x n covariance matrix to describe the non-independence among observations in Y, and provide a GLS-centering of data. Note that Cov and A can be the same, if one wishes to align GLS residuals to the same matrix used to obtain them. Note also that no explicit GLS-centering is performed on A. If this is desired, A should be GLS-centered beforehand.
transform.	An optional argument if a covariance matrix is provided to transform GLS-centered residuals, if TRUE. If FALSE, only GLS-centering is performed. Only if transform = TRUE (the default) can one expect the variances of ordinate scores in a principal component analysis to match eigenvalues.

scale.	a logical value indicating whether the variables should be scaled to have unit variance before the analysis takes place. The default is FALSE.
tol	A value indicating the magnitude below which components should be omitted. (Components are omitted if their standard deviations are less than or equal to tol times the standard deviation of the first component.) With the default null setting, no components are omitted (unless rank. is provided). Other settings for tol could be <code>tol = sqrt(.Machine\$double.eps)</code> , which would omit essentially constant components, or <code>tol = 0</code> , to retain all components, even if redundant. This argument is exactly the same as in prcomp
rank.	Optionally, a number specifying the maximal rank, i.e., maximal number of aligned components to be used. This argument can be set as alternative or in addition to tol, useful notably when the desired rank is considerably smaller than the dimensions of the matrix. This argument is exactly the same as in prcomp
newdata	An optional data frame of values for the same variables of Y to be projected onto aligned components. This is only possible with OLS (<code>transform. = FALSE</code>).

Details

The function performs a singular value decomposition, $\mathbf{t}(\mathbf{A})\mathbf{Z} = \mathbf{U}\mathbf{D}\mathbf{t}(\mathbf{V})$, where \mathbf{Z} is a matrix of residuals (obtained from \mathbf{Y} ; see below) and \mathbf{A} is an alignment matrix with the same number of rows as \mathbf{Z} . (\mathbf{t} indicates matrix transposition.) \mathbf{U} and \mathbf{V} are the matrices of left and right singular vectors, and \mathbf{D} is a diagonal matrix of singular values. \mathbf{V} are the vectors that describe maximized covariation between \mathbf{Y} and \mathbf{A} . If $\mathbf{A} = \mathbf{I}$, an $n \times n$ identity matrix, \mathbf{V} are the eigen vectors (principal components) of \mathbf{Y} .

\mathbf{Z} represents a centered and potentially standardized form of \mathbf{Y} . This function can center data via OLS or GLS means (the latter if a covariance matrix to describe the non-independence among observations is provided). If standardizing variables is preferred, then \mathbf{Z} both centers and scales the vectors of \mathbf{Y} by their standard deviations.

Data are projected onto aligned vectors, \mathbf{ZV} . If a GLS computation is made, the option to transform centered values (residuals) before projection is available. This is required for orthogonal projection, but from a transformed data space. Not transforming residuals maintains the Euclidean distances among observations and the OLS multivariate variance, but the projection is oblique (scores can be correlated).

The versatility of using an alignment approach is that alternative data space rotations are possible. Principal components are thus the vectors that maximize variance with respect to the data, themselves, but "components" of (co)variation can be described for any inter-matrix relationship, including phylogenetic signal, ecological signal, ontogenetic signal, size allometry, etc. More details are provided in Collyer and Adams (2021).

Much of this function is consistent with the [prcomp](#) function, except that centering data is not an option (it is required).

SUMMARY STATISTICS: For principal component plots, the traditional statistics to summarize the analysis include eigenvalues (variance by component), proportion of variance by component, and cumulative proportion of variance. When data are aligned to an alternative matrix, the statistics are less straightforward. A summary of of such an analysis (performed with [summary.ordinate](#)) will produce these additional statistics:

Singular Value Rather than eigenvalues, the singular values from singular value decomposition of the cross-product of the scaled alignment matrix and the data.

Proportion of Covariance Each component's singular value divided by the sum of singular values. The cumulative proportion is also returned. Note that these values do not explain the amount of covariance between the alignment matrix and data, but explain the distribution of the covariance. Large proportions can be misleading.

RV by Component The partial RV statistic by component. Cumulative values are also returned. The sum of partial RVs is Escoffier's RV statistic, which measures the amount of covariation between the alignment matrix and data. Caution should be used in interpreting these values, which can vary with the number of observations and number of variables. However, the RV is more reliable than proportion of singular value for interpretation of the strength of linear association for aligned components. (It is most analogous to proportion of variance for principal components.)

Value

An object of class `ordinate` is a list containing the following

<code>x</code>	Aligned component scores for all observations
<code>xn</code>	Optional projection of new data onto components.
<code>d</code>	The portion of the squared singular values attributed to the aligned components.
<code>sdev</code>	Standard deviations of <code>d</code> ; i.e., the scale of the components.
<code>rot</code>	The matrix of variable loadings, i.e. the singular vectors, V .
<code>center</code>	The OLS or GLS means vector used for centering.
<code>transform</code>	Whether GLS transformation was used in projection of residuals (only possible in conjunction with GLS-centering).
<code>scale</code>	The scaling used, or <code>FALSE</code> .
<code>alignment</code>	Whether data were aligned to principal axes or the name of another matrix.
<code>GLS</code>	A logical value to indicate if GLS-centering and projection was used.

Author(s)

Michael Collyer

References

Collyer, M.L. and D.C. Adams. 2021. Phylogenetically-aligned Component Analysis. *Methods in Ecology and evolution*. In press.

Revell, L. J. 2009. Size-correction and principal components for interspecific comparative studies. *Evolution*, 63:3258-3268.

See Also

[plot.ordinate](#), [prcomp](#), [plot.default](#), `gm.prcomp` within `geomorph`

Examples

```

# Examples use residuals from a regression of salamander
# morphological traits against body size (snout to vent length, SVL).
# Observations are species means and a phylogenetic covariance matrix
# describes the relatedness among observations.

data("PlethMorph")
Y <- as.data.frame(PlethMorph[c("TailLength", "HeadLength",
"Snout.ey", "BodyWidth",
"Forelimb", "Hindlimb")])
Y <- as.matrix(Y)
R <- lm.rpp(Y ~ SVL, data = PlethMorph,
iter = 0, print.progress = FALSE)$LM$residuals

# PCA (on correlation matrix)

PCA.ols <- ordinate(R, scale. = TRUE)
PCA.ols$rot
prcomp(R, scale. = TRUE)$rotation # should be the same

# phyPCA (sensu Revell, 2009)
# with projection of untransformed residuals (Collyer & Adams 2020)

PCA.gls <- ordinate(R, scale. = TRUE,
transform. = FALSE,
Cov = PlethMorph$PhyCov)

# phyPCA with transformed residuals (orthogonal projection,
# Collyer & Adams 2020)

PCA.t.gls <- ordinate(R, scale. = TRUE,
transform. = TRUE,
Cov = PlethMorph$PhyCov)

# Align to phylogenetic signal (in each case)

PaCA.ols <- ordinate(R, A = PlethMorph$PhyCov, scale. = TRUE)

PaCA.gls <- ordinate(R, A = PlethMorph$PhyCov,
scale. = TRUE,
transform. = FALSE,
Cov = PlethMorph$PhyCov)

PaCA.t.gls <- ordinate(R, A = PlethMorph$PhyCov,
scale. = TRUE,
transform. = TRUE,
Cov = PlethMorph$PhyCov)

# Summaries

summary(PCA.ols)
summary(PCA.gls)

```



```

summary(PCA.t.gls)
summary(PaCA.ols)
summary(PaCA.gls)
summary(PaCA.t.gls)

# Plots

par(mfrow = c(2,3))
plot(PCA.ols, main = "PCA OLS")
plot(PCA.gls, main = "PCA GLS")
plot(PCA.t.gls, main = "PCA t-GLS")
plot(PaCA.ols, main = "PaCA OLS")
plot(PaCA.gls, main = "PaCA GLS")
plot(PaCA.t.gls, main = "PaCA t-GLS")
par(mfrow = c(1,1))

# Changing some plot aesthetics (the arguments in plot.ordinate and
# plot.default are important for changing plot parameters)

P1 <- plot(PaCA.gls, main = "PaCA GLS", include.axes = TRUE)

P2 <- plot(PaCA.gls, main = "PaCA GLS", include.axes = TRUE,
col = 4, pch = 21, bg = PlethMorph$group)
add.tree(P2, PlethMorph$tree, edge.col = 4)

P3 <- plot(PaCA.gls, main = "PaCA GLS", include.axes = TRUE,
col = 4, pch = 21, bg = PlethMorph$group,
flip = 1)
add.tree(P3, PlethMorph$tree, edge.col = 4)

```

pairwise

Pairwise comparisons of lm.rpp fits

Description

Function generates distributions of pairwise statistics for a `lm.rpp` fit and returns important statistics for hypothesis tests.

Usage

```

pairwise(
  fit,
  fit.null = NULL,
  groups,
  covariate = NULL,
  verbose = FALSE,
  print.progress = FALSE
)

```

Arguments

<code>fit</code>	A linear model fit using <code>lm.rpp</code> .
<code>fit.null</code>	An alternative linear model fit to use as a null model for RRPP, if the null model of the fit is not desired. Note, for FRPP this argument should remain NULL and FRPP must be established in the <code>lm.rpp</code> fit (<code>RRPP = FALSE</code>). If the null model is uncertain, using <code>reveal.model.designs</code> will help elucidate the inherent null model used.
<code>groups</code>	A factor or vector that is coercible into a factor, describing the levels of the groups for which to find LS means or slopes. Normally this factor would be part of the model fit, but it is not necessary for that to be the case in order to obtain results.
<code>covariate</code>	A numeric vector for which to calculate slopes for comparison. If NULL, LS means will be calculated instead of slopes. Normally this variable would be part of the model fit, but it is not necessary for that to be the case in order to obtain results.
<code>verbose</code>	A logical value for whether to include extra results, specifically the Mahalanobis distances among means, which requires the calculation of residual covariance matrices for each permutation. This should be generally FALSE, unless Mahalanobis distances are desired, in which case it must be TRUE. Verbose computations can require much additional time.
<code>print.progress</code>	If a null model fit is provided, a logical value to indicate whether analytical results progress should be printed on screen. Unless large data sets are analyzed, this argument is probably not helpful.

Details

Based on an `lm.rpp` fit, this function will find fitted values over all permutations and based on a grouping factor, calculate either least squares (LS) means or slopes, and pairwise statistics among them. Pairwise statistics have multiple flavors, related to vector attributes:

Distance between vectors, "dist" Vectors for LS means or slopes originate at the origin and point to some location, having both a magnitude and direction. A distance between two vectors is the inner-product of the vector difference, i.e., the distance between their endpoints. For LS means, this distance is the difference between means. For multivariate slope vectors, this is the difference in location between estimated change for the dependent variables, per one-unit change of the covariate considered. For univariate slopes, this is the absolute difference between slopes.

Standardized distance between vectors, "stdist" Same as the distance between vectors, but distances are divided by the model standard error (square-root of the trace of the residual covariance matrix, adjusted by sample size). Pairwise tests with this statistic should be consistent with ANOVA results.

Mahalanobis distance between vectors, "mdist" Similar to the standardized distance between vectors but the inverse of the residual covariance matrix is used in calculation of the distance, rather than dividing the Euclidean distance between means and dividing by the standard error. If the residual covariance matrix is singular, Mahalanobis distances will not be calculated. Pairwise tests with this statistic should be consistent with MANOVA results.

Vector correlation, "VC" If LS mean or slope vectors are scaled to unit size, the vector correlation is the inner-product of the scaled vectors. The arccosine (acos) of this value is the angle between vectors, which can be expressed in radians or degrees. Vector correlation indicates the similarity of vector orientation, independent of vector length.

Difference in vector lengths, "DL" If the length of a vector is an important attribute – e.g., the amount of multivariate change per one-unit change in a covariate – then the absolute value of the difference in vector lengths is a practical statistic to compare vector lengths. Let d_1 and d_2 be the distances (length) of vectors. Then $|d_1 - d_2|$ is a statistic that compares their lengths. For slope vectors, this is a comparison of rates.

Variance, "var" Vectors of residuals from a linear model indicate can express the distances of observed values from fitted values. Mean squared distances of values (variance), by group, can be used to measure the amount of dispersion around estimated values for groups. Absolute differences between variances are used as test statistics to compare mean dispersion of values among groups. Variance degrees of freedom equal n , the group size, rather than $n-1$, as the purpose is to compare mean dispersion in the sample. (Additionally, tests with one subject in a group are possible, or at least not a hindrance to the analysis.)

The `summary.pairwise` function is used to select a test statistic for the statistics described above, as "dist", "VC", "DL", and "var", respectively. If vector correlation is tested, the `angle` type argument can be used to choose between radians and degrees.

The null model is defined via `lm.rrpp`, but one can also use an alternative null model as an optional argument. In this case, residual randomization in the permutation procedure (RRPP) will be performed using the alternative null model to generate fitted values. If full randomization of values (FRPP) is preferred, it must be established in the `lm.rrpp` fit and an alternative model should not be chosen. If one is unsure about the inherent null model used if an alternative is not specified as an argument, the function `reveal.model.designs` can be used.

Observed statistics, effect sizes, P-values, and one-tailed confidence limits based on the confidence requested will be summarized with the `summary.pairwise` function. Confidence limits are inherently one-tailed as the statistics are similar to absolute values. For example, a distance is analogous to an absolute difference. Therefore, the one-tailed confidence limits are more akin to two-tailed hypothesis tests. (A comparable example is to use the absolute value of a t-statistic, in which case the distribution has a lower bound of 0.)

Notes for RRPP 0.6.2 and subsequent versions:

In previous versions of `pairwise`, `summary.pairwise` had three test types: "dist", "VC", and "var". When one chose "dist", for LS mean vectors, the statistic was the inner-product of the vector difference. For slope vectors, "dist" returned the absolute value of the difference between vector lengths, which is "DL" in 0.6.2 and subsequent versions. This update uses the same calculation, irrespective of vector types. Generally, "DL" is the same as a contrast in rates for slope vectors, but might not have much meaning for LS means. Likewise, "dist" is the distance between vector endpoints, which might make more sense for LS means than slope vectors. Nevertheless, the user has more control over these decisions with version 0.6.2 and subsequent versions.

Notes for RRPP 2.0.4 and subsequent versions:

The test types, standardized distance between vectors, "stdist", and Mahalanobis distances between vectors were added. The former simply divides the distance between vectors by model standard error (square-root of the trace of the residual covariance matrix, adjusted by sample size). This is a multivariate generalization of a t-statistic for the difference between means. It

is not the same as Hotelling squared-T-statistic, which requires incorporating the inverse of the residual covariance matrix in the calculation of the distance, a calculation that also requires a non-singular covariance matrix. However, the Mahalanobis distances are similar (and proportional) to the Hotelling squared-T-statistic. Pairwise tests using Mahalanobis distances represent a non-parametric analog to the parametric Hotelling squared-T test. Both tests should be better for GLS model fits compared to Euclidean distances between means, as the total sums of squares are more likely to vary across random permutations. In general, if ANOVA is performed a pairwise test with "stdist" is a good association; if MANOVA is performed, a pairwise test with "mdist" is a good association.

Value

An object of class `pairwise` is a list containing the following

<code>LS.means</code>	LS means for groups, across permutations.
<code>slopes</code>	Slopes for groups, across permutations.
<code>means.dist</code>	Pairwise distances between means, across permutations.
<code>std.means.dist</code>	Pairwise distances between means, across permutations, standardized.
<code>mah.means.dist</code>	Pairwise Mahalanobis distances between means, across permutations.
<code>means.vec.cor</code>	Pairwise vector correlations between means, across permutations.
<code>means.lengths</code>	LS means vector lengths, by group, across permutations.
<code>means.diff.length</code>	Pairwise absolute differences between mean vector lengths, across permutations.
<code>slopes.dist</code>	Pairwise distances between slopes (end-points), across permutations.
<code>slopes.vec.cor</code>	Pairwise vector correlations between slope vectors, across permutations.
<code>slopes.lengths</code>	Slope vector lengths, by group, across permutations.
<code>slopes.diff.length</code>	Pairwise absolute differences between slope vector lengths, across permutations.
<code>n</code>	Sample size
<code>p</code>	Data dimensions; i.e., variable number
<code>PermInfo</code>	Information for random permutations, passed on from <code>lm.rpp</code> fit and possibly modified if an alternative null model was used.

Author(s)

Michael Collyer

References

- Collyer, M.L., D.J. Sekora, and D.C. Adams. 2015. A method for analysis of phenotypic change for phenotypes described by high-dimensional data. *Heredity*. 115:357-365.
- Adams, D.C and M.L. Collyer. 2018. Multivariate phylogenetic ANOVA: group-clade aggregation, biological challenges, and a refined permutation procedure. *Evolution*. In press.

See Also[lm.rrpp](#)**Examples**

```
## Not run:
# Examples use geometric morphometric data on pupfishes
# See the package, geomorph, for details about obtaining such data

# Body Shape Analysis (Multivariate) -----

data("Pupfish")

# Note:

dim(Pupfish$coords) # highly multivariate!

Pupfish$logSize <- log(Pupfish$CS)

# Note: one should use all dimensions of the data but with this
# example, there are many. Thus, only three principal components
# will be used for demonstration purposes.

Pupfish$Y <- ordinate(Pupfish$coords)$x[, 1:3]

## Pairwise comparisons among LS means

# Note: one should increase RRPP iterations but a
# smaller number is used here for demonstration
# efficiency. Generally, iter = 999 will take less
# than 1s for these examples with a modern computer.

fit1 <- lm.rrpp(Y ~ logSize + Sex * Pop, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 199)
summary(fit1, formula = FALSE)
anova(fit1)

pup.group <- interaction(Pupfish$Sex, Pupfish$Pop)
pup.group
PW1 <- pairwise(fit1, groups = pup.group)
PW1

# distances among means
summary(PW1, confidence = 0.95, test.type = "dist")
summary(PW1, confidence = 0.95, test.type = "dist", stat.table = FALSE)

# standardized distances among means
summary(PW1, confidence = 0.95, test.type = "stdist")

# Mahalanobis (generalized) distances among means
summary(PW1, confidence = 0.95, test.type = "mdist")
```

```

# absolute difference between mean vector lengths
summary(PW1, confidence = 0.95, test.type = "DL")

# correlation between mean vectors (angles in degrees)
summary(PW1, confidence = 0.95, test.type = "VC",
  angle.type = "deg")

# Can also compare the dispersion around means
summary(PW1, confidence = 0.95, test.type = "var")

## Pairwise comparisons of slopes

fit2 <- lm.rppp(Y ~ logSize * Sex * Pop, SS.type = "I",
  data = Pupfish, print.progress = FALSE, iter = 199)
summary(fit2, formula = FALSE)
anova(fit1, fit2)

# Using a null fit that excludes all factor-covariate
# interactions, not just the last one

PW2 <- pairwise(fit2, fit.null = fit1, groups = pup.group,
  covariate = Pupfish$logSize, print.progress = FALSE)
PW2

# distances between slope vectors (end-points)
summary(PW2, confidence = 0.95, test.type = "dist")
summary(PW2, confidence = 0.95, test.type = "dist", stat.table = FALSE)

# absolute difference between slope vector lengths
summary(PW2, confidence = 0.95, test.type = "DL")

# correlation between slope vectors (and angles)
summary(PW2, confidence = 0.95, test.type = "VC",
  angle.type = "deg")

# Can also compare the dispersion around group slopes
summary(PW2, confidence = 0.95, test.type = "var")

## End(Not run)

```

Description

Data for 37 species of plethodontid salamanders. Variables include snout to vent length (SVL) as species size, tail length, head length, snout to eye length, body width, forelimb length, and hind limb length, all measured in mm. A grouping variable is also included for functional guild size. A variable for species names is also included. The data set also includes a phylogenetic

covariance matrix based on a Brownian model of evolution, to assist in generalized least squares (GLS) estimation.

Details

The covariance matrix was estimated with the `vcv.phylo` function of the R package, `ape`, based on the tree described in Adams and Collyer (2018).

Author(s)

Michael Collyer and Dean Adams

References

Adams, D.C and Collyer, M.L. 2018. Multivariate phylogenetic anova: group-clade aggregation, biological challenges, and a refined permutation procedure. *Evolution*, 72: 1204-1215.

plot.interSubVar *Plot Function for RRPP*

Description

This function produces a heat map for inter-subject variability, based on results from a `measurement.error` object. The function, `interSubVar`, must first be used on the `measurement.error` object to obtain variability statistics. This function use the `image` function to produce plots. It does little to manipulate such plots, but any argument for `image` can be manipulated here, as well as the graphical parameters that can be adjusted within `image`.

Usage

```
## S3 method for class 'interSubVar'  
plot(x, ...)
```

Arguments

`x` Object from `interSubVar`
`...` Arguments passed onto `image` and `plot`.

Author(s)

Michael Collyer

plot.lm.rppp

*Plot Function for RRPP***Description**

Plot Function for RRPP

Usage

```
## S3 method for class 'lm.rppp'
plot(
  x,
  type = c("diagnostics", "regression", "PC"),
  resid.type = c("p", "n"),
  fitted.type = c("o", "t"),
  predictor = NULL,
  reg.type = c("PredLine", "RegScore"),
  ...
)
```

Arguments

x	plot object (from lm.rppp)
type	Indicates which type of plot, choosing among diagnostics, regression, or principal component plots. Diagnostic plots are similar to lm diagnostic plots, but for multivariate data. Regression plots plot multivariate dispersion in some fashion against predictor values. PC plots project data onto the eigenvectors of the covariance matrix for fitted values.
resid.type	If type = "diagnostics", an optional argument for whether Pearson ("p") or normalized ("n") residuals should be used. These residuals are the same for ordinary least-squares (OLS) estimation but differ for generalized least-squares (GLS) estimation. For the latter, normalizing residuals requires multiplying them by the transformation matrix obtained for GLS estimation.
fitted.type	As with resid.type, whether fitted values use observed ("o") or transformed ("t") values.
predictor	An optional vector if "regression" plot type is chosen, and is a variable likely used in lm.rppp . This vector is a vector of covariate values equal to the number of observations.
reg.type	If "regression" is chosen for plot type, this argument indicates whether prediction line (PredLine) or regression score (RegScore) plotting is performed. For explanation of prediction line, see Adams and Nistri (2010). For explanation of regression score, see Drake and Klingenberg (2008).
...	other arguments passed to plot (helpful to employ different colors or symbols for different groups). See plot.default and par

Author(s)

Michael Collyer

References

Drake, A. G., and C. P. Klingenberg. 2008. The pace of morphological change: Historical transformation of skull shape in St Bernard dogs. *Proc. R. Soc. B.* 275:71-76.

Adams, D. C., and A. Nistri. 2010. Ontogenetic convergence and evolution of foot morphology in European cave salamanders (Family: Plethodontidae). *BMC Evol. Biol.* 10:1-10.

Examples

```
## Not run:
# Univariate example
data(PlethMorph)
fitGLS <- lm.rrpp(TailLength ~ SVL, data = PlethMorph, Cov = PlethMorph$PhyCov,
  print.progress = FALSE, iter = 0)

par(mfrow = c(2, 2))
plot(fitGLS)
plot(fitGLS, resid.type = "n") # use normalized (transformed) residuals
plot(fitGLS, resid.type = "n", fitted.type = "t") # use also transformed fitted values

# Multivariate example

Y <- as.matrix(cbind(PlethMorph$TailLength,
  PlethMorph$HeadLength,
  PlethMorph$Snout.eye,
  PlethMorph$BodyWidth,
  PlethMorph$Forelimb,
  PlethMorph$Hindlimb))
PlethMorph$Y <- Y
fitGLSm <- lm.rrpp(Y ~ SVL, data = PlethMorph,
  Cov = PlethMorph$PhyCov,
  print.progress = FALSE, iter = 0)

par(mfrow = c(2, 2))
plot(fitGLSm)
plot(fitGLSm, resid.type = "n") # use normalized (transformed) residuals
plot(fitGLSm, resid.type = "n", fitted.type = "t") # use also transformed fitted values
par(mfrow = c(1, 1))

## End(Not run)
```

plot.looCV

Plot Function for RRPP

Description

Plot Function for RRPP

Usage

```
## S3 method for class 'looCV'
plot(x, axis1 = 1, axis2 = 2, flip = NULL, ...)
```

Arguments

x	An object of class <code>looCV</code>
axis1	A value indicating which component should be displayed as the X-axis (default = C1)
axis2	A value indicating which component should be displayed as the Y-axis (default = C2)
flip	An argument that if not NULL can be used to flip components in the plot. The values need to match axis1 or axis2. For example, if axis1 = 3 and axis2 = 4, flip = 1 will not change either axis; flip = 3 will flip only the horizontal axis; flip = c(3, 4) will flip both axes. Axis will only be flipped in first plot.
...	other arguments passed to plot (helpful to employ different colors or symbols for different groups). See

Author(s)

Michael Collyer

plot.measurement.error

Plot Function for RRPP

Description

This function produces multivariate signal-to-noise ratio plots for `measurement.error` objects. See the function, `plot.interSubVar` for plotting the inter-subject variability from a `measurement.error` object, after applying the function, `interSubVar`.

Usage

```
## S3 method for class 'measurement.error'
plot(
  x,
  separate.by.groups = TRUE,
  add.connectors = TRUE,
  add.labels = FALSE,
  use.std.vectors = FALSE,
  titles = NULL,
  add.legend = TRUE,
  ...
)
```

Arguments

x	Object from measurement.error
separate.by.groups	A logical value for whether to make separate plots for each group, if different groups are available. If FALSE, groups are still represented by different symbols in the plot, unless overridden by plot arguments.
add.connectors	A logical value for whether to add connectors, like vectors, between replicate observations of the same subjects.
add.labels	A logical value for whether to label subjects. Labels are either subject name (if available) or number of occurrence in the data set.
use.std.vectors	A logical value for whether to use vectors obtained from a standardized matrix, which are orthogonal. This is not strictly necessary.
titles	An optional vector or list for augmenting the titles of plots produced. The length of the vector or list should match the number of plots produced by other arguments.
add.legend	A logical value for whether to add a legend to plots. If separate.by.groups is TRUE, adding a legend to plots will be slightly redundant. If certain parameters are augmented by user (point characters, colors), add.legend will be made to be FALSE to prevent misinterpretation of intended plotting scheme.
...	Other arguments passed onto plot

Author(s)

Michael Collyer

plot.model.comparison *Plot Function for RRPP*

Description

Plot Function for RRPP

Usage

```
## S3 method for class 'model.comparison'
plot(x, ...)
```

Arguments

x	plot object (from model.comparison)
...	other arguments passed to plot (helpful to employ different colors or symbols for different groups). See plot.default and par

Author(s)

Michael Collyer

plot.ordinate

Plot Function for RRPP

Description

Plot Function for RRPP

Usage

```
## S3 method for class 'ordinate'
plot(x, axis1 = 1, axis2 = 2, flip = NULL, include.axes = TRUE, ...)
```

Arguments

x	An object of class <code>ordinate</code>
axis1	A value indicating which component should be displayed as the X-axis (default = C1)
axis2	A value indicating which component should be displayed as the Y-axis (default = C2)
flip	An argument that if not NULL can be used to flip components in the plot. The values need to match axis1 or axis2. For example, if axis1 = 3 and axis2 = 4, flip = 1 will not change either axis; flip = 3 will flip only the horizontal axis; flip = c(3, 4) will flip both axes.
include.axes	A logical argument for whether axes should be shown at x = 0 and y = 0. This is different than the axes argument in the generic <code>plot.default</code> function, which controls the edges of the plot (providing a box effect or not). Using include.axes = TRUE does not allow aesthetic control of the axes. If desired, it is better to use include.axes = FALSE and augment the plot object with <code>abline</code> (choosing h = 0 and v = 0 in separate applications).
...	other arguments passed to plot (helpful to employ different colors or symbols for different groups). See

Value

An object of class "plot.ordinate" is a list with components that can be used in other plot functions, such as the type of plot, points, a group factor, and other information depending on the plot parameters used.

Author(s)

Michael Collyer

plot.predict.lm.rpp *Plot Function for RRPP*

Description

Plot Function for RRPP

Usage

```
## S3 method for class 'predict.lm.rpp'  
plot(x, PC = FALSE, ellipse = FALSE, abscissa = NULL, label = TRUE, ...)
```

Arguments

x	plot object (from predict.lm.rpp)
PC	A logical argument for whether the data space should be rotated to its principal components
ellipse	A logical argument to change error bars to ellipses in multivariate plots. It has no function for univariate plots or is abscissa is not NULL.
abscissa	An optional vector (numeric or factor) equal in length to predictions to use for plotting as the abscissa (x-axis), in which case predictions are the ordinate (y-axis). This might be helpful if predictions are made for a continuous independent variable. The abscissa would be the same variable used to make predictions (and can be the data.frame used for newdata in predict.lm.rpp).
label	A logical argument for whether points should be labeled (in multivariate plots).
...	other arguments passed to plot, arrows, points, or text (helpful to employ different colors or symbols for different groups). See plot.default , arrows , points , par , and text

Author(s)

Michael Collyer

Examples

```
# See lm.rpp help file for examples.
```

`plot.trajectory.analysis`*Plot Function for RRPP*

Description

Function generates a principal component plot for trajectories

Usage

```
## S3 method for class 'trajectory.analysis'  
plot(x, ...)
```

Arguments

<code>x</code>	plot object (from trajectory.analysis)
<code>...</code>	other arguments passed to <code>plot</code> (helpful to employ different colors or symbols for different groups). See plot.default and par

Details

The function calculates and plots principal components of fitted values from [lm.rpp](#) that are passed onto [trajectory.analysis](#), and projects data onto them. This function is a set.up, and [add.trajectories](#) is needed to add trajectories to the plot. By having two stages of control, the plotting functions are more flexible. This function also returns plotting information that can be valuable for making individualized plots, if [add.trajectories](#) is not preferred.

Value

If an object is assigned, it will return:

<code>pca</code>	Principal component analysis performed using prcomp .
<code>pc.points</code>	Principal component scores for all data.
<code>trajectory.analysis</code>	Trajectory analysis passed on.
<code>trajectories</code>	<code>pca</code> Observed trajectories projected onto principal components.

Author(s)

Michael Collyer

References

- Adams, D. C., and M. M. Cerney. 2007. Quantifying biomechanical motion using Procrustes motion analysis. *J. Biomech.* 40:437-444.
- Adams, D. C., and M. L. Collyer. 2007. The analysis of character divergence along environmental gradients and other covariates. *Evolution* 61:510-515.
- Adams, D. C., and M. L. Collyer. 2009. A general framework for the analysis of phenotypic trajectories in evolutionary studies. *Evolution* 63:1143-1154.
- Collyer, M. L., and D. C. Adams. 2007. Analysis of two-state multivariate phenotypic change in ecological studies. *Ecology* 88:683-692.
- Collyer, M. L., and D. C. Adams. 2013. Phenotypic trajectory analysis: comparison of shape change patterns in evolution and ecology. *Hystrix* 24: 75-83.
- Collyer, M.L., D.J. Sekora, and D.C. Adams. 2015. A method for analysis of phenotypic change for phenotypes described by high-dimensional data. *Heredity*. 115:357-365.

See Also

[plot.default](#) and [par](#)

Examples

```
# See trajectory.analysis help file for examples
```

predict.lm.rppp	<i>predict for lm.rppp model fits</i>
-----------------	---------------------------------------

Description

Computes predicted values from an [lm.rppp](#) model fit, using bootstrapped residuals to generate confidence intervals. (Residuals are the residuals of the [lm.rppp](#) fit, not its null model. The bootstrap procedure resamples residual vectors with replacement.) The bootstrap permutations use the same number of iterations and seed as used in the [lm.rppp](#) model fit. A [predict.lm.rppp](#) object can be plotted using various options. See [plot.predict.lm.rppp](#).

Note that if data offsets are used (if the `offset` argument is used when fitting a [lm.rppp](#) model), they are ignored for estimating coefficients over iterations. Offsets are subtracted from data in [lm](#) and added to predicted values in [predict.lm](#), effectively adjusting the intercept and then un-adjusting it for predictions. This causes problems if the newdata have a different number of observations than the original model fit.

Usage

```
## S3 method for class 'lm.rppp'
predict(object, newdata = NULL, block = NULL, confidence = 0.95, ...)
```

Arguments

object	Object from <code>lm.rpp</code> .
newdata	Data frame of either class <code>data.frame</code> or <code>rrpp.data.frame</code> . If null, the data frame from the <code>lm.rpp</code> fit will be used, effectively calculating all fitted values and their confidence intervals. If a numeric variable is missing from <code>newdata</code> , an attempt to average the values will be made in prediction; i.e., least squares means for factor levels can be found. All factors used in the <code>lm.rpp</code> fit should be represented in the <code>newdata</code> data frame, with appropriate factor levels.
block	An optional factor for blocks within which to restrict resampling permutations.
confidence	The desired confidence interval level for prediction.
...	Other arguments (currently none)

Author(s)

Michael Collyer

Examples

```
## Not run:
# See examples for lm.rpp to see how predict.lm.rpp works in conjunction
# with other functions

data(Pupfish)

# CS is centroid (fish) size
fit <- lm.rpp(coords ~ log(CS) + Sex*Pop,
SS.type = "I", data = Pupfish, iter = 999)

# Predictions (holding alternative effects constant)

shapeDF <- expand.grid(Sex = levels(Pupfish$Sex), Pop = levels(Pupfish$Pop))
rownames(shapeDF) <- paste(shapeDF$Sex, shapeDF$Pop, sep = ".")
shapeDF

shapePreds <- predict(fit, shapeDF)
summary(shapePreds)
summary(shapePreds, PC = TRUE)

shapePreds99 <- predict(fit, shapeDF, confidence = 0.99)
summary(shapePreds99, PC = TRUE)

# Plot prediction

plot(shapePreds, PC = TRUE)
plot(shapePreds, PC = TRUE, ellipse = TRUE)
plot(shapePreds99, PC = TRUE)
plot(shapePreds99, PC = TRUE, ellipse = TRUE)

## End(Not run)
```

```
prep.lda
```

Linear discriminant function for lm.rpp model fits

Description

Function creates arguments for `lda` or `qda` from a `lm.rpp` fit.

Usage

```
prep.lda(
  fit,
  tol = 1e-07,
  PC.no = NULL,
  newdata = NULL,
  inherent.groups = FALSE,
  ...
)
```

Arguments

<code>fit</code>	A linear model fit using <code>lm.rpp</code> .
<code>tol</code>	A tolerance used to decide if the matrix of data is singular. This value is passed onto both <code>lda</code> and <code>prcomp</code> , internally.
<code>PC.no</code>	An optional argument to define the specific number of principal components (PC) used in analysis. The minimum of this value or the number of PCs resulting from the <code>tol</code> argument will be used.
<code>newdata</code>	An optional matrix (or object coercible to a matrix) for classification. If <code>NULL</code> , all observed data are used.
<code>inherent.groups</code>	A logical argument in case one wishes to have the inherent groups in the model fit revealed. If <code>TRUE</code> , no other analysis will be done than to reveal the groups. This argument should always be <code>FALSE</code> to perform a classification analysis.
<code>...</code>	Arguments passed to <code>lda</code> . See <code>lda</code> for details

Details

This function uses a `lm.rpp` fit to produce the data and the groups to use in `lda` or `qda`. There are two general purposes of this function that are challenging when using `lda`, directly. First, this function finds the inherent groups in the `lm.rpp` fit, based on factor levels. Second, this function finds pseudodata - rather than the observed data - that involve either or both a principal component projection with appropriate (or user-prescribed) dimensions and a transformation. The principal component projection incorporates GLS mean-centering, where appropriate. Transformation involves holding non-grouping model terms constant. This is accomplished by using the fitted values from the `lm.rpp` fit and the residuals of a `lm.rpp` fit with grouping factors, alone. When, the `lm.rpp` fit contains only grouping factors, this function produces raw data projected on principal components.

Regardless of variables input, data are projected onto PCs. The purpose of this function is to predict group association, and working in PC space facilitates this objective.

This is a new function and not all limits and scenarios have been tested before its release. Please report any issues or limitations or strange results to the maintainer.

Notes for RRPP 0.5.0 and subsequent versions:

Prior to version 0.5.0, the function, `classify`, was available. This function has been deprecated. It mimicked `lda` with added features that are largely retained with `prep.lda`. However, `prep.lda` facilitates the much more diverse options available with `lda`.

Value

A list of arguments that can be passed to `lda`. As a minimum, these arguments include `$x`, `$grouping`, and `$tol`. If `newdata` is not `NULL`, `$newdata`, using the same transformation and PCs as for the data, will also be included.

Author(s)

Michael Collyer

See Also

`lda`, `predict.lda`, `qda`, `predict.qda`

Examples

```
# Using the Pupfish data (see lm.rrpp help for more detail)

data(Pupfish)
Pupfish$logSize <- log(Pupfish$CS)
fit <- lm.rrpp(coords ~ logSize + Sex * Pop, SS.type = "I",
data = Pupfish, print.progress = FALSE, iter = 0)

prep.lda(fit, inherent.groups = TRUE) # see groups available
lda.args <- prep.lda(fit, CV = TRUE, PC.no = 6)
lda.args$x
lda.args$grouping

# not run:
# library(MASS)
# LDA <- do.call(lda, lda.args)
# LDA$posterior
# table(lda.args$grouping, LDA$class)
```

print.anova.lm.rppp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'anova.lm.rppp'  
print(x, ...)
```

Arguments

x print/summary object (from [lm.rppp](#))
... other arguments passed to print/summary

Author(s)

Michael Collyer

print.coef.lm.rppp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'coef.lm.rppp'  
print(x, ...)
```

Arguments

x Object from [coef.lm.rppp](#)
... Other arguments passed onto coef.lm.rppp

Author(s)

Michael Collyer

print.ICCstats *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'ICCstats'  
print(x, ...)
```

Arguments

x print/summary object (from [ICCstats](#))
... other arguments passed to print/summary

Author(s)

Michael Collyer

print.lm.rpp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'lm.rpp'  
print(x, ...)
```

Arguments

x print/summary object (from [lm.rpp](#))
... other arguments passed to print/summary

Author(s)

Michael Collyer

print.looCV *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'looCV'  
print(x, ...)
```

Arguments

x Object from [looCV](#)
... Other arguments passed onto print.looCV

Author(s)

Michael Collyer

print.lr_test *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'lr_test'  
print(x, ...)
```

Arguments

x Object from [lr_test](#)
... Other arguments passed onto print.lr_test

Author(s)

Michael Collyer

```
print.measurement.error
```

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'measurement.error'  
print(x, ...)
```

Arguments

x	Object from <code>measurement.error</code>
...	Other arguments passed onto <code>measurement.error</code>

Author(s)

Michael Collyer

Examples

```
## Not run:  
  
# Measurement error analysis on simulated data of fish shapes  
  
data(fishy)  
  
# Analysis unconcerned with groups  
  
ME1 <- measurement.error(  
  Y = "coords",  
  subjects = "subj",  
  replicates = "reps",  
  data = fishy)  
  
anova(ME1)  
ICCstats(ME1, subjects = "Subjects", with_in = "Systematic ME")  
plot(ME1)  
  
# Analysis concerned with groups  
  
ME2 <- measurement.error(  
  Y = "coords",  
  subjects = "subj",  
  replicates = "reps",  
  groups = "groups",
```

```

data = fishy)

anova(ME2)
ICCstats(ME2, subjects = "Subjects",
  with_in = "Systematic ME", groups = "groups")
P <- plot(ME2)
focusMEonSubjects(P, subjects = 18:20, shadow = TRUE)

## End(Not run)

```

```
print.model.comparison
```

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'model.comparison'
print(x, ...)
```

Arguments

x	Object from model.comparison
...	Other arguments passed onto model.comparison

Author(s)

Michael Collyer

```
print.ordinate
```

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'ordinate'
print(x, ...)
```

Arguments

x Object from [ordinate](#)
 ... Other arguments passed onto print.ordinate

Author(s)

Michael Collyer

print.pairwise *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'pairwise'
print(x, ...)
```

Arguments

x Object from [pairwise](#)
 ... Other arguments passed onto pairwise

Author(s)

Michael Collyer

print.predict.lm.rppp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'predict.lm.rppp'
print(x, PC = FALSE, ...)
```

Arguments

x Object from [predict.lm.rppp](#)
 PC Logical argument for whether to use predicted values rotated to their PCs
 ... Other arguments passed onto predict.lm.rppp

Author(s)

Michael Collyer

`print.summary.lm.rppp` *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'summary.lm.rppp'  
print(x, ...)
```

Arguments

x print/summary object (from [summary.lm.rppp](#))
... other arguments passed to print/summary

Author(s)

Michael Collyer

`print.summary.manova.lm.rppp`
Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'summary.manova.lm.rppp'  
print(x, ...)
```

Arguments

x Object from [summary.manova.lm.rppp](#)
... Other arguments passed onto `summary.manova.lm.rppp`

Author(s)

Michael Collyer

```
print.summary.ordinate
```

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'summary.ordinate'  
print(x, ...)
```

Arguments

x	Object from summary.ordinate
...	Other arguments passed onto print.ordinate

Author(s)

Michael Collyer

```
print.summary.pairwise
```

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'summary.pairwise'  
print(x, ...)
```

Arguments

x	Object from summary.pairwise
...	Other arguments passed onto summary.pairwise

Author(s)

Michael Collyer

```
print.summary.trajectory.analysis
    Print/Summary Function for RRPP
```

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'summary.trajectory.analysis'
print(x, ...)
```

Arguments

x	Object from summary.trajectory.analysis
...	Other arguments passed onto summary.trajectory.analysis

Author(s)

Michael Collyer

```
print.trajectory.analysis
    Print/Summary Function for RRPP
```

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'trajectory.analysis'
print(x, ...)
```

Arguments

x	Object from trajectory.analysis
...	Other arguments passed onto

Author(s)

Michael Collyer

Pupfish

Landmarks on pupfish

Description

Landmark data from *Cyprinodon pecosensis* body shapes, with indication of Sex and Population from which fish were sampled (Marsh or Sinkhole).

Details

These data were previously aligned with GPA. Centroid size (CS) is also provided. See the **geomorph** package for details.

Author(s)

Michael Collyer

References

Collyer, M.L., D.J. Sekora, and D.C. Adams. 2015. A method for analysis of phenotypic change for phenotypes described by high-dimensional data. *Heredity*. 113: doi:10.1038/hdy.2014.75.

PupfishHeads

Landmarks on pupfish heads

Description

Landmark data from *Cyprinodon pecosensis* head shapes, with variables for sex, month and year sampled, locality, head size, and coordinates of landmarks for head shape, per specimen. These data are a subset of a larger data set.

Details

The variable, "coords", are data that were previously aligned with GPA. The variable, "headSize", is the Centroid size of each vector of coordinates. See the **geomorph** package for details.

Author(s)

Michael Collyer

References

Gilbert, M.C. 2016. Impacts of habitat fragmentation on the cranial morphology of a threatened desert fish (*Cyprinodon pecosensis*). Masters Thesis, Western Kentucky University.

pval *Obtain P-value from a vector of values*

Description

A function to find the probability of values greater or lesser than target, from a vector of values presumably obtained in random permutations.

Usage

```
pval(s, target = NULL, greater = TRUE)
```

Arguments

s	The sampling distribution vector to use.
target	The value to target in the distribution. (If null, the first value in the vector is used.) If the target exists outside the range of s, a probability of 0 or 1 is certain.
greater	Logical value for whether the probability should be "greater than or equal to". Change to greater = FALSE for "less than or equal to".

Author(s)

Michael Collyer

QRforX *QR decomposition of linear model design matrices*

Description

This function performs a QR decomposition (factorization) on a linear model design matrix (X) and returns useful results for subsequent analysis. This is intended as an internal function but can be used externally. Because base::qr and Matrix::qr have different options for QR algorithms, this function assures that results are consistent for other RRPP function use, whether X is a dense or sparse matrix.

Usage

```
QRforX(X, returnQ = TRUE, reduce = TRUE, reQR = TRUE, ...)
```

Arguments

X	A linear model design matrix, but can be any object coercible to matrix.
returnQ	A logical value whether to return the Q matrix. Generating a Q matrix can be computationally intense for large matrices. If it is not explicitly needed, this argument can be FALSE.
reduce	A logical value for whether redundant parameters in X should be removed. This should be TRUE (default) for most cases.
reQR	A logical value for whether to re-perform QR if reduce = TRUE, and X has been reduced.
...	Further arguments passed to base::qr.

Value

An object of class QR is a list containing the following:

Q	The Q matrix, if requested.
R	The R matrix.
X	The X matrix, which could be changes from dense to sparse, or vice versa, and redundant columns removed.
rank	The rank of the X matrix.
fix	Logical value for whether redundant columns were removed form X. TRUE means columns were removed.
S4	Logical value for whether Q, R, and X are S4 class objects.

Author(s)

Michael Collyer

Examples

```
## Simple Example
data(Pupfish)
fit <- lm.rpp(coords ~ Pop, data = Pupfish, print.progress = FALSE)
QR <- QRforX(model.matrix(fit))
QR$Q
QR$R
QR$rank
QR$S4

## Not run, but one could get base::qr and Matrix::qr results as

# base::qr(as.matrix(QR$X))
# Matrix::qr(QR$X)

## Complex example

data("PupfishHeads")
fit <- suppressWarnings(lm.rpp(headSize ~ sex +
```

```
locality/year, data = PupfishHeads))
X <- model.matrix(fit)
dim(X) # Already reduced
colnames(X)
X <- model.matrix(terms(fit), fit$LM$data)
dim(X) # Retains redundant parameters
colnames(X)
QR <- QRforX(X)
QR$fixed
dim(QR$X) # Reduced again
colnames(QR$X)
```

residuals.lm.rpp *Extract residuals*

Description

Extract residuals

Usage

```
## S3 method for class 'lm.rpp'
residuals(object, ...)
```

Arguments

object	plot object (from lm.rpp)
...	Arguments passed to other functions

Author(s)

Michael Collyer

Examples

```
# See examples for lm.rpp
```

reveal.model.designs *Reveal model designs used in lm.rrpp fit*

Description

Function returns every full and reduced model for model terms used in lm.rrpp fits. This function is useful for revealing the null and full model that would be used in the pairwise function, if a specific null model is not declared as an argument (fit.null in the [pairwise](#) function). It also helps to demonstrate how sums of squares and cross-products (SSCP) are calculated in lm.rrpp permutations (iterations), from the difference between fitted values for null and full designs.

Usage

```
reveal.model.designs(fit)
```

Arguments

fit A linear model fit from [lm.rrpp](#).

Author(s)

Michael Collyer

Examples

```
data(Pupfish)
fit1 <- lm.rrpp(coords~ Pop*Sex, data = Pupfish,
SS.type = "I", print.progress = FALSE, iter = 0)
fit2 <- lm.rrpp(coords~ Pop*Sex, data = Pupfish,
SS.type = "II", print.progress = FALSE, iter = 0)
fit3 <- lm.rrpp(coords~ Pop*Sex, data = Pupfish,
SS.type = "III", print.progress = FALSE, iter = 0)

reveal.model.designs(fit1)
reveal.model.designs(fit2)
reveal.model.designs(fit3)
```

rrpp.data.frame *Create a data frame for lm.rrpp analysis*

Description

Create a data frame for lm.rrpp analysis, when covariance or distance matrices are used

Usage

```
rrpp.data.frame(...)
```

Arguments

```
...           Components (objects) to combine in the data frame.
```

Details

This function is not much different than `data.frame` but is more flexible to allow distance matrices and covariance matrices to be included. Essentially, this function creates a list, much like an object of class `data.frame` is also a list. However, `rrpp.data.frame` is less concerned with coercing the list into a matrix and more concerned with matching the number of observations (`n`). It is wise to use this function with any `lm.rrpp` analysis so that `lm.rrpp` does not have to search the global environment for needed data.

It is assumed that multiple data sets for the same subjects are in the same order.

See `lm.rrpp` for examples.

Author(s)

Michael Collyer

Examples

```
# Why use a rrpp.data.frame?
y <- matrix(rnorm(30), 10, 3)
x <- rnorm(10)
df <- data.frame(x = x, y = y)
df
rdf <- rrpp.data.frame(x = x, y = y)
rdf # looks more like a list

is.list(df)
is.list(rdf)

d <- dist(y) # distance matrix as data

# One can try this but it will result in an error
# df <- data.frame(df, d = d)
rdf <- rrpp.data.frame(rdf, d = d) # works

fit <- lm.rrpp(d ~ x, data = rdf, iter = 99)
summary(fit)
```

`scaleCov`*Scaling of a Covariance Matrix*

Description

Function performs linear and exponential scaling of a covariance, either including or excluding diagonals or off-diagonal elements.

Usage

```
scaleCov(  
  Cov,  
  scale. = 1,  
  exponent = 1,  
  scale.diagonal = FALSE,  
  scale.only.diagonal = FALSE  
)
```

Arguments

<code>Cov</code>	Square matrix to be scaled.
<code>scale.</code>	The linear scaling parameter. Values are multiplied by this numeric value.
<code>exponent</code>	The exponentiation scaling parameter. Values are raised to this power.
<code>scale.diagonal</code>	Logical to indicate if diagonal should be included.
<code>scale.only.diagonal</code>	Logical to indicate if only the diagonal should be scaled.

Details

The function scales covariances as $\text{scale} * \text{cov}^{\text{exponent}}$, where `cov` is any covariance or variance in the covariance matrix. Arguments allow inclusion or exclusion of either the diagonal or off-diagonal elements to be scaled. It is assumed that a covariance matrix is scaled, but any square matrix will work.

Value

A square matrix.

Author(s)

Michael Collyer

Examples

```

## Not run:
data(Pupfish)
Pupfish$logSize <- log(Pupfish$CS)
fit1 <- lm.rrpp(coords ~ logSize, data = Pupfish, iter = 0,
print.progress = FALSE)
fit2 <- lm.rrpp(coords ~ Pop, data = Pupfish, iter = 0,
print.progress = FALSE)
fit3 <- lm.rrpp(coords ~ Sex, data = Pupfish, iter = 0,
print.progress = FALSE)
fit4 <- lm.rrpp(coords ~ logSize + Sex, data = Pupfish, iter = 0,
print.progress = FALSE)
fit5 <- lm.rrpp(coords ~ logSize + Pop, data = Pupfish, iter = 0,
print.progress = FALSE)
fit6 <- lm.rrpp(coords ~ logSize + Sex * Pop, data = Pupfish, iter = 0,
print.progress = FALSE)

modComp1 <- model.comparison(fit1, fit2, fit3, fit4, fit5,
fit6, type = "cov.trace")
modComp2 <- model.comparison(fit1, fit2, fit3, fit4, fit5,
fit6, type = "logLik", tol = 0.01)

summary(modComp1)
summary(modComp2)

par(mfcol = c(1,2))
plot(modComp1)
plot(modComp2)

# Comparing fits with covariance matrices
# an example for scaling a phylogenetic covariance matrix with
# the scaling parameter, lambda

data("PlethMorph")
Cov <- PlethMorph$PhyCov
lambda <- seq(0, 1, 0.1)

Cov1 <- scaleCov(Cov, scale. = lambda[1])
Cov2 <- scaleCov(Cov, scale. = lambda[2])
Cov3 <- scaleCov(Cov, scale. = lambda[3])
Cov4 <- scaleCov(Cov, scale. = lambda[4])
Cov5 <- scaleCov(Cov, scale. = lambda[5])
Cov6 <- scaleCov(Cov, scale. = lambda[6])
Cov7 <- scaleCov(Cov, scale. = lambda[7])
Cov8 <- scaleCov(Cov, scale. = lambda[8])
Cov9 <- scaleCov(Cov, scale. = lambda[9])
Cov10 <- scaleCov(Cov, scale. = lambda[10])
Cov11 <- scaleCov(Cov, scale. = lambda[11])

fit1 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov1)
fit2 <- lm.rrpp(SVL ~ 1, data = PlethMorph, Cov = Cov2)

```

```

fit3 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov3)
fit4 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov4)
fit5 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov5)
fit6 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov6)
fit7 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov7)
fit8 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov8)
fit9 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov9)
fit10 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov10)
fit11 <- lm.rppp(SVL ~ 1, data = PlethMorph, Cov = Cov11)

par(mfrow = c(1,1))

MC1 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
  fit7, fit8, fit9, fit10, fit11,
  type = "logLik")
MC1
plot(MC1)

MC2 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
  fit7, fit8, fit9, fit10, fit11,
  type = "logLik", predictor = lambda)
MC2
plot(MC2)

MC3 <- model.comparison(fit1, fit2, fit3, fit4, fit5, fit6,
  fit7, fit8, fit9, fit10, fit11,
  type = "Z", predictor = lambda)
MC3
plot(MC3)

## End(Not run)

```

summary.anova.lm.rppp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```

## S3 method for class 'anova.lm.rppp'
summary(object, ...)

```

Arguments

object	Object from predict.lm.rppp
...	Other arguments passed onto predict.lm.rppp

Author(s)

Michael Collyer

summary.coef.lm.rpp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'coef.lm.rpp'  
summary(object, ...)
```

Arguments

object Object from [coef.lm.rpp](#)
... Other arguments passed onto coef.lm.rpp

Author(s)

Michael Collyer

summary.ICCstats *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'ICCstats'  
summary(object, ...)
```

Arguments

object print/summary object (from [ICCstats](#))
... other arguments passed to print/summary

Author(s)

Michael Collyer

summary.lm.rpp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'lm.rpp'
summary(object, formula = TRUE, ...)
```

Arguments

object	print/summary object (from lm.rpp)
formula	Logical argument for whether to include formula in summary table
...	other arguments passed to print/summary

Author(s)

Michael Collyer

summary.looCV *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'looCV'
summary(object, ...)
```

Arguments

object	Object from looCV
...	Other arguments passed onto print.looCV

Author(s)

Michael Collyer

summary.lr_test *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'lr_test'
summary(object, ...)
```

Arguments

object Object from [lr_test](#)
 ... Other arguments passed onto print.lr_test

Author(s)

Michael Collyer

summary.manova.lm.rppp *Print/Summary Function for RRPP*

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'manova.lm.rppp'
summary(object, test = c("Roy", "Pillai", "Hotelling-Lawley", "Wilks"), ...)
```

Arguments

object Object from [lm.rppp](#), updated with [manova.update](#)
 test Type of multivariate test statistic to use.
 ... Other arguments passed onto manova.lm.rppp

Author(s)

Michael Collyer

summary.measurement.error

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'measurement.error'  
summary(object, ...)
```

Arguments

object	Object from measurement.error
...	Other arguments passed onto measurement.error

Author(s)

Michael Collyer

summary.model.comparison

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'model.comparison'  
summary(object, ...)
```

Arguments

object	Object from model.comparison
...	Other arguments passed onto model.comparison

Author(s)

Michael Collyer

summary.ordinate	<i>Print/Summary Function for RRPP</i>
------------------	--

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'ordinate'  
summary(object, ...)
```

Arguments

object	Object from ordinate
...	Other arguments passed onto print.ordinate

Author(s)

Michael Collyer

summary.pairwise	<i>Print/Summary Function for RRPP</i>
------------------	--

Description

See [pairwise](#) for further description.

Usage

```
## S3 method for class 'pairwise'  
summary(  
  object,  
  stat.table = TRUE,  
  test.type = c("dist", "stdist", "mdist", "VC", "DL", "var"),  
  angle.type = c("rad", "deg"),  
  confidence = 0.95,  
  show.vectors = FALSE,  
  ...  
)
```

Arguments

object	Object from pairwise
stat.table	Logical argument for whether results should be returned in one table (if TRUE) or separate pairwise tables (if FALSE)
test.type	the type of statistic to test. See below should be used in the test.
angle.type	If test.type = "VC", whether angle results are expressed in radians or degrees.
confidence	Confidence level to use for upper confidence limit; default = 0.95 (alpha = 0.05)
show.vectors	Logical value to indicate whether vectors should be printed.
...	Other arguments passed onto pairwise

Details

The following summarize the test that can be performed:

Distance between vectors, "dist" Vectors for LS means or slopes originate at the origin and point to some location, having both a magnitude and direction. A distance between two vectors is the inner-product of the vector difference, i.e., the distance between their endpoints. For LS means, this distance is the difference between means. For multivariate slope vectors, this is the difference in location between estimated change for the dependent variables, per one-unit change of the covariate considered. For univariate slopes, this is the absolute difference between slopes.

Standardized distance between vectors, "stdist" Same as the distance between vectors, but distances are divided by the model standard error (square-root of the trace of the residual covariance matrix). Pairwise tests with this statistic should be consistent with ANOVA results.

Mahalanobis distance between vectors, "mdist" Similar to the standardized distance between vectors but the inverse of the residual covariance matrix is used in calculation of the distance, rather than dividing the Euclidean distance between means and dividing by the standard error. If the residual covariance matrix is singular, Mahalanobis distances will not be calculated. Pairwise tests with this statistic should be consistent with MANOVA results.

Vector correlation, "VC" If LS mean or slope vectors are scaled to unit size, the vector correlation is the inner-product of the scaled vectors. The arccosine (acos) of this value is the angle between vectors, which can be expressed in radians or degrees. Vector correlation indicates the similarity of vector orientation, independent of vector length.

Difference in vector lengths, "DL" If the length of a vector is an important attribute – e.g., the amount of multivariate change per one-unit change in a covariate – then the absolute value of the difference in vector lengths is a practical statistic to compare vector lengths. Let d_1 and d_2 be the distances (length) of vectors. Then $|d_1 - d_2|$ is a statistic that compares their lengths.

Variance, "var" Vectors of residuals from a linear model indicate can express the distances of observed values from fitted values. Mean squared distances of values (variance), by group, can be used to measure the amount of dispersion around estimated values for groups. Absolute differences between variances are used as test statistics to compare mean dispersion of values among groups. Variance degrees of freedom equal n , the group size, rather than $n-1$, as the purpose is to compare mean dispersion in the sample. (Additionally, tests with one subject in a group are possible, or at least not a hindrance to the analysis.)

The argument, `test.type` is used to select one of the tests above. See [pairwise](#) for examples.

Notes for RRPP 0.6.2 and subsequent versions:

In previous versions of pairwise, `summary.pairwise` had three test types: "dist", "VC", and "var". When one chose "dist", for LS mean vectors, the statistic was the inner-product of the vector difference. For slope vectors, "dist" returned the absolute value of the difference between vector lengths, which is "DL" in 0.6.2 and subsequent versions. This update uses the same calculation, irrespective of vector types. Generally, "DL" is the same as a contrast in rates for slope vectors, but might not have much meaning for LS means. Likewise, "dist" is the distance between vector endpoints, which might make more sense for LS means than slope vectors. Nevertheless, the user has more control over these decisions with version 0.6.2 and subsequent versions.

Notes for RRPP 2.0.4 and subsequent versions:

The test types, standardized distance between vectors, "stdist", and Mahalanobis distances between vectors were added. The former simply divides the distance between vectors by model standard error (square-root of the trace of the residual covariance matrix). This is a multivariate generalization of a t-statistic for the difference between means. It is not the same as Hotelling squared-T-statistic, which requires incorporating the inverse of the residual covariance matrix in the calculation of the distance, a calculation that also requires a non-singular covariance matrix. However, the Mahalanobis distances are similar (and proportional) to the Hotelling squared-T-statistic. Pairwise tests using Mahalanobis distances represent a non-parametric analog to the parametric Hotelling squared-T test. Both tests should be better for GLS model fits compared to Euclidean distances between means, as the total sums of squares are more likely to vary across random permutations. In general, if ANOVA is performed a pairwise test with "stdist" is a good association; if MANOVA is performed, a pairwise test with "mdist" is a good association.

Author(s)

Michael Collyer

summary.predict.lm.rppp

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'predict.lm.rppp'
summary(object, ...)
```

Arguments

object	Object from <code>predict.lm.rppp</code>
...	Other arguments passed onto <code>predict.lm.rppp</code>

Author(s)

Michael Collyer

summary.trajectory.analysis

Print/Summary Function for RRPP

Description

Print/Summary Function for RRPP

Usage

```
## S3 method for class 'trajectory.analysis'
summary(
  object,
  stat.table = TRUE,
  attribute = c("MD", "TC", "SD"),
  angle.type = c("rad", "deg"),
  confidence = 0.95,
  show.trajectories = FALSE,
  ...
)
```

Arguments

object	Object from trajectory.analysis
stat.table	Logical argument for whether results should be returned in one table (if TRUE) or separate pairwise tables (if FALSE)
attribute	Whether magnitude differences (MD, absolute difference in trajectory path lengths), trajectory correlations (TC), or trajectory shape differences (SD) are summarized.
angle.type	If attribute = "TC", whether angle results are expressed in radians or degrees.
confidence	Confidence level to use for upper confidence limit; default = 0.95 (alpha = 0.05)
show.trajectories	Logical value to indicate whether trajectories should be printed.
...	Other arguments passed onto trajectory.analysis

Author(s)

Michael Collyer

terms.lm.rpp	<i>Extract the terms from an lm.rpp object</i>
--------------	--

Description

terms.lm.rpp returns the terms constructed for an lm.rpp object.

Usage

```
## S3 method for class 'lm.rpp'  
terms(x, ...)
```

Arguments

x	Object from lm.rpp
...	further arguments passed to or from other methods

Author(s)

Michael Collyer

trajectory.analysis	<i>Quantify and compare shape change trajectories</i>
---------------------	---

Description

Function estimates attributes of multivariate trajectories

Usage

```
trajectory.analysis(  
  fit,  
  fit.null = NULL,  
  groups,  
  traj.pts,  
  pca = TRUE,  
  print.progress = FALSE  
)
```

Arguments

<code>fit</code>	A linear model fit using <code>lm.rpp</code> .
<code>fit.null</code>	An alternative linear model fit to use as a null model for RRPP, if the null model of the fit is not desired. Note, if RRPP = FALSE (FRPP rather than RRPP), then the null model has only an intercept. If the null model is uncertain, using <code>reveal.model.designs</code> will help elucidate the inherent null model used.
<code>groups</code>	A factor or vector coercible to factor that defines trajectories.
<code>traj.pts</code>	Either a single value or a vector coercible to factor to define trajectory points. If only a single value, it is assumed that the data are already in the form, <code>y1p1, y2p1, y3p1, ..., y2p2, y3p2, ..., yjp1, yjp2, yjp3, ..., yjpk</code> , for <code>j</code> variables comprising <code>k</code> trajectory points; i.e., <code>traj.pts = k</code> . If a factor, then a group * traj.pt factorial model is assumed, where <code>traj.pts</code> defines the levels for points within groups.
<code>pca</code>	A logical value to optionally project group:point means onto principal components (perform PCA on a covariance matrix of the means) This option only applies to factorial designs (<code>traj.pts</code> is a factor).
<code>print.progress</code>	A logical value to indicate whether a progress bar should be printed to the screen. This is helpful for long-running analyses.

Details

The function quantifies multivariate trajectories from a set of observations, and assesses variation in attributes of the trajectories via RRPP. A trajectory is defined by a sequence of points in the data space. These trajectories can be quantified for various attributes (their size, orientation, and shape), and comparisons of these attribute enable the statistical comparison of shape change trajectories (Collyer and Adams 2007; Adams and Collyer 2007; Adams and Collyer 2009; Turner et al. 2010; Collyer and Adams 2013).

This function is a modified version of `pairwise`, retaining the least squares (LS) means as trajectory points. Analysis starts with a `lm.rpp` fit (but a `procD.lm` fit from `geomorph` can also be used). LS means are calculated using a grouping variable. Data can be trajectories, as a start (sensu Adams and Cerney 2007), or trajectories can be calculated from data using a factorial model (in which case trajectory points are defined by factor levels).

This function produces statistics that can be summarized with the `summary.trajectory.analysis` function. The summaries are consistent with those in the `summary.pairwise` function, pertaining to trajectory attributes including, magnitude difference (MD), the difference in path lengths of trajectories; trajectory correlations (TC), better thought of as angular differences between trajectory principal axes; and if trajectories have three or more points, shape difference (SD), the square root of summed squared point differences, after scaling, centering, and rotating trajectories. The SD is the "Procrustes" distance between trajectories (Adams and Collyer 2009), much the same way as the shape difference between anatomical landmark configurations in geometric morphometrics. If attribute = "TC" is chosen for the summary, then the angle type ("rad" or "deg"), can be chosen for either radians and degrees, respectively, to return angles between principal axes.)

Plotting can be performed with `plot.trajectory.analysis` and `add.trajectories`. The former plots all principal component scores for the data, and allows point-by-point control of plot parameters. The later adds trajectories points and lines, with constrained control. By saving the

plot.trajectory.analysis object, plotting information can be retained and advanced plotting can be performed. See examples below.

Value

An object of class "trajectory.analysis" returns a list of the following:

LS.means	LS.means from pairwise function.
trajectories	Trajectories from every permutation.
PD	Path distances of trajectories from every permutation.
MD	Magnitude differences between trajectories from every permutation.
TC	Trajectory correlations from every permutation.
SD	Trajectory shape differences from every permutation.

Author(s)

Dean Adams and Michael Collyer

References

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Examples

```
## Not run:
### Analysis of sexual dimorphism vectors (factorial approach)
data(Pupfish)
fit <- lm.rpp(coords ~ Pop * Sex, data = Pupfish, iter = 199)
reveal.model.designs(fit)
TA <- trajectory.analysis(fit, groups = Pupfish$Pop,
traj.pts = Pupfish$Sex, print.progress = FALSE)

# Magnitude difference (absolute difference between path distances)
summary(TA, attribute = "MD")

# Correlations (angles) between trajectories
summary(TA, attribute = "TC", angle.type = "deg")
```

```

# No shape differences between vectors
summary(TA, attribute = "SD")

# Retain results
TA.summary <- summary(TA, attribute = "MD")
TA.summary$summary.table

# Plot results
TP <- plot(TA, pch = as.numeric(Pupfish$Pop) + 20, bg = as.numeric(Pupfish$Sex),
cex = 0.7, col = "gray")
add.trajectories(TP, traj.pch = c(21, 22), start.bg = 1, end.bg = 2)
legend("topright", levels(Pupfish$Pop), pch = c(21, 22), pt.bg = 1)

### Analysis when data are already trajectories (motion paths)

# data are planar Cartesian coordinates (x, y) across 5 points (10 variables)
data(motionpaths)
fit <- lm.rrpp(trajectories ~ groups, data = motionpaths, iter = 199)
TA <- trajectory.analysis(fit, groups = motionpaths$groups, traj.pts = 5)

# Magnitude difference (absolute difference between path distances)
summary(TA, attribute = "MD")

# Correlations (angles) between trajectories
summary(TA, attribute = "TC", angle.type = "deg")

# Shape differences between trajectories
summary(TA, attribute = "SD")

TP <- plot(TA, pch = 21, bg = as.numeric(motionpaths$groups),
cex = 0.7, col = "gray")
add.trajectories(TP, traj.pch = 21, traj.bg = 1:4)

## End(Not run)

```

vec.cor.matrix

Support function for RRPP

Description

Calculate vector correlations for a matrix (by rows). Used for pairwise comparisons.

Usage

```
vec.cor.matrix(M)
```

Arguments

M Matrix for vector correlations.

Author(s)

Michael Collyer

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